

Quiz # 5 Ch.#21 T131-Sec. 7-9-v1

Student ID:..... Student Name:..... Section #

Q#1: Particles A and B are electrically neutral and are separated by $5.0 \mu\text{m}$. If 5.0×10^6 electrons are transferred from particle A to particle B, the magnitude of the electric force between them is: (Ans: $2.3 \times 10^{-4} \text{N}$)

$$Q_A = -5 \times 10^6 \times 1.6 \times 10^{-19}, \quad Q_B = +5 \times 10^6 \times 1.6 \times 10^{-19}$$

$$F = k \frac{Q_A Q_B}{d^2}$$

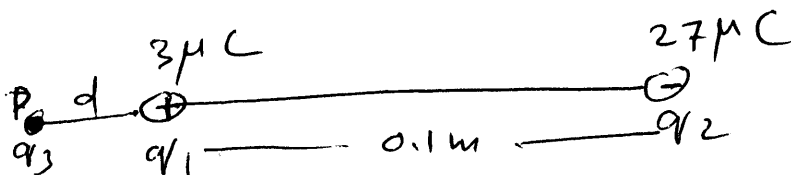
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$$|F| = k \frac{|Q_A| |Q_B|}{d^2} = \frac{9 \times 10^9 \times (5 \times 10^6 \times 1.6 \times 10^{-19})^2}{(5 \times 10^{-6})^2}$$

$$= 23.04 \times 10^{-5} = 2.3 \times 10^{-4} \text{N}$$

Q4. Two fixed particles of charges $q_1 = +3.0 \times 10^{-6} \text{C}$ and $q_2 = -27 \times 10^{-6} \text{C}$, are 10 cm apart. How far from q_1 should a third charge be located so that the net force on it is zero?

A) 5.0 cm



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6

$$|F_{13}| = |F_{23}|$$

$$\frac{k q_1 q_3}{d^2} = \frac{k q_2 q_3}{(d+0.1)^2} \Rightarrow \frac{q_1}{d^2} = \frac{q_2}{(d+0.1)^2}$$

$$\frac{d+0.1}{d} = \sqrt{\frac{q_2}{q_1}} = \sqrt{\frac{27 \times 10^{-6}}{3 \times 10^{-6}}} = 3$$

$$\frac{d+0.1}{d} = 3 \Rightarrow 3d - d = 0.1$$

$$d = \frac{0.1}{2} = 0.05 \text{ m}$$

Quiz # 5 Ch.#21 T131-Sec. 7-9-v2

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Q#1: Two neutral metal spheres are separated by 300 m. How many electrons must be transferred from one sphere to the other so that their force of attraction has a magnitude of 10^6 N? A) 2×10^{19}

$$q_1 = -q, q_2 = +q, F_{q_1 q_2} = 10^6 \text{ N}, d = 300 \text{ m}$$

$$|F| = \frac{k q^2}{d^2} \Rightarrow q = \sqrt{\frac{|F| d^2}{k}}$$

$$q = \sqrt{\frac{10^6 \times (300)^2}{9 \times 10^9}} = \sqrt{10} = 3.162 \text{ C}$$

$$= \frac{3.162}{1.6 \times 10^{-19}} e = 2 \times 10^{19} e$$

Q#2: Consider the charges shown in figure 1. Find the magnitude and sign of charge Q_4 so that the net electrostatic force on charge Q_5 is zero. (Ans: +1.8 nC)

$$F_{\text{net}-x} = 0$$

$$\text{For } |F_{\text{net}-y}| = 0, \frac{k Q_4 Q_5}{(0.03)^2} = \frac{k Q_3 Q_5}{(0.05)^2}$$

