

## Chapter 2

The electromagnetic theory was developed by Maxwell.

- Hertz produced electromagnetic waves confirming Maxwell theory.
- He also showed that electromagnetic waves and light were one and the same.  
 $\Rightarrow$  Light is a wave!
- Stefan found experimentally for a hot solid

Stefan's Law  $\rightarrow e = \sigma T^4$  (Watt/m<sup>2</sup>)

T: Kelvin

$\sigma$ : Stefan-Boltzmann const. =  $5.67 \times 10^{-8} \frac{\text{W} \cdot \text{m}^{-2}}{\text{K}^4}$

- Five years later, Boltzmann derived Stefan's law from Maxwell + thermodynamics.

- A body which absorbs radiation of all wavelengths is called a blackbody.
- The radiation emitted from a blackbody has a continuous spectrum.
- Wien proposed a relationship between  $\lambda_{\max}$  and  $T$  for the blackbody distribution.

$$\lambda_{\max} = \frac{2.898 \times 10^{-3}}{T} \quad \text{Wien's displacement law.}$$

- Wien proposed the spectral energy density for a blackbody:

$$\rightarrow u(\nu, T) = A \nu^3 e^{-\frac{\beta \nu}{T}}$$

Wien's  
exponential law

$A$  &  $\beta$ : fitting parameters

The law failed to fit the experimental data at long wavelengths!

(see Fig. 2.5 in the text book)

According to Planck, the spectral energy density  $u(f, T)$  is:

$$u(f, T) df = \bar{E} \underbrace{N(f) df}_{\substack{\uparrow \text{ \# of oscillators} \\ \text{having freq.} \\ \text{between } f \text{ and} \\ f + df}} \quad \text{--- (1)}$$

$\uparrow$   
average energy emitted per oscillator

He also showed that

$$N(f) df = \frac{8\pi f^2}{c^3} df \quad \text{--- (2)}$$

Rayleigh-Jeans  
(classical)  
theory

$$\bar{E} = k_B T \quad \text{--- (3)}$$

energy of the oscillator is continuous.

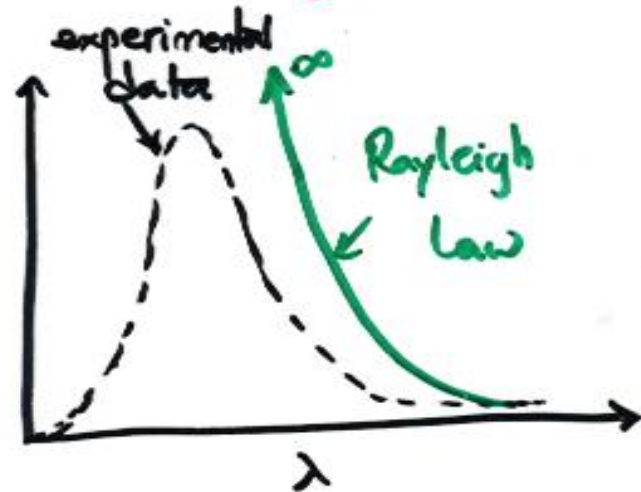
Planck  
(quantum)  
theory

$$\bar{E} = \frac{hf}{e^{hf/kT} - 1} \quad \text{--- (4)}$$

using the energy of the oscillator is quantized

## Rayleigh - Jeans Law

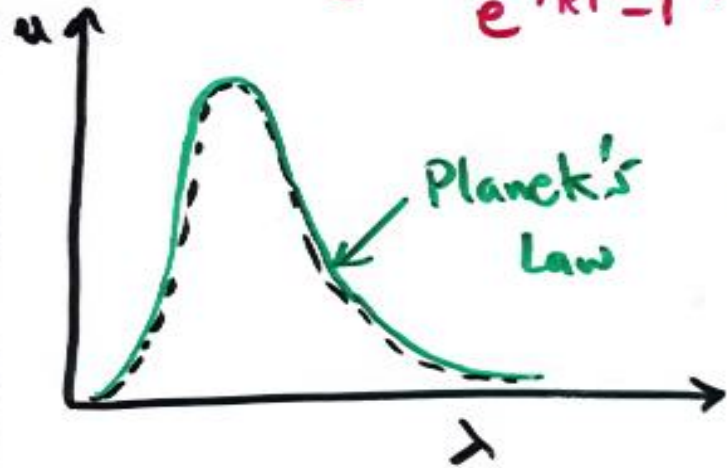
$$u(f, T) = \frac{8\pi f^2}{c^3} k_B T$$



