

## Chapter 30 - Faraday's and Lenz's Laws

### Faraday's Law of Induction

Q1. Consider a circular loop of radius  $R = 20$  cm lying in the  $x$ - $y$  plane. There is throughout the region a uniform magnetic field given by:  $\mathbf{B} = (5.0\mathbf{i} + 4.0\mathbf{j} + 3.0\mathbf{k})$  T.

Calculate the magnetic flux through the loop. Ans:  $0.38 \text{ Tm}^2$

Q2. A uniform magnetic field  $\mathbf{B} = (2.0\mathbf{i} + 4.0\mathbf{j} + 5.0\mathbf{k})$  T intersects a circular surface of radius 2 cm lying in the  $yz$  plane. What is the magnetic flux through this surface? Ans:  $2.5 \times 10^{-3} \text{ Tm}^2$

Q3. Consider a cube of side  $L = 10$  cm positioned as shown in Figure 6. Throughout the region, There is a magnetic field  $\mathbf{B} = (4.0\mathbf{i} + 5.0\mathbf{j} - 6.0\mathbf{k})$  T. Calculate the magnetic flux through the shaded face of the cube. Ans:  $-0.06 \text{ Tm}^2$

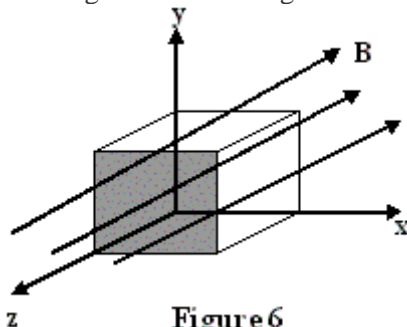


Figure 6

Q4. A constant magnetic flux of  $4.0 \times 10^{-5}$  Wb is maintained through a coil for 0.5 s. What emf is induced in the coil by this flux during that period? Ans: Zero.

Q5. A 2.0 Tesla uniform magnetic field makes an angle of 60 degrees with the  $xy$ -plane. The magnetic flux through an area of  $3 \text{ m}^2$  portion of the  $xy$ -plane is: Ans: 5.2 Wb.

Q6. Figure 12 shows a conducting loop consisting of a half circle of radius 0.20 m and three straight sections. The loop lies in a uniform magnetic field that is directed as shown in the figure and is given by:  $\mathbf{B} = 4.5t^2 - 10t$ , with  $B$  in tesla and  $t$  in seconds. What is the magnitude of the induced emf at  $t = 10$  s? Ans: 8.2 V

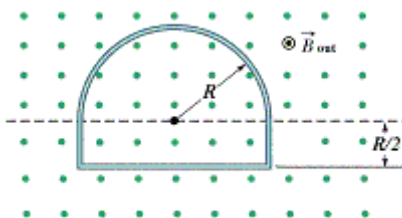


Figure 12

Q7. A 400-turn coil of total resistance 6.0 ohm has a cross sectional area of  $30 \text{ cm}^2$ . How rapidly should a magnetic field parallel to the coil axis change in order to induce a current of 0.3 A in the coil? Ans: 1.5 T/s.

Q8. A circular wire loop of area  $0.5 \text{ m}^2$  is perpendicular to a magnetic field of 0.8 T. If the coil is removed completely from the field in 0.1 s, the average emf induced in the loop has a magnitude: Ans: 4.0 V.

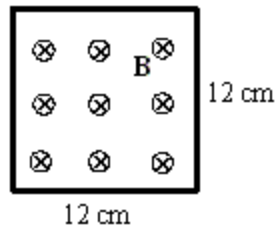
### Lenz's Law

Q9. A plane loop of wire consisting of a single turn of cross-sectional area  $0.20 \text{ m}^2$  is perpendicular to a magnetic field that increases uniformly in magnitude from 0.25 T to 3.25 T in a time of 2.0 s. What is the resistance of the coil if the induced current has a value of 2.0 A? Ans: 0.15 Ohm.

Q10. Each turn of a 100-turn coil, whose resistance is 60 Ohm, encloses an area of  $80 \text{ cm}^2$ . What should be the rate of change of a magnetic field parallel to its axes in order to induce a current of 1 mA in the coil? Ans: 0.075 T/s.

