King Fahd University of Petroleum & Minerals Department of Mathematics and Statistics

> Math 102 Exam I 102 Saturday, March 26, 2011

EXAM COVER

Number of versions: 4 Number of questions: 20 Number of Answers: 5 per question

This exam was prepared using mcqs For questions send an email to Dr. Ibrahim Al-Lehyani (iallehyani@kaau.edu.sa) King Fahd University of Petroleum & Minerals Department of Mathematics and Statistics

> Math 102 Exam I 102 Saturday, March 26, 2011 Net Time Allowed: 120 minutes

MASTER VERSION

- 1. Using four rectangles and midpoint approximation, the area under the graph of $y = x^2$ from 1 to 9 is approximately equal to
 - (a) 240
 - (b) 180
 - (c) 120
 - (d) 84
 - (e) 164

2. An expression as a limit for the area under the graph of the function $y = x \cos x$ on $\left[0, \frac{\pi}{2}\right]$ is

(a)
$$\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi^2 i}{(2n)^2} \cos\left(\frac{\pi i}{2n}\right)$$

(b)
$$\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi^2 i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

(c)
$$\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

(d)
$$\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi^2 i}{n^2} \cos\left(\frac{\pi i}{n}\right)$$

(e) $\lim_{n \to +\infty} \sum_{i=1}^{1=n} \frac{\pi^2 i}{n} \cos\left(\frac{\pi i}{n}\right)$

MASTER

- 3. The limit $\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{4}{n} \cosh\left(\frac{4i}{n} + 2\right)$ can be interpreted as the area under the graph of the function
 - (a) $y = \cosh(x+2), \quad 0 \le x \le 4$
 - (b) $y = 2\cosh x, \quad 0 \le x \le 4$
 - (c) $y = \cosh \frac{x}{2}, \quad 0 \le x \le 4$
 - (d) $y = \cosh(x+2), \quad 2 \le x \le 4$
 - (e) $y = \cosh x, \quad 0 \le x \le 4$

- 4. If f is an even function and $\int_{-2}^{2} f(x)dx = 4$ and $\int_{0}^{7} f(x)dx = 3$, then $\int_{-2}^{7} f(x)dx$ is
 - (a) 5
 - (b) -1
 - (c) 1
 - (d) 7
 - (e) 10

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MASTER

5. If
$$f(x) = \begin{cases} -1, & 2 \le x \le 3\\ x - 4, & 3 \le x \le 9\\ 5, & 9 \le x \le 10 \end{cases}$$
, then $\int_2^{10} f(x) \, dx$ is

- (a) 16
- (b) 15
- (c) 17
- (d) 18
- (e) 19

6. The value of the integral $\int_{-4}^{0} (2 + \sqrt{16 - x^2}) dx$ is

- (a) $8 + 4\pi$
- (b) 4π
- (c) 8
- (d) $2 + 8\pi$
- (e) $-8 + 8\pi$

7. Let
$$f(x) = \int_{x^2}^{x^3} \tan^{-1} t \, dt$$
. Then $f(1) + f'(1)$ is

- (a) $\frac{\pi}{4}$
- (b) 0
- (c) $\frac{\pi}{2}$
- (d) 2
- (e) $\frac{\pi}{6}$

8. Let $F(x) = \int_{1}^{x} f(t) dt$ where $f(t) = \int_{1}^{t^{2}} \frac{\sqrt{1+u^{4}}}{u} du$. Then F''(2) is

- (a) $\sqrt{257}$
- (b) 16
- (c) $\sqrt{255}$
- (d) 15
- (e) $\sqrt{270}$

MASTER

- 9. If the velocity of a particle moving along a straight line is given by $v(t) = \frac{1}{2} \cos t$, the distance traveled during the interval time $\left[0, \frac{\pi}{2}\right]$ is
 - (a) $\sqrt{3} 1 \frac{\pi}{12}$
 - (b) $\frac{\pi}{4} 1$
 - (c) $\sqrt{3} 1 + \frac{\pi}{12}$
 - (d) $1 \frac{\pi}{4}$ (e) $\sqrt{3} + 1 - \frac{\pi}{12}$

- 10. The value of the integral $\int_{1}^{6} \frac{x^2 + 3x 5}{x^2} dx$ is
 - (a) $\frac{5}{6} + 3 \ln 6$ (b) $\frac{5}{6} - 3 \ln 6$ (c) $\frac{61}{6} + 3 \ln 6$ (d) $\frac{17}{6} + 3 \ln 6$ (e) $\frac{17}{6} - 3 \ln 6$

- 11. The value of the integral $\int_0^{\pi/4} \frac{1+\sin\theta}{\cos^2\theta} d\theta$ is
 - (a) $\sqrt{2}$ (b) 2 (c) $\frac{\sqrt{2}}{2}$ (d) $\frac{3\sqrt{2}}{2}$ (e) $\frac{\sqrt{2}}{3}$

12. The area under the curve $y = e^{\cos x} \sin x$ from 0 to $\frac{\pi}{2}$ is

- (a) e 1
- (b) e+1
- (c) $e^{-1} 1$
- (d) $e^{-1} + 1$
- (e) $e + e^{-1}$

MASTER

13. The value of the integral
$$\int_{1}^{e} \frac{dx}{2x + x \ln x^3}$$
 is

(a) $\frac{1}{3} \ln \frac{5}{2}$ (b) $\ln \frac{5}{2}$ (c) $\frac{1}{3} \ln 5$ (d) $\frac{1}{3} \ln 10$ (e) $\frac{1}{3 \ln 5}$