$\lambda \rightarrow 0 \quad u \rightarrow \infty$   
ultraviolet catastrophe

## Planck's function

$$u(f, T) = \frac{8\pi f^2}{c^3} \left( \frac{hf}{e^{\frac{hf}{kT}} - 1} \right)$$



Planck's Law fit  
the experimental  
data for the blackbody

At high  $f$  ( $f \rightarrow \infty$ ) where  $\frac{hf}{kT} \gg 1$   
 $\lambda \rightarrow 0$

$$e^{\frac{hf}{kT}} - 1 \approx e^{-\frac{hf}{kT}}$$

$$\Rightarrow u(f, T) \approx \frac{8\pi f^3 h}{c^3} e^{-\frac{hf}{kT}} \quad [\text{Wien's Law}]$$

• At low  $f$  ( $f \rightarrow 0$ )  $\frac{hf}{kT} \ll 1$   
 $\lambda \rightarrow \infty$

$$\frac{1}{e^{\frac{hf}{kT}} - 1} = \frac{1}{1 + \frac{hf}{kT} - 1} = \frac{kT}{hf}$$

and  $u(f, T) \approx \frac{8\pi}{c^3} f^2 kT$  [ Rayleigh-Jeans Law ]

## Chapter 2

- Planck fitted the black body radiation spectrum by considering that the radiation energy is **quantized** and not continuous.
- Energy is emitted or absorbed in bundles called photons of energy  $hf$ .
- The spectral distribution of a blackbody is given by the Planck radiation law:

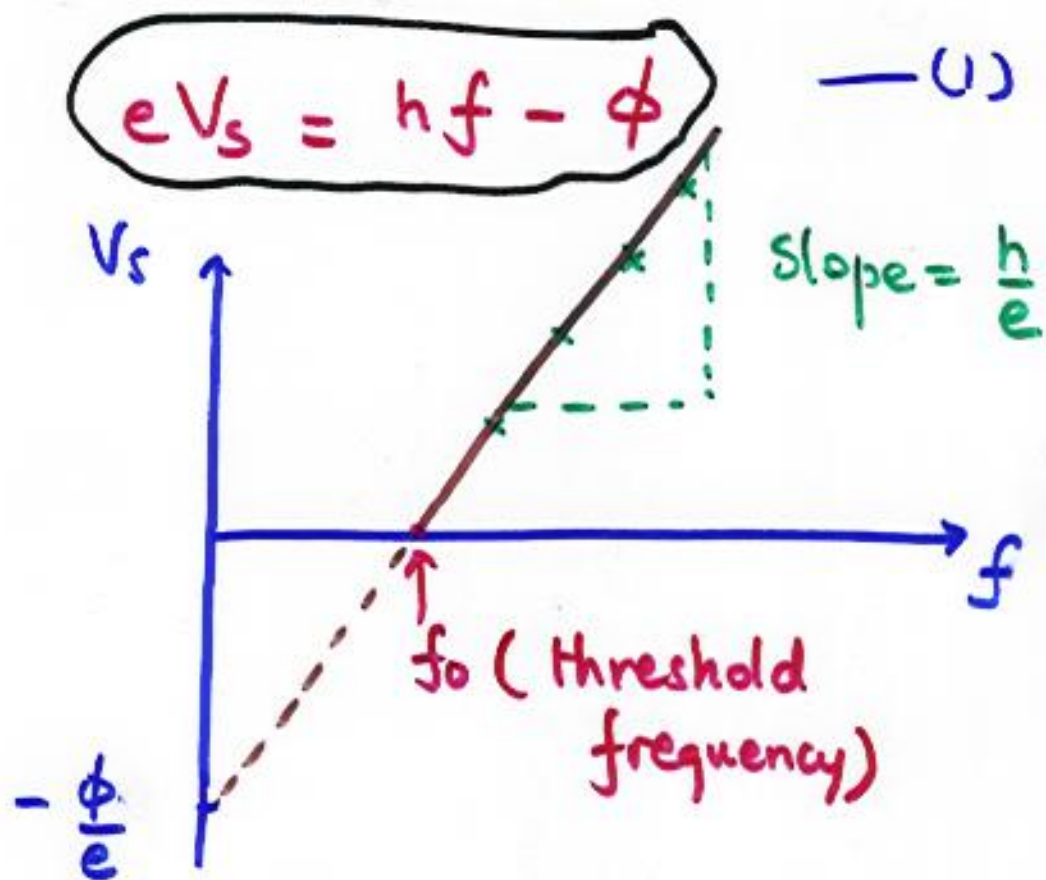
$$u(f, T) = \frac{8\pi h f^3}{c^3} \frac{1}{e^{hf/kT} - 1}$$

- when  $f \rightarrow \infty$  we recover Wien's law
- when  $f \rightarrow 0$  we recover Rayleigh-Jeans law