$$Q_4 = \frac{(0.03)^2}{(0.05)^2} \times Q_3$$

$$= 0.36 \times Q_3$$

$$Q_4 = 1.8 \text{ nC}$$

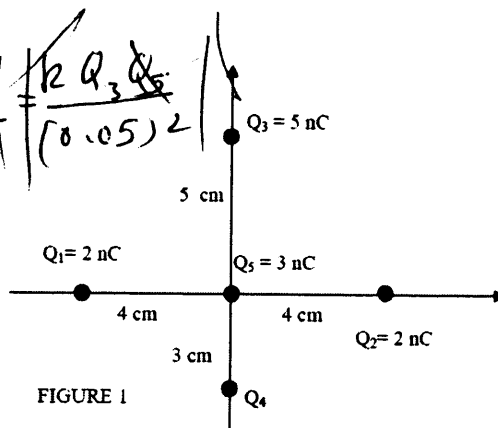


FIGURE 1

Quiz # 5 Ch.#21 T131-Sec. 7-9-v3

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Q#1: Particle 1 with charge q_1 , and particle 2 with charge q_2 are on the x axis, with particle 1 at $x = 4.0$ cm and particle 2 at $x = -2.0$ cm. Find the relationship between q_1 and q_2 so that the net force on a third particle of charge q located at the origin, be zero,

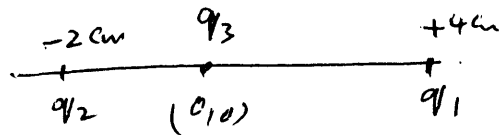
A) $q_2 = q_1 / 4$

$$|F_{31}| = |F_{32}|$$

$$\left| \frac{k q_3 q_1}{(0.04)^2} \right| = \left| \frac{k q_3 q_2}{(0.02)^2} \right|$$

$$\frac{q_2}{q_1} = \frac{(0.02)^2}{(0.04)^2} = \frac{4}{16} = \frac{1}{4}$$

$$q_2 = \frac{q_1}{4}$$



Q#2: A particle with charge $2.0 \mu\text{C}$ is placed at the origin, an identical particle, with the same charge, is placed 2.0 cm from the origin on the positive x axis, and a third identical particle, with the same charge, is placed 2.0 cm from the origin on the positive y axis.

The magnitude of the force on the particle at the origin is: A) 1.3×10^2 N

Force ~~on~~ particle at the origin

$$\vec{F} = -F_x \hat{i} + F_y \hat{j}$$

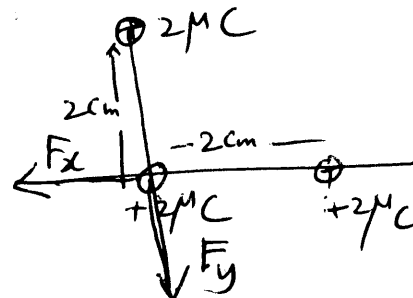
$$= -(F_x + F_y)$$

$$= -k q^2 \left(\frac{1}{x^2} \hat{i} + \frac{1}{y^2} \hat{j} \right)$$

$$= -k q^2 \left(\frac{1}{(0.02)^2} \hat{i} + \frac{1}{(0.02)^2} \hat{j} \right) = -\frac{k q^2}{(0.02)^2} (\hat{i} + \hat{j})$$

$$|F| = \frac{k q^2 \sqrt{2}}{(0.02)^2} = \frac{9 \times 10^9 \times (2 \times 10^{-6})^2 \times \sqrt{2}}{(0.02)^2}$$

$$= 130 \text{ N} = 1.3 \times 10^2 \text{ N}$$



Quiz # 5 Ch.#21 T131-Sec. 7-9-v4

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Q1 Three point charges Q_1 , $Q_2 = 20 \mu\text{C}$ and $Q_3 = 50 \mu\text{C}$ are located as shown in the figure.

If the net force on Q_3 is in the direction of the negative y-axis, find the charge of Q_1 .