14. The area of the region bounded by the curves $y = \ln x$, x + y = 1, and y = 1 is

(a)
$$e - \frac{3}{2}$$

(b) $e - \frac{2}{3}$
(c) $e - \frac{1}{2}$
(d) $\frac{e}{2} - \frac{1}{2}$
(e) $e - \frac{1}{4}$

15. The area of the region inside the circle $y^2 + x^2 - 2x = 0$ and above the parabola $y = x^2$ is

(a)
$$\int_0^1 (\sqrt{1 - (x - 1)^2} - x^2) dx$$

(b)
$$\int_0^1 (\sqrt{1 + (x - 1)^2} - x^2) dx$$

(c) $\int_0^1 (\sqrt{1 - (1 - x)^2} + x^2) dx$

(d)
$$\int_{-1}^{1} (\sqrt{1 - (x - 1)^2} - x^2) dx$$

(e)
$$\int_{-1}^{1} (\sqrt{(x-1)^2 + 1} - x^2) dx$$

- 16. The area of the region enclosed by the graphs of the functions $y = x^3 x$ and y = 3x is
 - (a) 8
 - (b) 0
 - (c) $\frac{7}{2}$
 - (d) 4
 - (e) 2

MASTER

- 17. The volume of the solid obtained when the region bounded by $y = e^x$, $y = \frac{1}{x+1}$, x = 0 and x = 1 is rotated about *x*-axis is
 - (a) $\frac{\pi}{2}(e^2 2)$ (b) $\pi(e^2 - 2)$ (c) $\pi\left(e^2 - \frac{1}{2}\right)$ (d) $\frac{\pi}{2}(e - 1)$ (e) $\frac{\pi}{2}(e^2 - 1)$

- 18. The base of a solid is bounded by the curves $y = x^3$, y = 0and x = 1. If the cross-sections of the solid perpendicular to the x-axis are squares, then the volume of the solid is
 - (a) $\frac{1}{7}$ (b) $\frac{3}{4}$ (c) $\frac{1}{2}$ (d) $\frac{3}{7}$ (e) 1

MASTER

19. The volume of the solid generated when the region enclosed by $y = x^3$, y = 1, and x = 0 is revolved about the line y = 1is equal to

(a)
$$2\pi \int_0^1 (y^{1/3} - y^{4/3}) dy$$

(b) $2\pi \int_0^1 (y^{4/3} - y^{1/3}) dy$
(c) $2\pi \int_0^1 (1 - y) y dy$
(d) $2\pi \int_0^1 (y - 1) y dy$
(e) $2\pi \int_0^1 (y - 1)^2 dy$

- 20. The volume of the solid generated by revolving the region bounded by the curves $y = \frac{1}{x}$, y = 0, x = 1 and x = 3about the line x = 3 is
 - (a) $2\pi(3\ln 3 2)$
 - (b) $\pi \ln 3$
 - (c) $3\pi \ln 2$
 - (d) $2 \ln 3$
 - (e) $\pi (1 \ln 3)$

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ID: ______ Sec: _____.

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1. If
$$f(x) = \begin{cases} -1, & 2 \le x \le 3\\ x - 4, & 3 \le x \le 9\\ 5, & 9 \le x \le 10 \end{cases}$$
, then $\int_2^{10} f(x) \, dx$ is

- (a) 16
- (b) 18
- (c) 19
- (d) 17
- (e) 15

- 2. Using four rectangles and midpoint approximation, the area under the graph of $y = x^2$ from 1 to 9 is approximately equal to
 - (a) 180
 - (b) 164
 - (c) 84
 - (d) 120
 - (e) 240

- 3. If f is an even function and $\int_{-2}^{2} f(x)dx = 4$ and $\int_{0}^{7} f(x)dx = 3$, then $\int_{-2}^{7} f(x)dx$ is
 - (a) 5
 - (b) -1
 - (c) 7
 - (d) 1
 - (e) 10

4. An expression as a limit for the area under the graph of the function $y = x \cos x$ on $\left[0, \frac{\pi}{2}\right]$ is

(a)
$$\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

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$$\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi^2 i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

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- 5. The limit $\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{4}{n} \cosh\left(\frac{4i}{n} + 2\right)$ can be interpreted as the area under the graph of the function
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- 6. Let $F(x) = \int_{1}^{x} f(t) dt$ where $f(t) = \int_{1}^{t^{2}} \frac{\sqrt{1+u^{4}}}{u} du$. Then F''(2) is
 - (a) $\sqrt{270}$
 - (b) $\sqrt{255}$
 - (c) $\sqrt{257}$
 - (d) 15
 - (e) 16

7. Let
$$f(x) = \int_{x^2}^{x^3} \tan^{-1} t \, dt$$
. Then $f(1) + f'(1)$ is

- (a) $\frac{\pi}{2}$
- (b) 0
- (c) $\frac{\pi}{6}$
- (d) 2
- (e) $\frac{\pi}{4}$

8. If the velocity of a particle moving along a straight line is given by $v(t) = \frac{1}{2} - \cos t$, the distance traveled during the interval time $\left[0, \frac{\pi}{2}\right]$ is

(a) $\sqrt{3} - 1 - \frac{\pi}{12}$ (b) $\sqrt{3} + 1 - \frac{\pi}{12}$ (c) $\sqrt{3} - 1 + \frac{\pi}{12}$ (d) $\frac{\pi}{4} - 1$ (e) $1 - \frac{\pi}{4}$