### \* Photo electric effect



- The wave nature of light cannot explain some features of the photoelectric effect.
- Einstein had to consider light as quanta. Each quantum has an energy  $E = hf$  so that



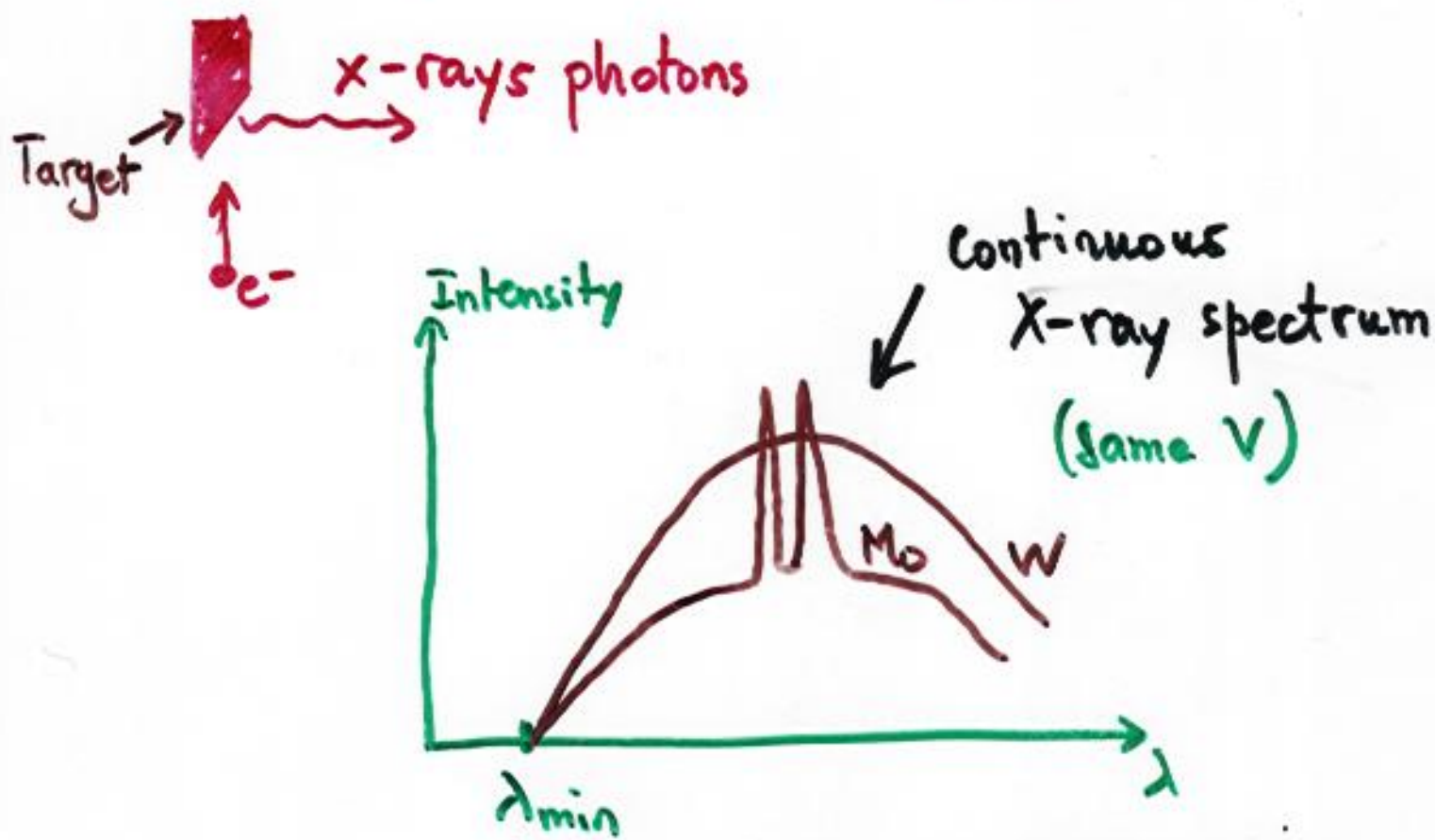
$V_s$ : stopping potential

$\phi$ : work function of the metal

- The ejected  $e^-$  has energy  $K = hf - \phi$ !

. There will be no ejected  $e^-$  if the frequency of light is less than  $f_0$ .

\* X-rays are produced by bombarding a target with fast moving electrons.  
(This is the opposite of the photoelectric effect)



$$\lambda_{min} = \frac{hc}{eV} = \frac{12400 \text{ eV} \cdot \text{\AA}}{V}$$

accelerating potential