

Show all necessary steps for full marks.**Question 1: (5 points)(Textbook P.2 Exercise 32):** Find the following

(a): $\frac{2}{\frac{2}{3}} - \frac{\frac{2}{3}}{2} = ?$

(b): $\frac{\frac{2}{5} + \frac{1}{2}}{\frac{1}{10} + \frac{3}{15}} = ?$

Solution:

32. (a) $\frac{2}{\frac{2}{3}} - \frac{\frac{2}{3}}{2} = 2 \cdot \frac{3}{2} - \frac{2}{3} \cdot \frac{1}{2} = 3 - \frac{1}{3} = \frac{9}{3} - \frac{1}{3} = \frac{8}{3}$

(b) $\frac{\frac{2}{5} + \frac{1}{2}}{\frac{1}{10} + \frac{3}{15}} = \frac{\frac{2}{5} + \frac{1}{2}}{\frac{1}{10} + \frac{1}{5}} = \frac{\frac{2}{5} + \frac{1}{2}}{\frac{1}{10} + \frac{1}{5}} \cdot \frac{10}{10} = \frac{4+5}{1+2} = \frac{9}{3} = 3$

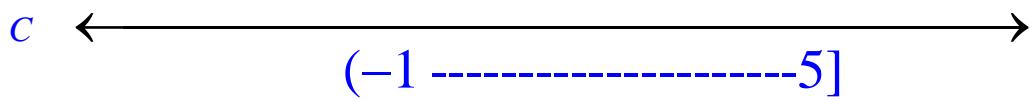
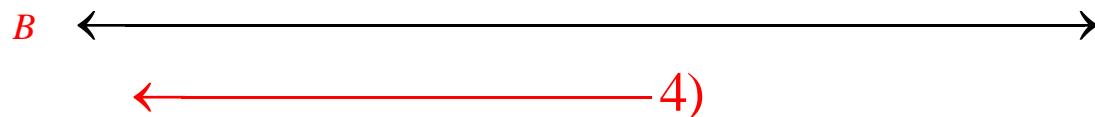
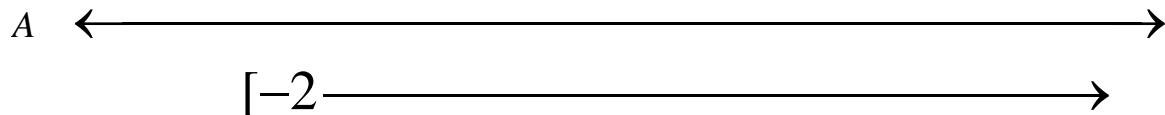
Question 2: (5 points)(Textbook P.2 Exercises 45 and 46): If $A = \{x | x \geq -2\}$, $B = \{x | x < 4\}$ and $C = \{x | -1 < x \leq 5\}$, then find

(a): $B \cup C = ?$

(b): $B \cap C = ?$

(c): $A \cup C = ?$

(d): $A \cap C = ?$

Solution:

(a) $B \cup C = \{x | x \leq 5\}$

(b) $B \cap C = \{x | -1 < x < 4\}$

(c) $A \cup C = \{x | x \geq -2\} = [-2, \infty) = A$

(d) $A \cap C = \{x | -1 < x \leq 5\} = (-1, 5]$

Question 3: (5 points): Find the value of the expression $-17 + 3[8x - 4(3x - 2)]$ when $x = -\frac{3}{4}$

Solution:

$$\begin{aligned}
 -17 + 3[8x - 4(3x - 2)] &= -17 + 3[8x - 12x + 8] \\
 &= -17 + 3[-4x + 8] \\
 &= -17 + 3\left[(-4)\left(-\frac{3}{4}\right) + 8\right] \\
 &= -17 + 3[3 + 8] \\
 &= -17 + 33 \\
 &= 16
 \end{aligned}$$

Question 4: (5 points): If $-3 < x < -1$, then write the expression $|3+x| + |2+2x| + \|-x\|$ without the absolute value symbols.

Solution: $x > -3 \Rightarrow x + 3 > 0 \Rightarrow |x + 3| = x + 3$
 $x < -1 \Rightarrow x + 1 < 0 \Rightarrow 2 + 2x < 0 \Rightarrow |2 + 2x| = -(|2 + 2x|) = -2 - 2x$
 $\|-x\| = |x| = -x$

The expression $|3+x| + |2+2x| + \|-x\| = x + 3 - 2 - 2x - x = 1 - 2x$