- 9. The value of the integral $\int_1^6 \frac{x^2 + 3x 5}{x^2} dx$ is
 - (a) $\frac{5}{6} 3 \ln 6$ (b) $\frac{17}{6} + 3 \ln 6$ (c) $\frac{17}{6} - 3 \ln 6$ (d) $\frac{61}{6} + 3 \ln 6$ (e) $\frac{5}{6} + 3 \ln 6$

- 10. The value of the integral $\int_{-4}^{0} (2 + \sqrt{16 x^2}) dx$ is
 - (a) $8 + 4\pi$
 - (b) 8
 - (c) 4π
 - (d) $2 + 8\pi$
 - (e) $-8 + 8\pi$

11. The area under the curve $y = e^{\cos x} \sin x$ from 0 to $\frac{\pi}{2}$ is

- (a) e+1
- (b) $e + e^{-1}$
- (c) e 1
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12. The value of the integral $\int_{1}^{e} \frac{dx}{2x + x \ln x^3}$ is

(a)
$$\frac{1}{3} \ln \frac{5}{2}$$

(b) $\frac{1}{3 \ln 5}$
(c) $\frac{1}{3} \ln 5$
(d) $\ln \frac{5}{2}$
(e) $\frac{1}{3} \ln 10$

13. The value of the integral $\int_0^{\pi/4} \frac{1+\sin\theta}{\cos^2\theta} d\theta$ is

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$$\frac{3\sqrt{2}}{2}$$

(b) 2
(c) $\frac{\sqrt{2}}{3}$
(d) $\sqrt{2}$
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- (d) $\int_0^1 (\sqrt{1 + (x 1)^2} x^2) dx$

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- 16. The volume of the solid generated by revolving the region bounded by the curves $y = \frac{1}{x}$, y = 0, x = 1 and x = 3about the line x = 3 is
 - (a) $\pi(1 \ln 3)$
 - (b) $\pi \ln 3$
 - (c) $3\pi \ln 2$
 - (d) $2\pi(3\ln 3 2)$
 - (e) $2 \ln 3$

- 17. The area of the region enclosed by the graphs of the functions $y = x^3 x$ and y = 3x is
 - (a) 2
 - (b) $\frac{7}{2}$
 - (c) 8
 - (d) 4
 - (e) 0

- 18. The base of a solid is bounded by the curves $y = x^3$, y = 0and x = 1. If the cross-sections of the solid perpendicular to the x-axis are squares, then the volume of the solid is
 - (a) 1
 - (b) $\frac{3}{7}$ (c) $\frac{1}{2}$ (d) $\frac{3}{4}$
 - (e) $\frac{1}{7}$

19. The volume of the solid generated when the region enclosed by $y = x^3$, y = 1, and x = 0 is revolved about the line y = 1is equal to

(a)
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(b) $2\pi \int_0^1 (y^{4/3} - y^{1/3}) dy$
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Sec

1	a	b	с	d	е	f
2	a	b	с	d	е	f
3	a	b	с	d	е	f
4	a	b	с	d	е	f
5	a	b	с	d	е	f
6	a	b	с	d	е	f
7	a	b	с	d	е	f
8	a	b	с	d	е	f
9	a	b	с	d	е	f
10	a	b	с	d	е	f
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51	a	b	с	d	е	f
52	a	b	с	d	е	f
53	a	b	с	d	е	f
54	a	b	с	d	е	f
55	a	b	с	d	е	f
56	a	b	с	d	е	f
57	a	b	с	d	е	f
58	a	b	с	d	е	f
59	a	b	с	d	е	f
60	a	b	с	d	е	f
61	a	b	с	d	е	f
62	a	b	с	d	е	f
63	a	b	с	d	е	f
64	a	b	с	d	е	f
65	a	b	с	d	е	f
66	a	b	с	d	е	f
67	a	b	с	d	е	f
68	a	b	с	d	е	f
69	a	b	с	d	е	f
70	a	b	с	d	е	f

001

King Fahd University of Petroleum & Minerals Department of Mathematics and Statistics

CODE 002	Math 102	CODE 002
	Exam I	
	102	
	Saturday, March 26, 2011	
	Net Time Allowed: 120 minutes	
Name:		

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 - (a) 164
 - (b) 120
 - (c) 84
 - (d) 180
 - (e) 240

2. If f is an even function and $\int_{-2}^{2} f(x)dx = 4$ and $\int_{0}^{7} f(x)dx = 3$, then $\int_{-2}^{7} f(x)dx$ is

- (a) 1
- (b) 7
- (c) -1
- (d) 10
- (e) 5

3. If
$$f(x) = \begin{cases} -1, & 2 \le x \le 3\\ x - 4, & 3 \le x \le 9\\ 5, & 9 \le x \le 10 \end{cases}$$
, then $\int_2^{10} f(x) \, dx$ is

- (a) 18
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(d)
$$\lim_{n \to +\infty} \sum_{i=1}^{1=n} \frac{\pi^2 i}{n} \cos\left(\frac{\pi i}{n}\right)$$

(e) $\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi^2 i}{n^2} \cos\left(\frac{\pi i}{n}\right)$

002

5. The limit $\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{4}{n} \cosh\left(\frac{4i}{n} + 2\right)$ can be interpreted as the area under the graph of the function

