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# Structure and electrical properties of SrO-borovanadate $(V_2O_5)_{0.5}(SrO)_{0.5-\nu}(B_2O_3)_{\nu}$ glassses

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#### ARTICLE INFO

#### ABSTRACT

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SrO-borovanadate glasses with nominal composition  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_y, 0.0 \le y \le 0.4$  were prepared by a normal quench technique and investigated by direct current (DC) electrical conductivity, inductively coupled plasma (ICP) spectroscopy, infrared (IR) spectroscopy and X-ray powder diffraction (XRD) studies in an attempt to understand the nature of mechanism governing the DC electrical conductivity and the effect of addition of  $B_2O_3$  on the structure and electrical properties of these glasses. XRD patterns confirm the amorphous nature of the present glasses and actual compositions of the glasses were determined by ICP spectroscopy. The temperature dependence of DC electrical conductivity of these glasses has been studied in terms of different hopping models. The IR results agree with previous investigations on similar glasses and it has been concluded that similar to SrOvanadate glasses, metavandate chain-like structures of SrV<sub>2</sub>O<sub>6</sub> and individual VO<sub>4</sub> units also occur in SrO-borovanadate glasses. The SrV<sub>2</sub>O<sub>6</sub> and VO<sub>n</sub> polyhedra predominate in the low B<sub>2</sub>O<sub>3</sub>-containing SrOborovanadate glasses as B substitutes into the V sites of the various  $VO_n$  polyhedra and only when the concentration of B<sub>2</sub>O<sub>3</sub> exceeds the SrO content do BO<sub>n</sub> structures appear. This qualitative picture of three distinct structural groupings for Sr-vanadate and Sr-borovanadate glasses is consistent with the proposed glass structure on previous IR and extended X-ray absorption fine structure (EXAFS) studies on these types of glasses. The conductivity results were analyzed with reference to theoretical models existing in the literature and the analysis shows that the conductivity data are consistent with Mott's nearest neighbor hopping model. Analysis of the conductivity data shows that they are consistent with Mott's nearest neighbor hopping model. However, both Mott VRH and Greaves models are suitable to explain the data. Schnakenberg's generalized polaron hopping model is also consistent with temperature dependence of activation energy. However, various model parameters such as density of states, hopping energy, etc. obtained from the best fits were not found to be in accordance with the prediction of the Mott model.

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#### 1. Introduction

Transition metal (TM) oxide glasses have been frequently studied from both mechanical and physical points of view in order to better understand the transport mechanism in these semiconducting glasses [1–3]. The semiconducting behavior in these glasses arises from an unpaired  $3d^1$  electron hopping between TM ions [1,4,5] when the TM ions exist in two or more valence states, e.g., from an electron hopping from a V<sup>4+</sup> site to a V<sup>5+</sup> site. Since the unpaired electron induces a polarization around the TM ion, conduction can be described in terms of a model based on polarons. In recent years, amorphous V<sub>2</sub>O<sub>5</sub> has attracted attention because of its potential use as a cathode material in solid-state devices. Direct current (DC) conductivity of vanadium oxide glasses in which V<sub>2</sub>O<sub>5</sub> has been extensively studied and these studies have shown that the

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"small polaron" model can be used to describe the electronic transport phenomena in these materials. Several studies have been made on the structure of Sr and other vanadate glasses [6–9]. Very few studies have been carried out on glasses containing  $B_2O_3$  and  $V_2O_5$ . These glasses have their potential applications as optical and electrical memory switching [10], cathode materials for making solid devices and optical fiber [11,12]. In the present work, the effect of  $B_2O_3$  content on the electrical and structural properties of SrO-borovanadate glasses has been examined with the help of Fourier transform infrared spectroscopy and DC conductivity studies as explained. It is hoped that this experimental data will help in further understanding the mechanisms of the electrical properties in these glasses.

#### 2. Experimental methods

#### 2.1. Sample preparation

The glasses investigated in this paper were prepared by melting dry mixtures of reagent-grade  $V_2O_5$ ,  $B_2O_3$  and SrO in

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Table 1 Nominal and actual molar compositions of Sr-borovanadate  $(V_2O_5)_{0.5}$  (SrO)<sub>0.5-y</sub>  $(B_2O_3)_y$  glasses.