A) $-10 \mu\text{C}$

$$F_{\text{net}-x} = 0 \text{ then } |$$

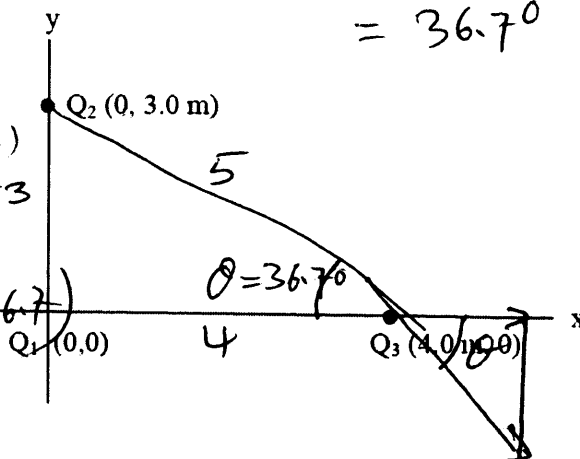
$$\theta = \cos^{-1}\left(\frac{4}{5}\right) = 36.7^\circ$$

$$|F_{13-x}| = |F_{23-x}|$$

$$\frac{k Q_1 Q_3}{(4)^2} = \frac{k Q_2 Q_3 \cos(36.7)}{(5)^2}$$

$$|Q_1| = \frac{(4^2)}{(5^2)} |Q_2| \cos(36.7)$$

$$|Q_1| = 10.26 \mu\text{C}$$



Q#2: The distance between two identical conductor spheres is 0.50 m. Initially, one sphere has a charge of $-8.0 \mu\text{C}$ and the other sphere has a charge of $+2.0 \mu\text{C}$. If the spheres are connected with a very thin conducting wire, what will be the electrostatic force on each sphere? A) 0.32 N, repulsive.

$$\text{charge on each sphere after touching} = \frac{-8 \mu\text{C} + 2 \mu\text{C}}{2}$$

$$q = -3 \mu\text{C}$$

$$|F| = \frac{k q^2}{(0.5)^2} = \frac{9 \times 10^9 \times (3 \times 10^{-6})^2}{(0.5)^2}$$

$$|F| = 0.324 \text{ N}$$

Quiz # 5 Ch.#21 T131-Sec. 7-9-v5

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Q#1: Two identical conducting spheres A and B carry Q and 2Q charges respectively, and are separated by a distance much larger than their diameters. Initially the electrostatic force between them is F. A third identical uncharged conducting sphere C is first touched to A, then to B, and then moved away. As a result of this, the electrostatic force between A and B becomes: A) F/1.6

Force F before touching, $F = \frac{k \cdot Q \times 2Q}{d^2} = \frac{2kQ^2}{d^2}$

After touching charge in each sphere $Q'_1 = \frac{Q}{2}$; $Q'_2 = \frac{2Q + Q}{2} = 1.25Q$

Force F' (after touching) between them. $= \frac{k Q'_1 Q'_2}{d^2} =$

$F' = k \frac{Q}{2} \times \frac{1.25Q}{d^2} = \left(\frac{1.25}{2}\right) \frac{kQ^2}{d^2}$

$\frac{F'}{F} = \frac{\frac{1.25}{2} kQ^2/d^2}{kQ^2/d^2} = \left(\frac{1.25}{2}\right) F = 0.625 F = \frac{F}{1.6}$

Q#2: Two identical positively charged ions are separated from each other by a distance of 6.8×10^{-9} m. If the electrostatic force between them is 4.5×10^{-9} N, how many electrons are missing from each ion? A) 30

$|F| = \frac{k q^2}{d^2} \Rightarrow q = \sqrt{\frac{|F| d^2}{k}}$

$q = \sqrt{\frac{4.5 \times 10^{-9} \times (6.8 \times 10^{-9})^2}{9 \times 10^9}}$