(a)
$$y = \cosh x, \quad 0 \le x \le 4$$

(b)
$$y = \cosh \frac{x}{2}, \quad 0 \le x \le 4$$

(c) $y = \cosh(x+2), \quad 2 \le x \le 4$

(d)
$$y = \cosh(x+2), \quad 0 \le x \le 4$$

(e)
$$y = 2\cosh x, \quad 0 \le x \le 4$$

6. The value of the integral $\int_{-4}^{0} (2 + \sqrt{16 - x^2}) dx$ is

- (a) $8 + 4\pi$
- (b) $-8 + 8\pi$
- (c) 8
- (d) $2 + 8\pi$
- (e) 4π

7. Let
$$f(x) = \int_{x^2}^{x^3} \tan^{-1} t \, dt$$
. Then $f(1) + f'(1)$ is

- (a) 0
- (b) 2
- (c) $\frac{\pi}{4}$
- (d) $\frac{\pi}{6}$
- (e) $\frac{\pi}{2}$

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 - (a) $\sqrt{3} + 1 \frac{\pi}{12}$ (b) $1 - \frac{\pi}{4}$ (c) $\sqrt{3} - 1 - \frac{\pi}{12}$ (d) $\frac{\pi}{4} - 1$ (e) $\sqrt{3} - 1 + \frac{\pi}{12}$

- 9. The value of the integral $\int_1^6 \frac{x^2 + 3x 5}{x^2} dx$ is
 - (a) $\frac{17}{6} + 3 \ln 6$ (b) $\frac{17}{6} - 3 \ln 6$ (c) $\frac{5}{6} - 3 \ln 6$ (d) $\frac{5}{6} + 3 \ln 6$ (e) $\frac{61}{6} + 3 \ln 6$

10. Let
$$F(x) = \int_{1}^{x} f(t) dt$$
 where $f(t) = \int_{1}^{t^2} \frac{\sqrt{1+u^4}}{u} du$. Then $F''(2)$ is

- (a) $\sqrt{255}$
- (b) $\sqrt{257}$
- (c) 16
- (d) $\sqrt{270}$
- (e) 15

11. The value of the integral $\int_{1}^{e} \frac{dx}{2x + x \ln x^3}$ is

(a)
$$\frac{1}{3 \ln 5}$$

(b) $\frac{1}{3} \ln \frac{5}{2}$
(c) $\frac{1}{3} \ln 10$
(d) $\ln \frac{5}{2}$
(e) $\frac{1}{3} \ln 5$

12. The area of the region bounded by the curves $y = \ln x$, x + y = 1, and y = 1 is

(a)
$$e - \frac{1}{2}$$

(b) $e - \frac{3}{2}$
(c) $e - \frac{1}{4}$
(d) $\frac{e}{2} - \frac{1}{2}$
(e) $e - \frac{2}{3}$

13. The area of the region inside the circle $y^2 + x^2 - 2x = 0$ and above the parabola $y = x^2$ is

(a)
$$\int_{-1}^{1} (\sqrt{1 - (x - 1)^2} - x^2) dx$$

(b)
$$\int_{-1}^{1} (\sqrt{(x-1)^2 + 1} - x^2) dx$$

(c) $\int_0^1 (\sqrt{1 - (x - 1)^2} - x^2) dx$

(d)
$$\int_0^1 (\sqrt{1 + (x - 1)^2} - x^2) dx$$

(e)
$$\int_0^1 (\sqrt{1 - (1 - x)^2} + x^2) dx$$

14. The area under the curve $y = e^{\cos x} \sin x$ from 0 to $\frac{\pi}{2}$ is

- (a) $e^{-1} 1$
- (b) $e + e^{-1}$
- (c) $e^{-1} + 1$
- (d) e 1
- (e) e+1

- 15. The value of the integral $\int_0^{\pi/4} \frac{1+\sin\theta}{\cos^2\theta} d\theta$ is
 - (a) 2 (b) $\frac{\sqrt{2}}{2}$ (c) $\frac{\sqrt{2}}{3}$

(d)
$$\frac{3\sqrt{2}}{2}$$

(e) $\sqrt{2}$

- 16. The volume of the solid generated by revolving the region bounded by the curves $y = \frac{1}{x}$, y = 0, x = 1 and x = 3 about the line x = 3 is
 - (a) $2\pi(3\ln 3 2)$
 - (b) $3\pi \ln 2$
 - (c) $\pi \ln 3$
 - (d) $\pi (1 \ln 3)$
 - (e) $2 \ln 3$

- 17. The base of a solid is bounded by the curves $y = x^3$, y = 0and x = 1. If the cross-sections of the solid perpendicular to the x-axis are squares, then the volume of the solid is
 - (a) 1
 - (b) $\frac{3}{7}$
 - (c) $\frac{1}{2}$
 - (d) $\frac{1}{7}$
 - (e) $\frac{3}{4}$

- 18. The volume of the solid obtained when the region bounded by $y = e^x$, $y = \frac{1}{x+1}$, x = 0 and x = 1 is rotated about x-axis is
 - (a) $\frac{\pi}{2}(e-1)$ (b) $\frac{\pi}{2}(e^2-2)$ (c) $\pi(e^2-2)$ (d) $\pi\left(e^2-\frac{1}{2}\right)$ (e) $\frac{\pi}{2}(e^2-1)$

19. The volume of the solid generated when the region enclosed by $y = x^3$, y = 1, and x = 0 is revolved about the line y = 1is equal to