Nominal	SrO	B <sub>2</sub> O <sub>3</sub>	V <sub>2</sub> O <sub>5</sub>	Al <sub>2</sub> O <sub>3</sub>
y = 0.0	0.497	-	0.482	0.021
y = 0.1	0.373	0.0987	0.458	0.070
y = 0.2	0.284	0.179	0.448	0.090
y = 0.3	0.192	0.280	0.468	0.060
v = 0.4	0.092	0.384	0.454	0.070

The uncertainty in the ICP analysis of the molar fraction is  $\pm 5\%$ .

alumina crucibles with nominal compositions (V<sub>2</sub>O<sub>5</sub>)<sub>0.5</sub>  $(\text{SrO})_{0.5-y}(B_2O_3)_y, 0.0 \le y \le 0.4$ . Since the oxidation and reduction reactions in a glass melt are known to depend on the size of the melt, on the sample geometry, on whether the melt is static or stirred, on thermal history and on quenching rate, all glass samples were prepared under similar conditions to standardize these factors. Approximately 30g of chemicals were thoroughly mixed to obtain a homogenized mixture for each V<sub>2</sub>O<sub>5</sub> concentration. The crucible containing the batch mixture was then transferred to an electrically heated melting furnace maintained at 1000-1100 °C depending on the composition of the sample. The melt was left for about an hour under atmospheric conditions in the furnace during which the melt was occasionally stirred with an alumina rod. The homogenized melt was then cast onto a stainless-steel plate mold to form glass disks of approximately 1.5 cm diameter and 3 mm thickness for DC conductivity measurements. After casting, the specimens were annealed at 200 °C for 2 h. X-ray powder diffraction patterns indicated that the glasses formed were completely amorphous. After preparation, the samples were stored in a vacuum desiccator to minimize any further oxidation of the glass samples. The actual compositions of glasses were determined by inductively coupled plasma spectroscopy (ICP) and are listed in Table 1. The inclusion of alumina from the crucibles used in melting of the glass mixtures is a possible source of impurities and has been detected in the ICP studies of these glasses.

#### 2.2. Measurement techniques

#### 2.2.1. DC conductivity

For measuring DC conductivity, disc-shaped samples were made, polished and then the evaporation of gold electrodes on polished surfaces was carried out in vacuum. Measurements of DC conductivity as a function of temperature, in all the samples, were made by the two-probe technique. A constant voltage was applied and the current was measured in the temperature range 293–473 K. To obtain the variation of conductivity with temperature, the sample was placed in a furnace, brought to the desired temperature and maintained at that temperature for sufficient time before taking the measurements to ensure thermal stability. The temperature was measured by a Pt/Pt–10% Rh thermocouple. From the conductivity versus temperature data, the values of different parameters were obtained using different theoretical models as explained in Section 4.

#### 2.2.2. X-ray diffraction (XRD)

X-ray diffraction (XRD) patterns of the samples were recorded using a Shimadzu XRD-6000 X-ray diffractometer using a Cu anode ( $K_{\alpha}$ ,  $\lambda = 1.5418$  Å).

#### 2.2.3. Infrared spectra (IR)

Infrared spectra (IR) were recorded on a Perkin–Elmer Model 16F PC FT-IR spectrophotometer loaded with spectrum v2.00 software (MA, USA). Sample pellets for various glasses were prepared for FT-IR measurements by mixing approximately 1–2 mg the glass powder with about 100–150 mg of spectroscopic-grade KBr powder and grinding the mixture to a very fine powder and then compressing the mixture in an evacuable die under 10,000 pound pressure. The KBr powder was dried at 110 °C and allowed to cool in a vacuum desiccator prior to making the pellets, to avoid adsorption of moisture. All IR spectra of samples were recorded in the range 400–4000 cm<sup>-1</sup> using the following settings: number of scans 4; gain 1; apodization weak; OPD velocity 0.3 cm/s; and resolution 4.

#### 3. Results and discussion

#### 3.1. X-ray diffraction

The amorphous nature of the samples was confirmed from X-ray diffraction. XRD patterns for the glasses are shown in Fig. 1. The XRD pattern of V<sub>2</sub>O<sub>5</sub> polycrystalline powder has 3 strongest peaks at  $2\theta = 20.3^{\circ}$ , 26.1° and 31° with intensities 100%, 75% and 52%, respectively. Fig. 1 exhibits a broad diffuse scattering at low angles instead of crystalline peaks confirming a long-range structural disorder characteristic of amorphous network, i.e., XRD patterns indicated glassy behavior with a broad hump at  $2\theta = 25-27^{\circ}$  with the observation of no peak corresponding to V<sub>2</sub>O<sub>5</sub> indicating that V<sub>2</sub>O<sub>5</sub> has completely entered the glass matrix and that the glasses formed were completely amorphous.

