## RECITATION 3 ch. 4

•22 A small ball rolls horizontally off the edge of a tabletop that is 1.20 m high. It strikes the floor at a point 1.52 m horizontally from the table edge. (a) How long is the ball in the air? (b) What is its speed at the instant it leaves the table?

a)

$$y - y_0 = v_{0y}t - \frac{1}{2}gt^2$$

With  $y = v_0 = 0$ ,

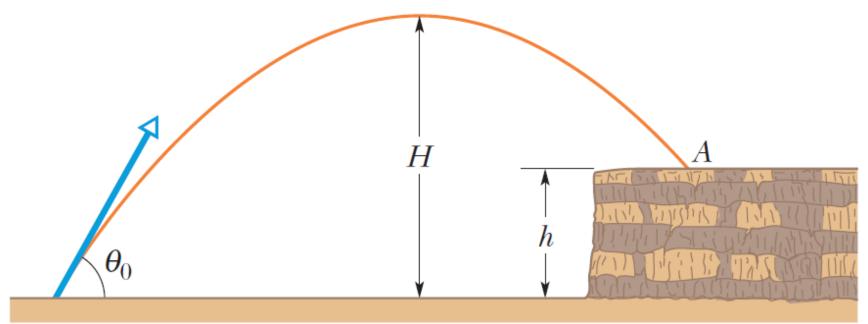
$$t = \sqrt{2y_0/g} = \sqrt{2(1.20)/9.81} = 0.495 \text{ s.}$$

b)

$$v_{x0} = \frac{\Delta x}{\Delta t} = \frac{1.20}{0.495} = 2.43 \frac{\text{m}}{\text{s}}.$$

$$v = \sqrt{v_{0x}^2 + v_{0y}^2} = \sqrt{(2.43)^2 + 0} = 2.43 \frac{\text{m}}{\text{s}}.$$

••28 In Fig. 4-34, a stone is projected at a cliff of height with an initial speed of 42.0 m/s directed at angle  $\theta_0 = 60.0^{\circ}$  above the horizontal. The stone strikes at A, 5.50 s after launching. Find (a) the height h of the cliff, (b) the speed of the stone just before impact at A, and (c) the maximum height H reached above the ground.



$$y - y_0 = v_{0y}t - \frac{1}{2}gt^2$$

With  $y_0 = 0$  and y = h,

$$h = v_{0y}t - \frac{1}{2}gt^2 = (42.0\sin 60.0^\circ)(5.50) - \frac{1}{2}(9.81)(5.50)^2$$
$$= 51.8 \text{ m}.$$

b)

$$v_y = v_{0y} - gt = 42.0 \sin 60.0^{\circ} - (9.81)(5.50) = -17.6 \text{ m/s}$$
  
$$v_x = v_{0x} = 42.0 \cos 60.0^{\circ} = 21.0 \text{ m/s}.$$

$$v = \sqrt{v_x^2 + v_y^2} = 27.4 \text{ m/s}.$$

$$v_y^2 = v_{0y}^2 - 2g\Delta y$$

For 
$$v_y = 0$$
,  $y_0 = 0$  and  $y = H$  
$$0 = v_{0y}^2 - 2gH$$
 
$$H = \frac{v_{0y}^2}{2g} = \frac{(42.0 \sin 60.0^\circ)^2}{2(9.81)} = 67.5 \text{ m}.$$

•56 An Earth satellite moves in a circular orbit 640 km above Earth's surface with a period of 98.0 min. What are the (a) speed and (b) magnitude of the centripetal acceleration of the satellite?

a) 
$$r = 6.40 \times 10^{5} \text{m} + 6.37 \times 10^{6} \text{m} = 7.01 \times 10^{6} \text{m}$$
 
$$v = \frac{2\pi r}{T} = \frac{2\pi (7.01 \times 10^{6})}{(98.0)(60)} = 7.49 \times 10^{3} \text{m/s}.$$
 b) 
$$a = \frac{v^{2}}{r} = \frac{(7.49 \times 10^{3})^{2}}{7.01 \times 10^{6}} = 8.00 \text{ m/s}.$$

••77 SSM Snow is falling vertically at a constant speed of 8.0 m/s. At what angle from the vertical do the snowflakes appear to be falling as viewed by the driver of a car traveling on a straight, level road with a speed of 50 km/h?

Fame A is ground and frame B is the car.

$$\vec{v}_{PA} = \vec{v}_{PB} + \vec{v}_{BA}$$

$$\vec{v}_{PB} = \vec{v}_{PA} - \vec{v}_{BA} = \left(-8.0 \frac{\text{m}}{\text{s}}\right)\hat{j} - \left(14 \frac{\text{m}}{\text{s}}\right)\hat{i} = \theta$$

$$\theta = \tan^{-1} \frac{-8.0}{-14} = 30^{\circ} + 180^{\circ} = 210^{\circ}.$$

The view angle from the vertical is then 60°.