(a)
$$2\pi \int_0^1 (y^{1/3} - y^{4/3}) dy$$

(b) $2\pi \int_0^1 (y - 1)^2 dy$
(c) $2\pi \int_0^1 (1 - y) y dy$
(d) $2\pi \int_0^1 (y^{4/3} - y^{1/3}) dy$
(e) $2\pi \int_0^1 (y - 1) y dy$

20. The area of the region enclosed by the graphs of the functions $y = x^3 - x$ and y = 3x is

- (a) $\frac{7}{2}$ (b) 4 (c) 8 (d) 0
- (e) 2

Sec

1	a	b	с	d	е	f
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67	a	b	с	d	е	f
68	a	b	с	d	е	f
69	a	b	с	d	е	f
70	a	b	с	d	е	f

002
King Fahd University of Petroleum & Minerals Department of Mathematics and Statistics

CODE 003	Math 102	CODE 00	3
	Exam I		
	102		
	Saturday, March 26, 2011		
	Net Time Allowed: 120 minutes		
Name:			

ID: ______ Sec: _____

Check that this exam has 20 questions.

Important Instructions:

- 1. All types of calculators, pagers or mobile phones are NOT allowed during the examination.
- 2. Use HB 2.5 pencils only.
- 3. Use a good eraser. DO NOT use the erasers attached to the pencil.
- 4. Write your name, ID number and Section number on the examination paper and in the upper left corner of the answer sheet.
- 5. When bubbling your ID number and Section number, be sure that the bubbles match with the numbers that you write.
- 6. The Test Code Number is already bubbled in your answer sheet. Make sure that it is the same as that printed on your question paper.
- 7. When bubbling, make sure that the bubbled space is fully covered.
- 8. When erasing a bubble, make sure that you do not leave any trace of penciling.

1. An expression as a limit for the area under the graph of the function $y = x \cos x$ on $\left[0, \frac{\pi}{2}\right]$ is

(a)
$$\lim_{n \to +\infty} \sum_{i=1}^{1=n} \frac{\pi^2 i}{n} \cos\left(\frac{\pi i}{n}\right)$$

(b)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi^2 i}{(2n)^2} \cos\left(\frac{\pi i}{2n}\right)$$

(c)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi^2 i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

(d)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

(e)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi^2 i}{n^2} \cos\left(\frac{\pi i}{n}\right)$$

- 2. Using four rectangles and midpoint approximation, the area under the graph of $y = x^2$ from 1 to 9 is approximately equal to
 - (a) 180
 - (b) 120
 - (c) 164
 - (d) 240
 - (e) 84

- 3. If f is an even function and $\int_{-2}^{2} f(x)dx = 4$ and $\int_{0}^{7} f(x)dx = 3$, then $\int_{-2}^{7} f(x)dx$ is
 - (a) 7
 - (b) -1
 - (c) 10
 - (d) 5
 - (e) 1

- 4. The limit $\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{4}{n} \cosh\left(\frac{4i}{n} + 2\right)$ can be interpreted as the area under the graph of the function
 - (a) $y = \cosh(x+2), \quad 0 \le x \le 4$
 - (b) $y = \cosh(x+2), \quad 2 \le x \le 4$
 - (c) $y = \cosh x, \quad 0 \le x \le 4$
 - (d) $y = 2\cosh x, \quad 0 \le x \le 4$
 - (e) $y = \cosh \frac{x}{2}$, $0 \le x \le 4$

5. If
$$f(x) = \begin{cases} -1, & 2 \le x \le 3\\ x - 4, & 3 \le x \le 9\\ 5, & 9 \le x \le 10 \end{cases}$$
, then $\int_2^{10} f(x) \, dx$ is

- (a) 17
- (b) 18
- (c) 16
- (d) 15
- (e) 19

6. The value of the integral $\int_1^6 \frac{x^2 + 3x - 5}{x^2} dx$ is

(a)
$$\frac{17}{6} + 3 \ln 6$$

(b) $\frac{5}{6} - 3 \ln 6$
(c) $\frac{61}{6} + 3 \ln 6$
(d) $\frac{5}{6} + 3 \ln 6$
(e) $\frac{17}{6} - 3 \ln 6$

7. Let
$$F(x) = \int_{1}^{x} f(t) dt$$
 where $f(t) = \int_{1}^{t^2} \frac{\sqrt{1+u^4}}{u} du$. Then $F''(2)$ is

- (a) $\sqrt{270}$
- (b) 15
- (c) $\sqrt{255}$
- (d) $\sqrt{257}$
- (e) 16

8. Let
$$f(x) = \int_{x^2}^{x^3} \tan^{-1} t \, dt$$
. Then $f(1) + f'(1)$ is

- (a) $\frac{\pi}{2}$
- (b) 2
- (c) 0
- (d) $\frac{\pi}{6}$
- (e) $\frac{\pi}{4}$

- 9. If the velocity of a particle moving along a straight line is given by $v(t) = \frac{1}{2} \cos t$, the distance traveled during the interval time $\left[0, \frac{\pi}{2}\right]$ is
 - (a) $\frac{\pi}{4} 1$
 - (b) $\sqrt{3} 1 + \frac{\pi}{12}$
 - (c) $1 \frac{\pi}{4}$
 - (d) $\sqrt{3} 1 \frac{\pi}{12}$
 - (e) $\sqrt{3} + 1 \frac{\pi}{12}$

- 10. The value of the integral $\int_{-4}^{0} (2 + \sqrt{16 x^2}) dx$ is
 - (a) 8
 - (b) $2 + 8\pi$
 - (c) $-8 + 8\pi$
 - (d) 4π
 - (e) $8 + 4\pi$