#### 3.2. FT-IR spectra

Although infrared spectra were recorded in the wider range 400–4000 cm<sup>-1</sup>, the range 400–2000 cm<sup>-1</sup> for all glasses was selected and shown in Fig. 1 and Table 2. This is the fingerprinting range of primary interest as no significant changes are observed beyond 2000 cm<sup>-1</sup> and also spectra from 2000 cm<sup>-1</sup> towards higher numbers look the same for all compositions. For comparison, spectra are also shown for V<sub>2</sub>O<sub>5</sub>, SrO and B<sub>2</sub>O<sub>3</sub> in Fig. 1 and Table 2.

#### 3.2.1. IR for pure $B_2O_3$

The transmission peaks observed for  $B_2O_3$  are shown in Fig. 2 and Table 2 as follows:  $1505-1352 \text{ cm}^{-1}$  (broad peak)



Fig. 1. XRD for different glass composition of SrO-borovanadate  $(V_2O_5)_{0.5}$  (SrO)<sub>0.5-v</sub>(B<sub>2</sub>O<sub>3</sub>)<sub>v</sub> glasses at room temperature.

1190–1137 cm<sup>-1</sup> (small peaks but sharp), 1008–948 cm<sup>-1</sup> (sharp peaks), 806–771 cm<sup>-1</sup> (broad peak), and a sharp peak at 694 cm<sup>-1</sup>. There are small peaks in the region 646–467 cm<sup>-1</sup>. The presented IR spectrum for  $B_2O_3$  shows quite a good match with that reported in the literature [9].

#### 3.2.2. IR for pure $V_2O_5$

As seen from Fig. 2, peaks were recorded at  $1019 \text{ cm}^{-1}$  (main peak used in the discussion), 845–805 cm<sup>-1</sup> (broad peak), broad band from 594 to 470 cm<sup>-1</sup> together with small bumps at 1502 and 1190 cm<sup>-1</sup>. Our data agree quite well with that shown in Ref. [13], where peaks have been observed at 1020, 810, 600 and 480 cm<sup>-1</sup>.

#### 3.2.3. IR for pure SrO

For SrO powder, peaks were recorded at 1699, 1458, 1026 and  $855 \, \text{cm}^{-1}$  with broad bands from 585 to  $600 \, \text{cm}^{-1}$  and 409 to  $450 \, \text{cm}^{-1}$  as shown in Table 2.

## 3.2.4. Main features of IR spectra for Sr-borovanadate glasses $(V_2O_5)_{0.5}(SrO)_{0.5-v}(B_2O_3)_v$

Infrared spectra studies have been carried out on powdered samples dispersed in KBr pellets and shown in Fig. 2 for the range 400–2000 cm<sup>-1</sup>. For all glasses, water band around 3400 cm<sup>-1</sup> and –OH stretching peaks around 2400 were observed. A peak was observed at 1646 cm<sup>-1</sup> for all glasses and is independent of the concentration of the constituents of the glasses. The origin of these peaks is not obvious, but the –OH bending mode gives rise to absorption in this region and the possibility of some adsorbed water giving rise to these peaks cannot be ruled out. Hence, the bands observed in the range 1600–3400 cm<sup>-1</sup> are possibly due to the hygroscopic nature of powdered samples. Further, these bands are obtained in all the glasses almost at the same position.

The strong band observed for  $V_2O_5$  at  $1019 \text{ cm}^{-1}$ , which was reported at  $1020 \text{ cm}^{-1}$  by previous studies [14], carried out on SrO-vanadate glasses, has been assigned to the vibration of the isolated V=O non-bridge bonds in the VO<sub>5</sub> trigonal bipyramids [15]. With the addition of SrO, changes are observed in the spectra. In the case of SrO-vanadate glasses with SrO content 20-30%, a band at  $968 \text{ cm}^{-1}$  is observed with reduced intensity in the spectra (a shoulder is also observed at  $968 \text{ cm}^{-1}$  for SrO content 40%) and for glasses with SrO content 30%, 40% and 50% a band at  $886 \text{ cm}^{-1}$  is observed but this band is missing from IR spectrum for glass containing 20% SrO [16]. Further, it is observed that the band around  $1020 \text{ cm}^{-1}$  completely vanishes for these glasses, suggesting that the isolated V=O bonds might have vanished or become too weak to be detected.

