

Image Enhancement (Spatial Filtering 2)

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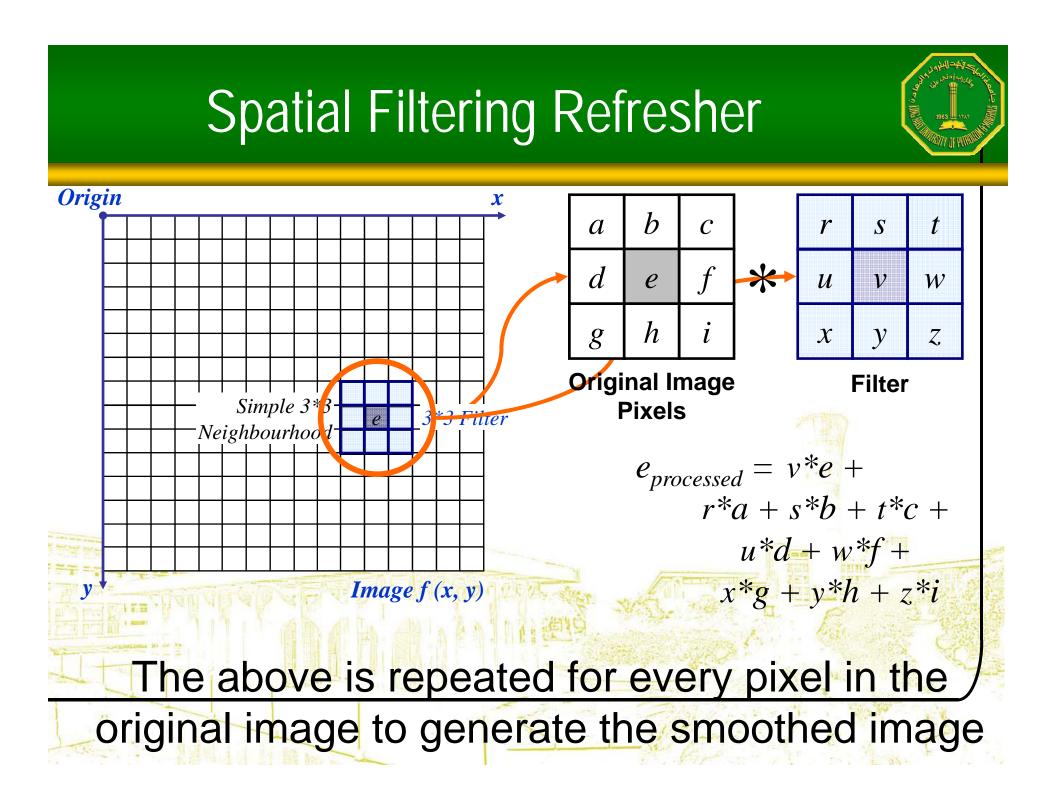
Contents



In this lecture we will look at more spatial filtering techniques

- Spatial filtering refresher
- Sharpening filters
 - 1st derivative filters
 - 2nd derivative filters

Combining filtering techniques



Sharpening Spatial Filters



Previously we have looked at smoothing filters which remove fine detail

Sharpening spatial filters seek to highlight fine detail

- Remove blurring from images
- Highlight edges

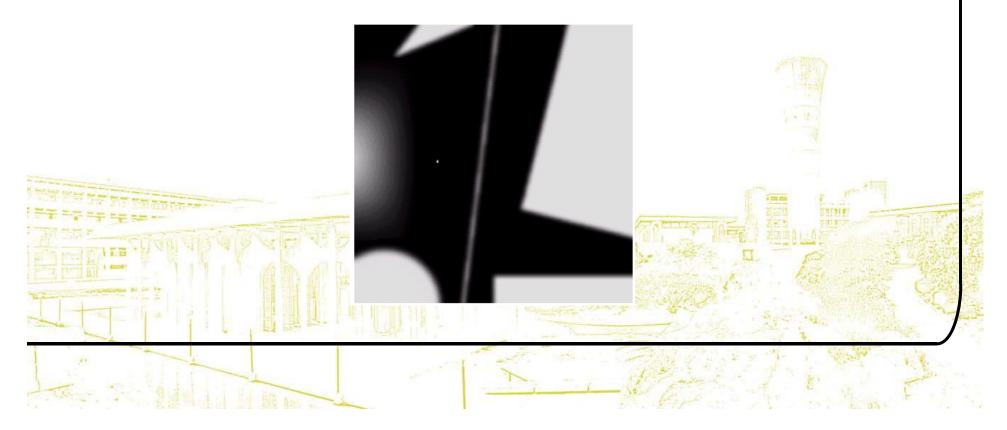
Sharpening filters are based on spatial differentiation