11. The area of the region inside the circle $y^2 + x^2 - 2x = 0$ and above the parabola $y = x^2$ is

(a)
$$\int_{-1}^{1} (\sqrt{1 - (x - 1)^2} - x^2) dx$$

(b)
$$\int_{-1}^{1} (\sqrt{(x-1)^2 + 1} - x^2) dx$$

(c)
$$\int_0^1 (\sqrt{1 + (x - 1)^2} - x^2) dx$$

(d)
$$\int_0^1 (\sqrt{1 - (x - 1)^2} - x^2) dx$$

(e)
$$\int_0^1 (\sqrt{1 - (1 - x)^2} + x^2) dx$$

12. The value of the integral
$$\int_{1}^{e} \frac{dx}{2x + x \ln x^3}$$
 is

(a)
$$\frac{1}{3} \ln 10$$

(b) $\frac{1}{3 \ln 5}$
(c) $\frac{1}{3} \ln 5$
(d) $\frac{1}{3} \ln \frac{5}{2}$
(e) $\ln \frac{5}{2}$

- 13. The value of the integral $\int_0^{\pi/4} \frac{1+\sin\theta}{\cos^2\theta} d\theta$ is
 - (a) 2 (b) $\sqrt{2}$ (c) $\frac{\sqrt{2}}{2}$ (d) $\frac{\sqrt{2}}{3}$ (e) $\frac{3\sqrt{2}}{2}$

14. The area of the region bounded by the curves $y = \ln x$, x + y = 1, and y = 1 is

(a)
$$e - \frac{1}{4}$$

(b) $e - \frac{3}{2}$
(c) $\frac{e}{2} - \frac{1}{2}$
(d) $e - \frac{2}{3}$
(e) $e - \frac{1}{2}$

15. The area under the curve $y = e^{\cos x} \sin x$ from 0 to $\frac{\pi}{2}$ is

- (a) $e^{-1} + 1$
- (b) e 1
- (c) $e^{-1} 1$
- (d) e + 1
- (e) $e + e^{-1}$

- 16. The volume of the solid generated when the region enclosed by $y = x^3$, y = 1, and x = 0 is revolved about the line y = 1is equal to
 - (a) $2\pi \int_0^1 (y^{4/3} y^{1/3}) dy$ (b) $2\pi \int_0^1 (y - 1)^2 dy$ (c) $2\pi \int_0^1 (1 - y) y dy$ (d) $2\pi \int_0^1 (y - 1) y dy$ (e) $2\pi \int_0^1 (y^{1/3} - y^{4/3}) dy$

- 17. The volume of the solid generated by revolving the region bounded by the curves $y = \frac{1}{x}$, y = 0, x = 1 and x = 3about the line x = 3 is
 - (a) $3\pi \ln 2$
 - (b) $2 \ln 3$
 - (c) $2\pi(3\ln 3 2)$
 - (d) $\pi (1 \ln 3)$
 - (e) $\pi \ln 3$

- 18. The volume of the solid obtained when the region bounded by $y = e^x$, $y = \frac{1}{x+1}$, x = 0 and x = 1 is rotated about *x*-axis is
 - (a) $\pi \left(e^2 \frac{1}{2} \right)$ (b) $\pi (e^2 - 2)$ (c) $\frac{\pi}{2} (e^2 - 2)$ (d) $\frac{\pi}{2} (e - 1)$ (e) $\frac{\pi}{2} (e^2 - 1)$

- 19. The base of a solid is bounded by the curves $y = x^3$, y = 0and x = 1. If the cross-sections of the solid perpendicular to the x-axis are squares, then the volume of the solid is
 - (a) 1
 - (b) $\frac{3}{7}$
 - (c) $\frac{1}{2}$
 - (d) $\frac{3}{4}$
 - (e) $\frac{1}{7}$

- 20. The area of the region enclosed by the graphs of the functions $y = x^3 x$ and y = 3x is
 - (a) 4
 - (b) $\frac{7}{2}$
 - (c) 0
 - (d) 2
 - (e) 8

Sec

1	a	b	с	d	е	f
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King Fahd University of Petroleum & Minerals Department of Mathematics and Statistics

CODE 004	Math 102	CODE 004
	Exam I	
	102	
	Saturday, March 26, 2011	
	Net Time Allowed: 120 minutes	
Name:		

ID: _____ Sec: _

Check that this exam has 20 questions.

Important Instructions:

- 1. All types of calculators, pagers or mobile phones are NOT allowed during the examination.
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- 3. Use a good eraser. DO NOT use the erasers attached to the pencil.
- 4. Write your name, ID number and Section number on the examination paper and in the upper left corner of the answer sheet.
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- 6. The Test Code Number is already bubbled in your answer sheet. Make sure that it is the same as that printed on your question paper.
- 7. When bubbling, make sure that the bubbled space is fully covered.
- 8. When erasing a bubble, make sure that you do not leave any trace of penciling.