The IR spectra for SrO-borovanadate glasses arise largely from the modified borate networks. According to previous studies [17], the structure of boron oxide glass consists of a random network of planer BO<sub>3</sub> triangles with a certain fraction of six-membered (boroxol) rings. X-ray and neutron diffraction data suggest that glass structure consists of a random network of BO<sub>3</sub> triangles without boroxol rings. By looking at the IR spectra (Fig. 2 and Table 2), the vibrational modes of the borate network are seen to be active in four IR spectral regions, which are similar to those previously reported [18].

- (i) The first group of bands that occurs from 1200 to  $1600 \text{ cm}^{-1}$  is due to the asymmetric stretching–relaxation of the B–O bond of triangle BO<sub>3</sub> units.
- (ii) The second group lies between 900 and  $1200 \, \text{cm}^{-1}$  and is due to B–O bond stretching of the tetrahedral BO<sub>4</sub> units.
- (iii) The third group is around 800 and  $900 \text{ cm}^{-1}$  and is due to the bending of B–O–B linkages in borate networks.
- (iv) Below 800, there are several peaks in  $B_2O_3, V2O_5$  and SrO and are retained in all these glasses.

	$5-y(B_2O_3)y$
	) <sub>0.5</sub> (SrO) <sub>0</sub> .
	: (V <sub>2</sub> 0 <sub>5</sub>
	glasses
	/anadate
	O-borov
	, and Sr
	3, SrO
	<sub>5</sub> , B <sub>2</sub> O
	or $V_2O$
	n <sup>-1</sup> ) f(
	ks (cn
	ns pea
	absorptio
	infrared
~	teristic
Table 2	Charac

LIIAIAUEII		ausorphuoris peaks (crir	) IUL V2U5, 1	D2U3, D1U, d11U D1U-L	كعددهالع عالمالمالالالالا	(V2U5/0.5(31U/)0.5-y(D2U3)					
V <sub>2</sub> 05		1502s			1190s	1019 mp		845–805 bp			594–473 small pea
SrO	1699		1458			1026		855		600–585 broad	450-409 Small pe
$B_2O_3$		1505–1352 bp			1192, 1137sp	1037sh and 1008 sp	948 sp	806-771 bp	694 sp	646–467 small peaks	
y = 0.0	1646	1552-1500 sh or s	1453sh					890 bp	630sp	454-400bs	
y = 0.1	1646	1555-1536 Sh or s	1451sh	1384-1297bp	1231-1200bp			886 bp	634-400bs		
y = 0.2	1644	1554–1525 s	1448sh	SAME	SAME			886 bp	SAME		
y = 0.3	1646	1534 sh	1450sh	SAME	SAME		980sh		SAME		
	16.40	1 L L O - H	1 1004	CANAL	ulao OOC1						

s (small), sp (sharp peaks), mp (main peak), bp (broad peak), ob (obvious but small), sh (shoulder),bs (bunch of small peaks)

ks Iks



Fig. 2. IR spectra for SrO-borovanadate (V<sub>2</sub>O<sub>5</sub>)<sub>0.5</sub>(SrO)<sub>0.5-y</sub>(B<sub>2</sub>O<sub>3</sub>)<sub>y</sub> glasses, V<sub>2</sub>O<sub>5</sub>, B<sub>2</sub>O<sub>3</sub> and SrO oxides at room temperature.

In the present work, we try to investigate the effect of addition of B<sub>2</sub>O<sub>3</sub>, and note that in these SrO-borovanadate glasses, the content of  $V_2O_5$  is 50% (fixed). With the addition of  $B_2O_3$ , the IR spectra changes and new bands are observed in the region  $1200-1400 \text{ cm}^{-1}$  (Fig. 2 and Table 2). The shoulder near 990 cm<sup>-1</sup> observed for samples with y = 0.0 and 0.10 becomes enhanced into a peak as y increases to a value of 0.4. The bands observed at 886 cm<sup>-1</sup> for SrO-vanadate glasses [16] are also observed for these glasses with B<sub>2</sub>O<sub>3</sub> content 0–20%, while it disappears from glasses with B<sub>2</sub>O<sub>3</sub> content 30-40%. The IR results agree with previous investigations on similar glasses and it has been hypothesized that similar to SrO-vanadate glasses, metavandate chain-like structures of SrV<sub>2</sub>O<sub>6</sub> and individual VO<sub>4</sub> units also occur in SrO-borovanadate glasses. The  $SrV_2O_6$  and  $VO_n$  polyhedra predominate in low B<sub>2</sub>O<sub>3</sub> containing SrO-borovanadate glasses as B substitutes into V sites of various VO<sub>n</sub> polyhedra and only when the  $B_2O_3$  concentration exceeds the SrO content, do  $BO_n$  structures appear. This qualitative picture of three distinct structural groupings for Sr-vanadate and Sr-borovanadate glasses is consistent with the proposed glass structure on previous IR and extended X-ray absorption fine structure (EXAFS) studies on these types of glasses. However, the question remains as to whether oxygen surrounding the boron ions have binding energies or environments similar to that of the higher binding energy bridging oxygen in the VO<sub>5</sub> polyhedra or are more representative of the lower binding energy non-bridging oxygen.

