King Fahd University of Petroleum and Minerals

Prep-Year Math Program

Math (001)-Term (181)

Recitation P.7

Ouestion 1: Simplify the following rational expressions

(a):
$$\frac{2}{4+x} + \frac{16}{x^2-16} + \frac{6}{4-x}$$

(b):
$$\frac{4}{2-x} + \frac{5}{x^2 + 2x + 4} \div \frac{x^2 - 4x + 4}{x^3 - 8}$$

Answer: (a):
$$\frac{-4}{x-4}$$

(b):
$$\frac{1}{x-2}$$

Ouestion 2: Simplify

(a):
$$\frac{x^{-1} + (x+2)^{-1}}{x^{-1} - (x+2)^{-1}}$$

(b):
$$1 + \frac{1}{1 + \frac{1}{1 + x}}$$

Answer: (a): x + 1

Answer: (b):
$$\frac{2x+3}{x+2}$$

Question 3: The expression $\frac{2x^2 - 3x - 2}{x^2 - 1}$ simplifies to

(a)
$$\frac{x+1}{x-2}$$

(b)
$$\frac{x-2}{x+1}$$

(a)
$$\frac{x+1}{x-2}$$
 (b) $\frac{x-2}{x+1}$ (c) $\frac{2x+1}{x+2}$ (d) $\frac{x+2}{2x+1}$ (e) $\frac{x+2}{x-1}$

(d)
$$\frac{x+2}{2x+1}$$

(e)
$$\frac{x+2}{x-1}$$

Answer: (b)

Question 4: Simplify the following expression:

Answer:
$$\frac{1}{(1-x^2)^{3/2}} = \frac{(1-x^2)^{\frac{1}{2}}}{(1-x^2)^2}$$

Question 5: Rationalize the denominator of $\frac{2x-2y}{\sqrt{x}-\sqrt{y}}$

Answer: $2(\sqrt{x} + \sqrt{y})$

Question 6: Find the domain of (a): $\frac{\sqrt{x}}{x^2-3x-4}$ (b): $\frac{x^2-1}{x^2-x-2}$

(b):
$$\frac{x^2-1}{x^2-x-2}$$

Answer:

(a):
$$Domain = \{x \mid x \ge 0, x \ne 4\} = [0,4) \cup (4,\infty)$$

(b): $Domain = \{x \mid x \neq -1 \text{ and } x \neq 2\} = (-\infty, -1) \cup (-1, 2) \cup (2, \infty)$