$= 4.808 \times 10^{-18} \text{ C}$

$q = \frac{4.808 \times 10^{-18}}{1.6 \times 10^{-19}} = 30 \text{ electrons}$

Quiz # 5 Ch.#21 T131-Sec. 7-9-v6

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Q#1: Two point charges $q_1 = +2.0 \times 10^{-6} \text{ C}$ and $q_2 = -8.0 \times 10^{-6} \text{ C}$ are located at (0.0, 0.0) cm and (10.0, 0.0) cm, respectively. Another positive point charge q_3 is to be located somewhere, on x-axis, such that the net electrostatic force on it due to q_1 and q_2 is zero. Its location will be: A) (-10.0, 0.0) cm

$$|F_{13}| = |F_{23}| \quad \sqrt{|F_{13}| = |F_{23}|}, \quad q_3 \quad \begin{array}{c} +2 \times 10^{-6} \text{ C} \\ (0,0) \end{array} \quad \begin{array}{c} -8 \times 10^{-6} \text{ C} \\ (10,0) \end{array}$$

$$\frac{2 \times 10^{-6} \times k}{d^2} = \frac{8 \times 10^{-6} \times k}{(d+0.1)^2} \Rightarrow \frac{1}{d^2} = \frac{4}{(d+0.1)^2}$$

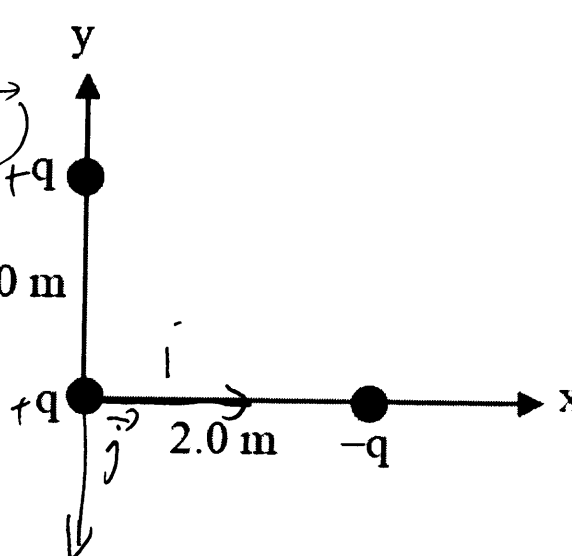
$$\frac{1}{d} = \frac{2}{d+0.1} \Rightarrow 2d = d+0.1 \Rightarrow d = 0.1 \text{ m}$$

Q#2: Three particles are fixed as shown in Figure 1. If $|q| = 2.0 \mu\text{C}$, what is the net electrostatic force on the particle at the origin? [\hat{i} and \hat{j} are unit vectors along the +x and +y axes, respectively (Ans: $(9.0 \times 10^{-3} \hat{i} - 9.0 \times 10^{-3} \hat{j}) \text{ N}$)]

$$\vec{F} = \frac{kq^2}{4} (\hat{i} - \hat{j})$$

$$= \frac{9}{4} \times 10 \times (2 \times 10^{-6})^2 (\hat{i} - \hat{j})$$

$$= 9 \times 10^{-3} (\hat{i} - \hat{j}) \text{ N}$$

$$\vec{F} = 9 \times 10^{-3} (2 \hat{i} - 2 \hat{j})$$


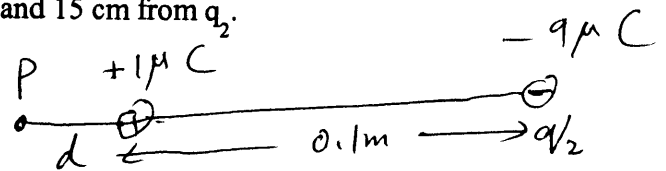
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Q#1: Two fixed particles, of charges $q_1 = +1.0 \times 10^{-6} \text{ C}$ and $q_2 = -9.0 \times 10^{-6} \text{ C}$, are 10 cm apart. How far from each should a third charge be located so that no net electrostatic force acts on it? (At 5 cm from q_1 and 15 cm from q_2 .)

