King Fahd University of Petroleum and Minerals Department of Mathematical Sciences Math 101 Final Exam Semester I, 2001–2002 (011)

Dr. Faisal Fairag

Name:			
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Sec:	7	11	
Serial No:			

Question #	Points
1	10
2	27
3	34
4	27
5	27
6	9
7-23	8 each
24	3 each
Total:	300

Form (2)

- 1. Let $f(x) = \frac{1}{3}x^3 \frac{1}{2}x^2$ (a) Find the interval on which f is decreasing

(b) Find the open interval on which f is concave up.

2. The equation $x^3 - x^2 - 2x + 1 = 0$ has one real solution for 0 < x < 1. Approximate it by Newton's Method. If $x_1 = 1$, then find x_6 .

3. Find the extreme values for $f(x) = x^{4/3} - 3x^{1/3}$ on the interval [-1,8] and determine where those values occur.

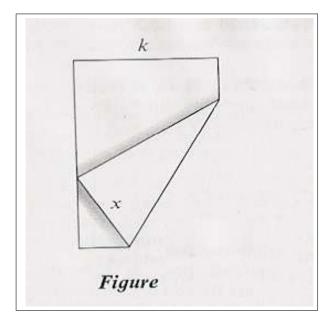
- 4. Let $f(x) = x^{2/3}(x+5)$ (a) Find all relative max. and all relative min.

(b) Find all inflection points

(c) Find all cusp which may or may not exist.

5. A rectangular field is to be bounded by a fence on three sides and by a wall on the fourth one. Find the dimensions of the field with maximum area that can be enclosed with 1000 meters of fence?

6. The lower corner of a page of width k is folded over so as just to reach the inner edge of the page (see Figure). Find the width of the part folded over (the value of x) when the area of the triangle floded over is a minimum.



7. Find the value of k, if possible, that will make the function continuous

$$f(x) = \begin{cases} x + 2k & x \le 1\\ kx^2 + x + 1 & x > 1 \end{cases}$$

- (a) -1
- (b) 2
- (c) 1
- (d) -2
- (e) none exists

8.
$$\lim_{x \to 0^+} (1 - \ln(2x))^{2x} =$$

- (a) 0
- (b) 1
- (c) $+\infty$
- (d) $-\infty$
- (e) -1

9. If $f(x) = x^4 - x$ on [-1, 1], find the value c that satisfies the Mean value Theorem.

- (a) 1
- (b) 0
- (c) 2
- (d) 3
- (e) 4

10.
$$\lim_{x\to 9} \frac{x+5}{\sqrt{x}-3} =$$

- (a) it does not exist
- (b) $+\infty$
- (c) $-\infty$
- (d) 84
- (e) -84

11.
$$\lim_{x \to -\infty} \sqrt{\frac{20x^{10} - 2x^5 + 2}{5x^{10} + x^5 - 3}} =$$

- (a) $+\infty$
- (b) 2
- (c) $-\infty$
- (d) -2
- (e) it does not exist

12. $y = \cot^{-1} \sqrt{x}$. Find dy/dx.

(a)
$$-\frac{x}{1+x}$$

(b)
$$-\frac{1}{2\sqrt{x}(1+x)}$$

(c)
$$-\frac{x}{(1+x^2)}$$

(d)
$$-\sqrt{\frac{1}{1+x^2}}$$

(e)
$$\frac{x}{1+x}$$

13.
$$\lim_{x \to 0^+} \frac{\sin x}{\ln(x^2 + 1)} =$$

- (a) $-\infty$
- (b) 10
- (c) 0
- (d) $+\infty$
- (e) -10

14. To prove that $\lim_{x\to 5}(x-2)=3$ a reasonable relationship between δ and ϵ would be

- (a) $\delta = \epsilon$
- (b) $\delta = 5\epsilon$
- (c) $\delta = \sqrt{\epsilon}$
- (d) $\delta = \frac{1}{\epsilon}$
- (e) $\delta = \frac{1}{\sqrt{\epsilon}}$

- 15. If $y = \frac{2}{x+3}$, then y'(0) =
 - (a) $\frac{-2}{9}$
 - (b) 0
 - (c) $\frac{4}{9}$
 - (d) $\frac{2}{9}$
 - (e) $\frac{-4}{9}$
- 16. $g(x) = x^3 f(x)$. Find g'(2), given that f(2) = 6 and f'(2) = 3
 - (a) 48
 - (b) -60
 - (c) 96
 - (d) 60
 - (e) -48
- 17. $y = x^{-3} + x$. Find y'''
 - (a) -6
 - (b) $-60x^{-6} + x^{-2}$
 - (c) $-60x^{-6} x^{-2}$
 - (d) $-3x^{-2} + 1$
 - (e) $-60x^{-6}$

18. If $y = x^5 \cos x$, find d^2y/dx^2

- (a) $20x^3 \cos x$
- (b) $20x^3 \cos x x^5 \cos x$
- (c) $20x^3\cos x + x^5\cos x$
- (d) $20x^3 \cos x 10x^4 \sin x x^5 \cos x$
- (e) $-x^5 \cos x$

19. Use dy to approximate $\sqrt{4.04}$ starting at x=4

- (a) 2.01
- (b) 1.99
- (c) 4.01
- (d) 3.99
- (e) 1.59

20. Find $\frac{dy}{dx}$ if $x^2 + y^2 = 49$.

- (a) $\frac{49x}{y}$
- (b) $\frac{x}{y}$
- (c) $-\frac{x}{y}$
- (d) $-\frac{49x}{y}$
- (e) $\frac{y}{x}$

- 21. find the limit $\lim_{x\to+\infty} \left(\cos\left(\frac{4}{x}\right) \cdot \sin\left(\frac{5}{x}\right)\right) =$
 - (a) 1
 - (b) -1
 - (c) $+\infty$
 - (d) $-\infty$
 - (e) 0
- 22. Find an equation for the tangent line to the curve $y = x^7 5$ at (1, -4).
 - (a) y = 7x
 - (b) y = 7x + 5
 - (c) y = 7x 3
 - (d) y = 7x 11
 - (e) y = 7x 5
- 23. The number of critical points for f(x) = |(x-1)(x-2)(x-3)| is
 - (a) 5
 - (b) 2
 - (c) 3
 - (d) 4
 - (e) 1

24. True (T) or False (F)

(a)
$$f(x) = |\tan^2 x|$$
 has no relative extrema on $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

(b)
$$f(x) = \frac{x^3}{x^5 - 2}$$
 has no horizontal asymptote ()

(c)
$$f(x) = |x^2 - 4|$$
 has points of discontinuity at $x = 2$ and $x = -2$.

(d) The function
$$f(x) = \frac{x+5}{x-1}$$
 has a removable discontinuity at $x = 1$

(e)
$$f(x) = \frac{1}{x^3}$$
 on $[-1, 1]$ satisfies the hypotheses of Rolle's Theorem (

(f) The Mean Value Theorem can be used on
$$f(x) = |x - 1|$$
 on $[-2, 1]$

(g)
$$\tan x$$
 has a point of inflection on $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

(h)
$$f(x) = x^{3/5}$$
 has a critical point (

(j) The slope of the tangent line to the graph of
$$f(x) = x^3 - 5$$
 at $x_0 = 3$ is 22.