Structure investigations of borovanadate glasses are less numerous than those for vanadate glasses. Recently, Raman and the EXAFS spectroscopic techniques [19,20] have been used to determine the structure of borovanadate glasses with ZnO and Li<sub>2</sub>O dopants. ZnO-borovanadate glasses, which are probably more similar to our SrO-borovanadate glass series, found VO<sub>4</sub> to be the predominated polyhedra with the symmetry around V<sup>5+</sup> ions being more distorted in comparison to crystalline materials. With increasing V<sub>2</sub>O<sub>5</sub> content relative to B<sub>2</sub>O<sub>3</sub>, the distorted VO<sub>4</sub> tetrahedra would initially be incorporated into borate groupings of BO<sub>3</sub> and BO<sub>4</sub> units. At higher concentrations, these metavanadate groups could be connected to each other directly forming, possibly, metavanadate chain structures. Moreover, Stevels' structural parameter decreases with the incorporation of VO<sub>4</sub>, and thus indicates a reduction in the average number of bridging oxygen per network-forming polyhedron [19]. Another structural study of the strontium borate glass system [21] indicates that Sr ions act only as a network modifier with a coordination number of 6 as determined from the EXAFS measurements. Based on these studies, it is speculated that the local structure of Sr-borovanadate glasses is quite similar to Sr-vanadate glasses, except that BO<sub>3</sub> polyhedra are substituted for the VO<sub>n</sub> polyhedral units.

It may be appropriate to mention that similar to the Sr-vanadate glass series, from our XPS studies [19], experimentally normalized peak areas under lower binding energy O 1s(1) peak for the entire Sr-borovanadate glass series are found to be in reasonably good agreement [22] with a formula where NBO depends only on the SrO and  $V_2O_5$  contents.

#### 3.3. DC electrical conductivity

The temperature dependence of dc electrical conductivity,  $\sigma$ , for these glasses is shown in Fig. 3 as plots of Log( $\sigma$ ) versus 1000/*T*. It is observed in the figure that the conductivity is almost activated for the temperature range of measurements, as the variation of activation energy with temperature is not significant over the entire temperature range of measurements. This dependence of dc conductivity obeys the well-known Arrhenius formula

$$\sigma = \sigma_{\rm o} \, \mathrm{Exp} \left[ -W/k_B T \right] \tag{1}$$

where *W* the activation energy for conduction and the average value of heights of the potential energy barriers that the mobile alkaline ions must overcome in its jumps. The pre-exponential factor,  $\sigma_{o}$ , contains several constants including the vibrational frequency of the ions and  $k_B$  is the Boltzmann constant.



**Fig. 3.** Temperature dependence of dc conductivity,  $\sigma$  for SrO-borovanadate  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_y$  glasses as plots of Log  $\sigma$  as a function of 1000/*T*. The solid lines are the least-square fits to the data.

Table 3 Activation energy W(eV) and Log  $\sigma(\Omega-m)^{-1}$  at 400 K for SrO-borovanadate glasses  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_{y}$ .

Nominal	W(eV)	Log $\sigma(\Omega-m)^{-1}$	$T_{cal} (K)^{a}$	NBO/TO <sup>b</sup>	V4+/Vtotal <sup>b</sup>
y = 0.0	0.59	-7.539		1.00	0.0206
y = 0.1	0.57	-5.069	230	0.891	0.0225
y = 0.2	0.44	-4.42		0.751	0.0270
y = 0.3	0.39	-2.252		0.649	0.0276
				0.619	0.0204

<sup>a</sup> Theoretical slope (tan  $\theta = -1/2.303 k_B T$ ).