$$\frac{k q_1 q_3}{d^2} = \frac{k q_2 q_3}{(d+0.1)^2}$$



$$\frac{1 \times 10^{-6}}{d^2} = \frac{9 \times 10^{-6}}{(d+0.1)^2} \Rightarrow \frac{1}{d} = \frac{3}{d+0.1}$$

$$3d = d+0.1 \Rightarrow 2d = 0.1 \Rightarrow d = 0.05 \text{ m}$$

$(0.05 \text{ m}, 0.05 + 0.1 = 0.15 \text{ m})$

Q#2: Two small identical conducting spheres, initially uncharged are separated by a distance of 1.0 m. Find the number of electrons that must be transferred from one sphere to the other in order to produce an attractive force of $2 \times 10^{-4} \text{ N}$ between the spheres. (Ans: 9.3×10^{15})

$$F = \frac{k q^2}{(d)^2} \Rightarrow q = \sqrt{\frac{F d^2}{k}} = \sqrt{\frac{2 \times 10^{-4} \times 1^2}{9 \times 10^9}}$$

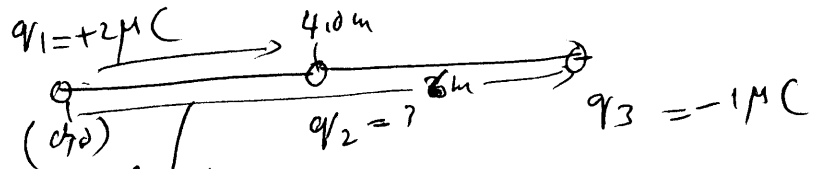
$$q = \sqrt{0.0222 \times 10^{-4}} = 0.149 \times 10^{-2} \text{ C}$$

$$= \frac{0.149 \times 10^{-2}}{1.6 \times 10^{-19}} = 9.32 \times 10^{15} \text{ e.}$$

Quiz # 5 Ch.#21 T131-Sec. 7-9-v8

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Q#1: Consider three charges on the x-axis: $q_1 = 2.0 \mu\text{C}$ located at $x_1 = 0.0 \text{ m}$, q_2 located at $x_2 = 4.0 \text{ m}$ and $q_3 = -1.0 \mu\text{C}$ located at $x_3 = 6.0 \text{ m}$. What is the value of q_2 such that the force on q_3 is zero? A) $q_2 = -0.22 \mu\text{C}$.



$$\frac{k q_2 q_3}{(2)^2} = \frac{k q_1 q_3}{(6)^2}$$

$$q_2 = \frac{4}{36} \times q_1 = \frac{4}{36} \times 2 \mu\text{C} = 0.22 \mu\text{C}$$

$$q_2 = -0.22 \mu\text{C}$$

Q2. Consider two identical conductor spheres, S_1 and S_2 . Initially, sphere S_1 has a charge of $-40 \mu\text{C}$ and Sphere S_2 has a charge of $+20 \mu\text{C}$. If the spheres are touched together and then separated by a distance of 0.20 m , what is the resultant force between them? (Ans: 23 N , repulsive)

Charges on each sphere after touching = $\frac{+20 \mu\text{C} - 40 \mu\text{C}}{2} = -10 \mu\text{C}$

$$F_1 = \frac{k (-10 \mu\text{C}) (-10 \mu\text{C})}{(0.2)^2}$$

$$= \frac{9 \times 10^9 \times 10^2 \times 10^{-6} \times 10^{-6}}{(0.2)^2}$$

$$= 22.5 \text{ N} \approx 23 \text{ N}$$

Quiz # 5 Ch.#21 T131-Sec. 7-9-v9

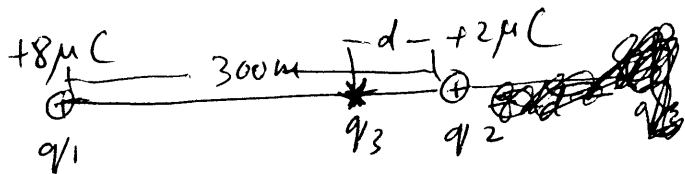
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Q1 Two neutral metal sphere are separated by 0.3 km. How much electric charge must be transferred from one sphere to the other so that their electrical attraction is 10^3 N? A1 0.1 C.