- 1. The limit $\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{4}{n} \cosh\left(\frac{4i}{n} + 2\right)$ can be interpreted as the area under the graph of the function
 - (a) $y = \cosh(x+2), \quad 0 \le x \le 4$
 - (b) $y = \cosh \frac{x}{2}, \quad 0 \le x \le 4$
 - (c) $y = \cosh x, \quad 0 \le x \le 4$
 - (d) $y = 2\cosh x, \quad 0 \le x \le 4$
 - (e) $y = \cosh(x+2), \quad 2 \le x \le 4$

- 2. If f is an even function and $\int_{-2}^{2} f(x)dx = 4$ and $\int_{0}^{7} f(x)dx = 3$, then $\int_{-2}^{7} f(x)dx$ is
 - (a) 7
 - (b) 10
 - (c) -1
 - (d) 1
 - (e) 5

3. If
$$f(x) = \begin{cases} -1, & 2 \le x \le 3\\ x - 4, & 3 \le x \le 9\\ 5, & 9 \le x \le 10 \end{cases}$$
, then $\int_2^{10} f(x) \, dx$ is

- (a) 19
- (b) 15
- (c) 16
- (d) 17
- (e) 18

An expression as a limit for the area under the graph of the 4. function $y = x \cos x$ on $\left[0, \frac{\pi}{2}\right]$ is

(a)
$$\lim_{n \to +\infty} \sum_{i=1}^{1=n} \frac{\pi^2 i}{n} \cos\left(\frac{\pi i}{n}\right)$$

(b)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

(c)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi^2 i}{2n^2} \cos\left(\frac{\pi i}{2n}\right)$$

(d)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi^2 i}{n^2} \cos\left(\frac{\pi i}{n}\right)$$

(e)
$$\lim_{n \to +\infty} \sum_{i=1}^n \frac{\pi^2 i}{(2n)^2} \cos\left(\frac{\pi i}{2n}\right)$$

e)
$$\lim_{n \to +\infty} \sum_{i=1}^{n} \frac{\pi i}{(2n)^2} \cos\left(\frac{\pi i}{2n}\right)$$

- 5. Using four rectangles and midpoint approximation, the area under the graph of $y = x^2$ from 1 to 9 is approximately equal to
 - (a) 180
 - (b) 84
 - (c) 120
 - (d) 240
 - (e) 164

- 6. If the velocity of a particle moving along a straight line is given by $v(t) = \frac{1}{2} \cos t$, the distance traveled during the interval time $\left[0, \frac{\pi}{2}\right]$ is
 - (a) $\frac{\pi}{4} 1$ (b) $\sqrt{3} + 1 - \frac{\pi}{12}$ (c) $\sqrt{3} - 1 + \frac{\pi}{12}$ (d) $\sqrt{3} - 1 - \frac{\pi}{12}$ (e) $1 - \frac{\pi}{4}$

- 7. The value of the integral $\int_{-4}^{0} (2 + \sqrt{16 x^2}) dx$ is
 - (a) 4π
 - (b) $2 + 8\pi$
 - (c) $8 + 4\pi$
 - (d) $-8 + 8\pi$
 - (e) 8

8. Let
$$F(x) = \int_{1}^{x} f(t) dt$$
 where $f(t) = \int_{1}^{t^{2}} \frac{\sqrt{1+u^{4}}}{u} du$. Then $F''(2)$ is

- (a) 15
- (b) $\sqrt{255}$
- (c) $\sqrt{270}$
- (d) 16
- (e) $\sqrt{257}$

9. Let
$$f(x) = \int_{x^2}^{x^3} \tan^{-1} t \, dt$$
. Then $f(1) + f'(1)$ is

(a) $\frac{\pi}{6}$ (b) $\frac{\pi}{2}$ (c) 2 (d) $\frac{\pi}{4}$

(e)
$$0$$

10. The value of the integral $\int_{1}^{6} \frac{x^2 + 3x - 5}{x^2} dx$ is

(a) $\frac{17}{6} + 3 \ln 6$ (b) $\frac{5}{6} - 3 \ln 6$ (c) $\frac{17}{6} - 3 \ln 6$ (d) $\frac{5}{6} + 3 \ln 6$ (e) $\frac{61}{6} + 3 \ln 6$

11. The value of the integral $\int_{1}^{e} \frac{dx}{2x + x \ln x^3}$ is

(a) $\frac{1}{3} \ln \frac{5}{2}$ (b) $\frac{1}{3} \ln 5$ (c) $\ln \frac{5}{2}$ (d) $\frac{1}{3 \ln 5}$ (e) $\frac{1}{3} \ln 10$

12. The area of the region inside the circle $y^2 + x^2 - 2x = 0$ and above the parabola $y = x^2$ is

(a)
$$\int_{-1}^{1} (\sqrt{(x-1)^2 + 1} - x^2) dx$$

(b) $\int_{-1}^{1} (\sqrt{1 - (x-1)^2} - x^2) dx$
(c) $\int_{0}^{1} (\sqrt{1 - (x-1)^2} - x^2) dx$
(d) $\int_{0}^{1} (\sqrt{1 + (x-1)^2} - x^2) dx$

(e)
$$\int_0^1 (\sqrt{1 - (1 - x)^2} + x^2) dx$$

13. The value of the integral $\int_0^{\pi/4} \frac{1+\sin\theta}{\cos^2\theta} d\theta$ is

(a)
$$\frac{3\sqrt{2}}{2}$$

(b) $\frac{\sqrt{2}}{3}$
(c) $\frac{\sqrt{2}}{2}$
(d) $\sqrt{2}$

(e) 2

14. The area of the region bounded by the curves $y = \ln x$, x + y = 1, and y = 1 is

(a)
$$e - \frac{1}{4}$$

(b) $e - \frac{3}{2}$
(c) $e - \frac{2}{3}$
(d) $e - \frac{1}{2}$
(e) $\frac{e}{2} - \frac{1}{2}$