<sup>b</sup> From reference (Khattak et al. Phys. Rev. B).

The values of 'W' were calculated by fitting the experimental data to the equation

$$\log \sigma = \log \sigma_{\rm o} - (W/1000 \, k_{\rm B}T)(1000/T)(1/2.303) \tag{2}$$

The activation energy W(eV) and the values of  $\log \sigma (\Omega m)^{-1}$  at 400 K are shown in Table 3 for SrO-borovanadate glasses. Mostly, studies have been concerned with the dependence of electrical conductivity on  $V_2O_5$  content and the  $V^{4+}/V^{5+}$  ratio. In their study of the electrical properties of glasses of the systems CaO-B<sub>2</sub>O<sub>3</sub>-V<sub>2</sub>O<sub>5</sub> and CaO-P<sub>2</sub>O<sub>5</sub>-V<sub>2</sub>O<sub>5</sub>, Kennedy and Mackenzie [23] indicated that for similar compositions and similar  $V^{4+}\!/\!V^{5+}$ ratios, the conductivity of borate glasses is lower than that of phosphate glasses. They deduced that the network former has a great effect on the electrical conduction of such glasses. Generally, it is known that ionic conductivity increases as a result of breakdown of bridging oxygen (BO) bonds and formation of nonbridging oxygen ions [24]. This produces the so-called open structure, through which the charge carriers can move with higher mobility. In our case, it is observed that NBO/O<sub>total</sub> decreases while both dc conductivity and the ratio  $V^{4\ast}/V_{\rm total}$ increase with increase in the content of B<sub>2</sub>O<sub>3</sub> [22,Table 3]. Hence, the bridging oxygen (BO) bonds are strengthened, which indicates that the conductivity depends on the ratio of  $V^{4+}/V_{total}$ , and hence the presence of electronic conductivity.

In Mott's model [25,26] for conduction process in TMO glasses, the conduction mechanism is considered in terms of phonon-assisted hopping of small polarons between localized states. According to this model, DC conductivity for the nearest-



**Fig. 4.** A plot of Log  $\sigma$  versus W for SrO-borovanadate  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_y$  glasses at 400 K.

neighbor hopping in non-adiabatic regime at high temperatures (T> $\theta_D$ /2) is given by

$$\sigma = v_0 N e^2 R^2 / k_B T C (1 - C) \exp(-2\alpha R) \exp(-W / k_B T)$$
(3)

where  $v_o$  is the longitudinal optical phonon frequency, *C* the fraction of reduced vanadium ions,  $V^{4+}/V_{total}$ ,  $\alpha^{-1}$  the localization length for the wave function, *R* the average hopping distance,  $k_B$  the Boltzmann constant, *e* the electronic charge and *w* the activation energy for hopping conduction.

The activation energy for hopping conduction is given by [5]

$$W = W_D + W_H/2, \text{ for } T > \theta_D/2$$
  
$$W \approx W_D, \text{ for } T < \theta_D/4$$

where  $W_H$  is the hopping energy,  $W_D$  the energy difference between two adjacent sites, i.e., disorder energy and  $\theta_D$  is the Debye temperature.

In the framework of Mott's model, the nature of the polaron hopping mechanism in the high-temperature range (adiabatic or non-adiabatic), where an activated behavior of conductivity was observed, can be ascertained from the plot  $Log \sigma$  versus activation energy, *W*, at an arbitrary experimental temperature in this range. It has been suggested [26,27] that the hopping would be in the adiabatic regime if the temperature estimated, Tc, from the slope of such a plot were close to the experimental temperature T. Otherwise, the hopping would be in the non-adiabatic regime. A plot of Log  $\sigma$  at 400 K versus W is shown in Fig. 4 for these glasses. It is evident from the figure that the data are very scattered but we have tried to fit the data into a straight line. The temperature calculated, Tc, from the fitted line is very different from the experimental temperature chosen (400K) (Table 3), suggesting that the conduction mechanism in the present glasses is due to non-adiabatic hopping of the polarons [25,26] (see Fig. 5).

The experimental results were analyzed with reference to theoretical models existing in the literature.