$$F = \frac{kq^2}{d^2}, \quad q = \sqrt{\frac{Fd^2}{k}}$$

$$\frac{4}{4} \quad q = \sqrt{\frac{10^3 \times (300)^2}{9 \times 10^9}} = \frac{1}{10} \text{ C}$$

Q#2: Two positive charges (+8.0 C and +2.0 C) are separated by 300 m. A third charge is placed a distance r from the +8.0 C charge so that the resultant electric force on the third charge due to the other two charges is zero. The distance r is : (A1 200 m.



$$\frac{6}{6} \quad |F_{13}| = |F_{23}|$$

$$\frac{kq_1q_3}{(300-d)^2} = \frac{kq_2q_3}{d^2} \Rightarrow \frac{\sqrt{q_1}}{300-d} = \frac{\sqrt{q_2}}{d}$$

$$2 \frac{\sqrt{8}}{300-d} = \frac{\sqrt{2}}{d} \Rightarrow \frac{2}{300-d} = \frac{1}{d}$$

$$2d = 300 - d$$

$$3d = 300$$

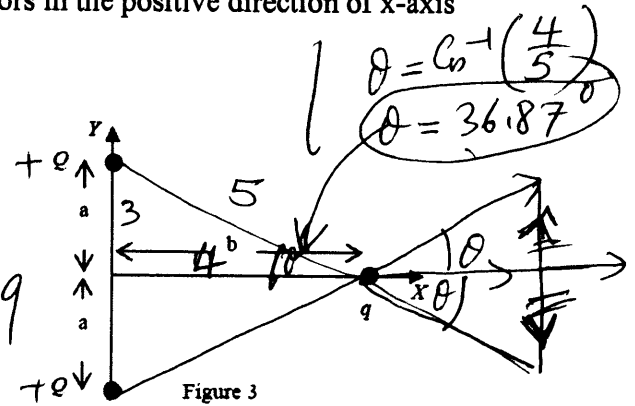
$$d = 100 \text{ m}$$

$$\text{distance from } q_1 = 300 - d = 300 - 100 = 200 \text{ m}$$

Quiz #5 Ch.#21 T131-Sec. 7-9-v10

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Q#1 In figure 3, $Q = 60 \text{ micro-C}$, $q = 20 \text{ micro-C}$, $a = 3.0 \text{ m}$, and $b = 4.0 \text{ m}$. Calculate the total electric force on q . [i and j are the unit vectors in the positive direction of x -axis and y -axis, respectively]. (A1 $0.69 i$ (N)).



$$|F_{net}| = 2 |F_{qQ-x}|$$

$$= 2 |F_{qQ}| \cos(36.9)$$

$$|F_{net}| = 2 \times \frac{k q Q}{(5)^2} \cos 37 = 0.69$$

$$\vec{F}_{net} = |F_{net}| \vec{i}$$

$$\vec{F}_{net} = 0.69 \vec{i}$$

Q#2: Consider two identical conductor spheres, A and B. Initially, sphere A has a charge of -80 Q and Sphere B has a charge of $+20 \text{ Q}$. If the spheres touched and then are separated by a distance of 0.3 m , what is the resultant force between them? [Take $Q = 5.7 \times 10^{-8} \text{ C}$] (A1 0.3 N).

After Touching Charge of each sphere

$$= \frac{-80Q + 20Q}{2} = -30Q$$

$$|F| = \frac{k (-30Q)^2}{(0.3)^2} = \frac{9 \times 10^9 \times (-30 \times 5.7 \times 10^{-8})^2}{(0.3)^2}$$

$$|F| = 0.292 \text{ N}$$