

Name:

Key

ID#:

- (a) Calculate the **frequency of revolution** and the **orbit radius** of the electron in the Bohr model of hydrogen for $n = 100$ and 10000 .
 (b) Calculate the **photon frequency** of transition from the n to $n-1$ states for the same values of n as in part (a).
 (c) Calculate $f_{\text{rev}} - f_{\text{photon}}$ for each case. What can you conclude?

(a) $f_{\text{rev}} = \frac{v}{2\pi r}$ but $m_e v r = n \hbar \Rightarrow v = \frac{n \hbar}{m_e r}$

$f_{\text{rev}} = \frac{n \hbar}{2\pi m_e r^2}$ but $r_n = a_0 n^2 \Rightarrow f_{\text{rev}} = \frac{n \hbar}{2\pi m_e a_0^2 n^4}$

$\Rightarrow f_{\text{rev}} = \frac{\hbar}{2\pi m_e a_0^2 n^3} = \frac{6.57 \times 10^{15}}{n^3}$

$n = 100$ $f_{100, \text{rev}} = 6.57 \times 10^9 \text{ Hz}$

$r_{100} = 5.3 \times 10^{-7} \text{ m}$

$n = 10,000$ $f_{10,000, \text{rev}} = 6.57 \times 10^3 \text{ Hz}$

$r_{10,000} = 5.3 \times 10^{-3} \text{ m}$

(b) $f_{\text{photon}} = \frac{\Delta E}{h} = \frac{13.6 \text{ eV}}{h} \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right) = 3.1 \times 10^{15} \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$

$n_i = 100 \rightarrow n_f = 99$ $f_{\text{photon}} = 3.3 \times 10^{15} \left(\frac{1}{99^2} - \frac{1}{100^2} \right) = 6.7 \times 10^9 \text{ Hz}$

$n_i = 10000 \rightarrow n_f = 9999$ $f_{\text{photon}} = 3.3 \times 10^{15} \left(\frac{1}{9999^2} - \frac{1}{10000^2} \right) = 6.6 \times 10^3 \text{ Hz}$

(c) The difference

$n = 100$

$\Delta f = 0.13 \times 10^9 \text{ Hz}$ (large)

$n = 10,000$

$\Delta f = 30 \text{ Hz}$



as n increases $f_{\text{rev}} \rightarrow f_{\text{jump}} \Rightarrow$ Bohr's correspondence principle !!!