Q11. A flat coil of wire consisting of 20 turns, each with an area of  $50 \text{ cm}^2$ , is positioned perpendicularly to a uniform magnetic field that increases its magnitude at a constant rate from 2.0 T to 6.0 T in 2.0 s. If the coil has a total resistance of 0.4 ohms, what is the magnitude of the induced current in the coil? Ans: 0.5 A

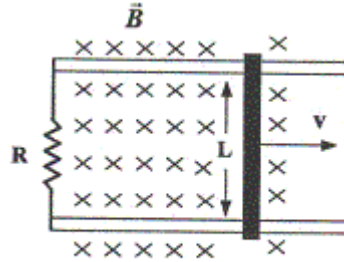
Q12. The square circuit shown in Figure 8 is in a uniform magnetic field directed into the page and is decreasing at a rate of 1.5 T/s. Calculate the induced current in the circuit if the resistance of the wire 10 ohms. Ans: 2.16 milli-A



**Figure 8**

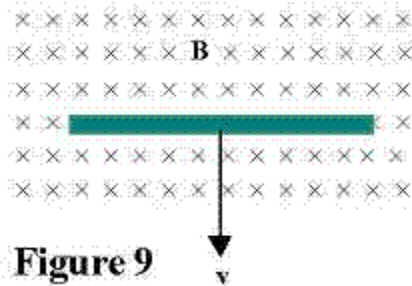
**Induction and Energy Transfers**

Q13. In the arrangement shown in Figure (7), a conducting bar moves to the right. Assume  $R=10\ \Omega$ ,  $L=0.5\ \text{m}$ , and that a uniform  $3.5\ \text{T}$  magnetic field is directed into the page. Neglect the mass of the bar, find the power dissipated in the resistor such that the bar moves to the right with a constant speed of  $4.0\ \text{m/s}$ ? Ans:  $4.9\ \text{W}$ .



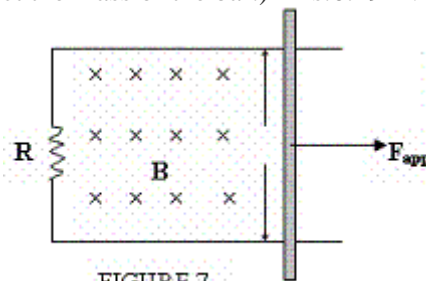
**Figure # 7**

Q14. A conducting rod of length  $1.2\ \text{m}$  is moving with a speed of  $10\ \text{m/s}$  as shown in Figure 9. If the magnetic field is  $0.55\ \text{T}$  into the page, calculate the potential difference between the ends of the rod. Ans:  $6.6\ \text{V}$



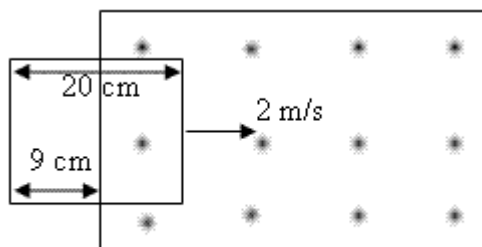
**Figure 9**

Q15. Figure 7 shows a conducting bar moving with a constant speed of  $5.0\ \text{m/s}$  to the right. Assume that  $R = 5.0\ \Omega$ ,  $L = 0.20\ \text{m}$ , and that a uniform magnetic field of  $3.5\ \text{T}$  is directed into the page. Calculate the magnitude of the applied force pulling the bar. (Neglect the mass of the bar.) Ans:  $0.49\ \text{N}$



**FIGURE 7**

Q16. The square coil shown in figure 12 is  $20\ \text{cm}$  on a side and has 15 turns of wire on it. It is moving to the right at  $2\ \text{m/s}$ . Find the induced emf in it at the instant shown, and the direction of the induced current in the coil. (The magnetic field is  $0.2\ \text{T}$  and its direction is out of the page.) Ans:  $1.2\ \text{V}$ , clockwise



**Figure 12**