#### 3.3.1. Greaves law of variable range hopping (VRH)

According to this model [28], the expression for conductivity can be written as

$$\sigma T^{1/2} = A \exp(-B/T^{1/4})$$
(4)

where *A* and *B* are constants. The values of *A* and *B* can be obtained from the intercept and slope, respectively, of the plot  $Log(\sigma T^{1/2})$ 



**Fig. 5.** A plot of Log  $(\sigma T^{1/2})$  versus  $T^{-1/4}$  for SrO-borovanadate  $(V_2O_5)_{0.5}(SrO)_{0.5-y}$  (B<sub>2</sub>O<sub>3</sub>)<sub>y</sub> glasses. The solid lines are the best fits to Eq. (4).



Parameters A, B,  $N_G$  obtained for Greaves variable-range hopping conduction<sup>a</sup> for SrO-borovanadate glasses  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_y$ ,  $\alpha = 33 \text{ nm}^{-1}$ .

Nominal	$\log A [(\Omega - m)^{-1} K^{1/2}]$	B (K <sup>1/4</sup> )/2.303	$N_G (\times 10^{21} \mathrm{eV^{-1}/cm^3})$
y = 0.0	23.053	129.479	0.97
y = 0.1	24.732	121.004	1.10
y = 0.2	18.809	93.978	3.15
y = 0.3	20.492	93.446	3.22

<sup>a</sup>  $\sigma T^{1/2} = A \exp(-B/T^{1/4}) N_G = (2.882 \times 10^{29})/(\text{slope})^4 \text{ eV}^{-1}/\text{cm}^3.$ 

versus  $T^{-1/4}$ . Further, the value of *B* can be written as  $B = 2.1[\alpha^3/k_B N_G]^{1/4}$ 

Fig. 5 shows the plots of  $Log(\sigma T^{1/2})$  versus  $T^{-1/4}$  and the linear relationship confirms the Greaves VRH model [28]. The values of parameters *A* and *B* obtained from these curves are given in Table 4. Values of the density of states at the Fermi level,  $N_G$ , were estimated from Eq. (5) assuming  $\alpha = 33 \text{ nm}^{-1}$  [29] and shown in Table 4. These values are consistent with those of the usual semiconducting oxide glasses [30,31], suggesting that this model is suitable to explain the conductivity data. Thus, it is concluded that the appearance of the VRH for the temperature interval of measurements, T = 293-470 K, is reasonable for the present glasses.

#### 3.3.2. Schnakenberg's polaron hopping model

A polaron hopping model, where  $W_D \neq 0$ , has been considered by Schnakenberg [32]. In this model, the optical multiphonon hopping process determines dc conductivity at high temperature, while at low temperatures the conductivity is determined by the acoustical single-phonon-assisted hopping process. In this model, the expression for dc conductivity as a function of temperature is given by

$$\sigma = A/T[\sin h (hv_o/k_BT]^{1/2} \operatorname{Exp}\left[-(4W_H/hv_o) \tan h (hv_o/4k_BT)\right] \times \operatorname{Exp}(-W_D/k_BT)$$
(6)

Eq. (6) predicts a temperature-dependent hopping energy which decreases with increase in temperature, consistent with the data presented in Fig. 3. Fig. 6 shows plots of Log ( $\sigma$ *T*) versus



**Fig. 6.** Best fits (solid curves) of the Schnakenberg model Eq. (6) to the experimental data for SrO-borovanadate  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_y$  glasses as plots of Log ( $\sigma$ T) versus 1000/T.

Table 5

(5)

Parameters obtained by fitting the dc conductivity data to the Schnakenberg model for SrO-borovanadate glasses  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_{y}$ .

Nominal	$v_0 \times 10^{13} (s^{-1})$	$W_H(\mathrm{eV})$	$W_D$ (eV)	$W_H + W_D/2 (eV)$
y = 0.0	0.99	0.48	0.02	0.49
y = 0.1	1.9	0.77	0.04	0.79
y = 0.2	2.1	0.73	0.04	0.75
y = 0.3	2.8	0.84	0.05	0.87

1000/*T* and the DC conductivity has been fitted to the theoretical values given by this model (Eq. (6)).  $W_{H}$ ,  $W_D$  and  $v_o$  were used as variable parameters in the fitting process and the best fits of the data have been obtained for the values of the parameters shown in Table 5. The values of  $v_o$  are close to the values previously reported [29]. However, this model yields high values of  $W_H$  than the values of the activation energy estimated for the temperature range of measurements (Table 2). Further,  $W_H+W_D/2$  is not equal to W (Table 3) and so is not in accordance with the prediction of the Mott model [25,26].

