King Fahd University of Petroleum and Minerals **Prep-Year Math Program**

Math (001)-Term (141) **Recitation R.7**

Question1:

simplify the following:

(a)
$$\frac{\left(3\sqrt{x^2 - 2} - 2\sqrt{x^2 + 2}\right)\left(3\sqrt{x^2 - 2} + 2\sqrt{x^2 + 2}\right)}{\left(x\sqrt{5} + \sqrt{26}\right)}$$
 (b)
$$\sqrt{(x + y)^2 - 4xy}$$
 Answer: (a): $x\sqrt{5} - \sqrt{26}$ (b): $|x - y|$

$$(b)\sqrt{\left(x+y\right)^2-4xy}$$

(b):
$$|x - y|$$

Question2:

Find the value of

(a)
$$\frac{3}{\sqrt{5}-\sqrt{2}} - \frac{2}{3\sqrt{2}}$$

(a)
$$\frac{3}{\sqrt{5} - \sqrt{2}} - \frac{2}{3\sqrt{2}}$$
 (b) $\frac{2}{\sqrt[3]{54}} + \frac{4}{\sqrt[3]{16}} - \frac{1}{\sqrt[3]{2}}$

$$(c)\frac{1}{\left|2-\sqrt{5}\right|} + \frac{1}{\left|-2-\sqrt{5}\right|}$$

$$(c)\frac{1}{\left|2-\sqrt{5}\right|} + \frac{1}{\left|-2-\sqrt{5}\right|} \qquad (d)\frac{\sqrt[13]{\left(-2\right)^{13}} - \sqrt[10]{\left(-2\right)^{10}}}{\sqrt{2}-1}$$

Answer: (a): $\sqrt{5} + \frac{2\sqrt{2}}{3}$ (b): $\frac{5\sqrt[3]{4}}{6}$ (c): $2\sqrt{5}$ (d): $-4(\sqrt{2}+1)$

(b):
$$\frac{5\sqrt[3]{4}}{6}$$

(c):
$$2\sqrt{5}$$

(d):
$$-4(\sqrt{2}+1)$$

Question3:

let $x = 7 + 3\sqrt{2}$ and $y = 7 - 3\sqrt{2}$ then one of the following is an integer

$$(a)x^2$$

$$(b)y^2$$

$$(c)\frac{x}{y}$$

$$(d)\frac{y}{x}$$

$$(e)x^2 + y^2$$

Answer: (e): $x^2 + y^2 = 67 + 42\sqrt{2} + 67 - 42\sqrt{2} = 134$ is an integer

Question4:

If a is any real number which of the following is TRUE

$$(a)\sqrt[4]{a^4} = |a|$$

$$(b)\sqrt[4]{a^2} = \sqrt{a}$$

$$(c)\sqrt[3]{a^3} = |a|$$

$$(d)\sqrt[7]{\sqrt[3]{a}} = a^{\frac{3}{7}}$$

$$(e)\sqrt[3]{a}\sqrt{a} = \sqrt[6]{a}$$

Answer: (a): TRUE (b): FALSE

(c): FALSE

(d): FALSE (e): FALSE