15. The area under the curve $y = e^{\cos x} \sin x$ from 0 to $\frac{\pi}{2}$ is

- (a) $e + e^{-1}$
- (b) $e^{-1} 1$
- (c) $e^{-1} + 1$
- (d) e 1
- (e) e+1

- 16. The volume of the solid generated by revolving the region bounded by the curves $y = \frac{1}{x}$, y = 0, x = 1 and x = 3about the line x = 3 is
 - (a) $\pi \ln 3$
 - (b) $2 \ln 3$
 - (c) $2\pi(3\ln 3 2)$
 - (d) $3\pi \ln 2$
 - (e) $\pi (1 \ln 3)$

- 17. The volume of the solid obtained when the region bounded by $y = e^x$, $y = \frac{1}{x+1}$, x = 0 and x = 1 is rotated about x-axis is
 - (a) $\pi \left(e^2 \frac{1}{2} \right)$ (b) $\frac{\pi}{2} (e - 1)$ (c) $\frac{\pi}{2} (e^2 - 2)$
 - (d) $\frac{\pi}{2}(e^2-1)$
 - (e) $\pi(e^2 2)$

- 18. The base of a solid is bounded by the curves $y = x^3$, y = 0and x = 1. If the cross-sections of the solid perpendicular to the x-axis are squares, then the volume of the solid is
 - (a) $\frac{3}{4}$ (b) $\frac{1}{2}$ (c) $\frac{3}{7}$ (d) $\frac{1}{7}$ (e) 1

19. The volume of the solid generated when the region enclosed by $y = x^3$, y = 1, and x = 0 is revolved about the line y = 1is equal to

(a)
$$2\pi \int_0^1 (y^{1/3} - y^{4/3}) dy$$

(b) $2\pi \int_0^1 (y - 1) y dy$
(c) $2\pi \int_0^1 (y^{4/3} - y^{1/3}) dy$
(d) $2\pi \int_0^1 (1 - y) y dy$
(e) $2\pi \int_0^1 (y - 1)^2 dy$

20. The area of the region enclosed by the graphs of the functions $y = x^3 - x$ and y = 3x is

- (a) 4
- (b) 8
- (c) 0
- (d) 2
- (e) $\frac{7}{2}$

Sec

1	a	b	с	d	е	f
2	a	b	с	d	е	f
3	a	b	с	d	е	f
4	a	b	с	d	е	f
5	a	b	с	d	е	f
6	a	b	с	d	е	f
7	a	b	с	d	е	f
8	a	b	с	d	е	f
9	a	b	с	d	е	f
10	a	b	с	d	е	f
11	a	b	с	d	е	f
12	a	b	с	d	е	f
13	a	b	с	d	е	f
14	a	b	с	d	е	f
15	a	b	с	d	е	f
16	a	b	с	d	е	f
17	a	b	с	d	е	f
18	a	b	с	d	е	f
19	a	b	с	d	е	f
20	a	b	с	d	е	f
21	a	b	с	d	е	f
22	a	b	с	d	е	f
23	a	b	с	d	е	f
24	a	b	с	d	е	f
25	a	b	с	d	е	f
26	a	b	с	d	е	f
27	a	b	с	d	е	f
28	a	b	с	d	е	f
29	a	b	с	d	е	f
30	a	b	с	d	е	f
31	a	b	с	d	е	f
32	a	b	с	d	е	f
33	a	b	с	d	е	f
34	a	b	с	d	е	f
35	a	b	с	d	е	f

36	a	b	с	d	е	f
37	a	b	с	d	е	f
38	a	b	с	d	е	f
39	a	b	с	d	е	f
40	a	b	с	d	е	f
41	a	b	с	d	е	f
42	а	b	с	d	е	f
43	а	b	с	d	е	f
44	а	b	с	d	е	f
45	а	b	с	d	е	f
46	a	b	с	d	е	f
47	а	b	с	d	е	f
48	a	b	с	d	е	f
49	а	b	с	d	е	f
50	a	b	с	d	е	f
51	а	b	с	d	е	f
52	а	b	с	d	е	f
53	а	b	с	d	е	f
54	a	b	с	d	е	f
55	а	b	с	d	е	f
56	a	b	с	d	е	f
57	а	b	с	d	е	f
58	а	b	с	d	е	f
59	a	b	с	d	е	f
60	a	b	с	d	е	f
61	a	b	с	d	е	f
62	a	b	с	d	е	f
63	a	b	с	d	е	f
64	a	b	с	d	е	f
65	a	b	с	d	е	f
66	a	b	с	d	е	f
67	a	b	с	d	е	f
68	a	b	с	d	е	f
69	a	b	с	d	е	f
70	a	b	с	d	е	f

004

Q	MM	V1	V2	V3	V4
1	a	a	e	b	a
2	a	е	е	d	е
3	a	a	d	d	с
4	a	с	с	а	е
5	a	с	d	с	d
6	a	с	a	d	d
7	a	е	с	d	с
8	a	a	с	е	е
9	a	e	d	d	d
10	a	a	b	е	d
11	a	с	b	d	a
12	a	a	b	d	с
13	a	d	с	b	d
14	a	с	d	b	b
15	a	e	е	b	d
16	a	d	a	е	с
17	a	с	d	с	с
18	a	е	b	с	d
19	a	е	a	е	a
20	a	е	с	е	b

ANSWER KEY

Answer Counts

V	a	b	с	d	е
1	0	6	7	3	4
2	4	1	5	5	5
3	4	3	3	7	3
4	2	2	7	6	3