#### 3.3.3. Mott's model

At low temperatures, where polaron binding energy is very small and disorder energy,  $W_D$ , plays a dominant role in the conduction mechanism, Mott and Davis [33] have shown that hops may occur preferentially beyond nearest neighbors. The conductivity for the so-called variable range hopping mechanism is given by

$$\sigma = B \operatorname{Exp}\left(-A/T^{1/4}\right) \tag{7}$$

where

$$A = 4[2 \alpha^3 / 9\pi k_B N(E_F)]^{1/4}$$
(8)

$$B = [e^2/2(8\pi)^{1/2}] v_0 [N(E_F)/\alpha k_B T]^{1/2}$$
(9)

and  $\alpha$  is the decay of the localized state wavefunction, and  $N(E_F)$  the density of state at the Fermi level. Fig. 7 shows plots of Log  $\sigma$  versus  $T^{-1/4}$  and it is observed that the plots are linear over almost the whole temperature range of measurements consistent with the Mott VRH model. Eq. (7) was fitted to the experimental data and the values of *A* and *B* calculated from these fits are given



**Fig. 7.** A plot of Log  $\sigma$  versus  $T^{-1/4}$  for SrO-borovanadate  $(V_2O_5)_{0.5}(SrO)_{0.5-y}(B_2O_3)_y$ glasses. The solid lines are best fits to Eq. (7).

#### Table 6

Parameters A, B,  $N(E_F)$  obtained for Mott's variable-range hopping and percolation model<sup>a</sup> for Sr-borovanadate glasses (V<sub>2</sub>O<sub>5</sub>)<sub>0.5</sub>(SrO)<sub>0.5-y</sub>(B<sub>2</sub>O<sub>3</sub>)<sub>y</sub>

Nominal	A (K <sup>1/4</sup> ) /2.303	$\log B \left[ (\Omega - m)^{-1} \right]$	$N(E_F)(x \ 10^{21} - \text{eV}^{-1} \text{ cm}^{-3})$
y = 0.0	129.479	21.374	0.953
y = 0.1	121.004	22.034	1.25
y = 0.2	93.978	16.655	3.44
y = 0.3	93.446	18.343	3.52

 $\alpha = 33 \text{ nm}^{-1}$ .

<sup>a</sup>  $\sigma = B \exp (-A/T^{1/4}) N(E_F) = 2.68 \times 10^{29} / (\text{slope})^4 \text{ eV}^{-1} \text{ cm}^{-3}.$ 

in Table 6. Assuming a reasonable value of  $\alpha^{-1} \approx 10 A^{\circ}$ , values of  $N(E_F)$  were calculated from Eq. (8). These values, shown in Table 6, are comparable with the values obtained for the vandate glasses formed with traditional network former and the other semiconducting glasses [33-36].

#### 4. Conclusions

The overall features of XRD patterns confirm the amorphous nature of the present glasses. The IR results agree with previous investigations on similar glasses and it has been hypothesized that with the introduction of B<sub>2</sub>O<sub>3</sub> into SrO-vanadate glasses, B atoms would substitute into V sites of various VO<sub>n</sub> polyhedra and not result in any additional structural units. On B<sub>2</sub>O<sub>3</sub> concentration exceeding the SrO content, a third grouping is realized as  $BO_n$ structures, such as metaborate chain structures, BO<sub>4</sub> polyhedra or Sr<sub>2</sub>B<sub>2</sub>O<sub>5</sub> units are formed in boron-rich regions in the borovandate glass network in addition to VO<sub>n</sub> polyhedra and SrV<sub>2</sub>O<sub>6</sub> structures. Thus, this qualitative picture of the local glass structure evolving as the relative concentration varies in these SrO-vanadate and SrO-borovanadate glasses is very similar to the interpretation of the glass structure based on the previous IR and EXFAS studies on

these glasses. The temperature dependence of DC electrical conductivity of SrO-vanadate and SrO-borovandate glasses has been studied in terms of different hopping models. The data suggest that the conduction mechanism in the present glasses is due to non-adiabatic hopping of polarons. Further, analysis of the conductivity data shows that the conductivity data are consistent with Mott's nearest neighbor hopping model. However, both Mott VRH and Greaves models are suitable to explain the data. Schnakenberg's generalized polaron hopping model is consistent with the temperature dependence of the activation energy. However, the various model parameters such as density of states, hopping energy, etc., obtained from the best fits were not found to be in accordance with the prediction of the Mott model [3].

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