Spatial Differentiation

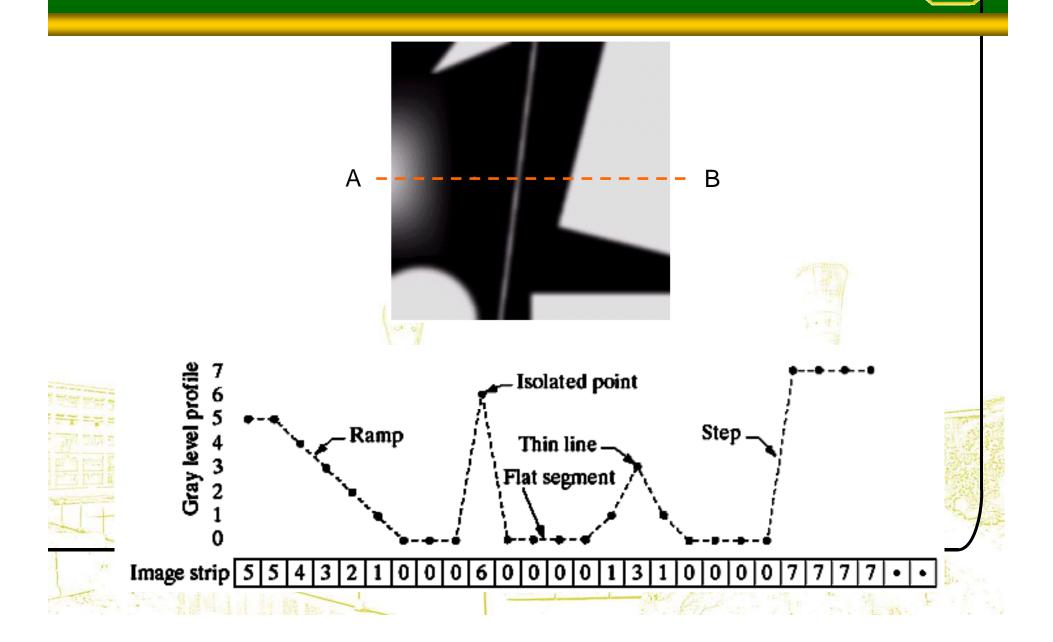


Differentiation measures the *rate of change* of a function

Let's consider a simple 1 dimensional example



Spatial Differentiation



1st Derivative



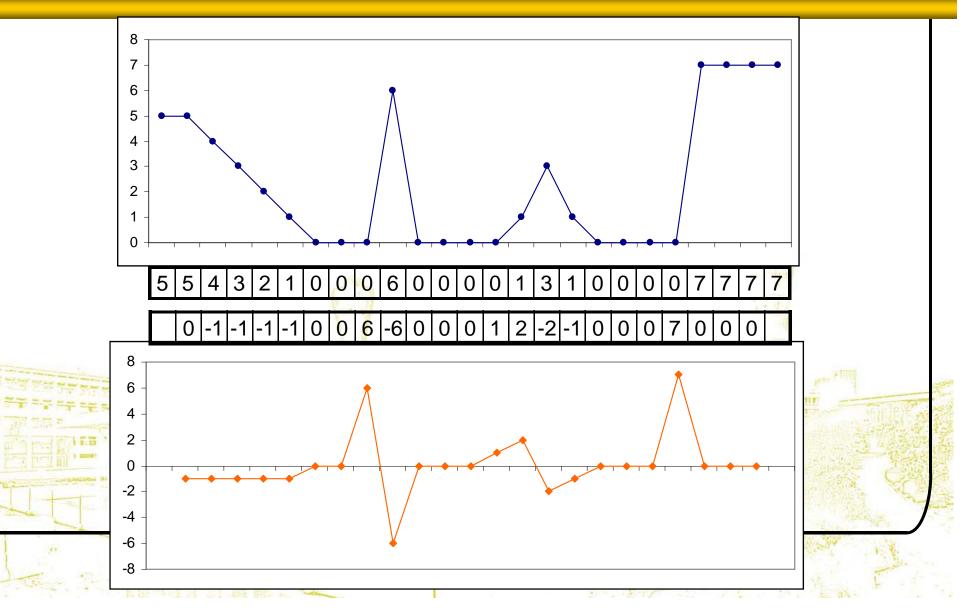
The formula for the 1^{st} derivative of a function is as follows:

$$\frac{\partial f}{\partial x} = f(x+1) - f(x)$$

It's just the difference between subsequent values and measures the rate of change of the function

1st Derivative (cont...)





2nd Derivative



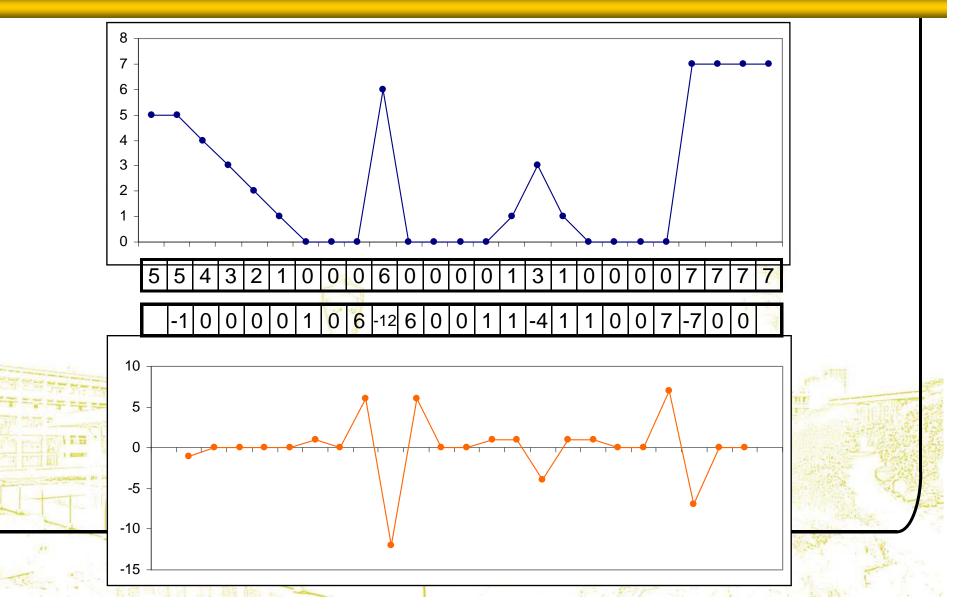
The formula for the 2nd derivative of a function is as follows: $\partial^2 f$

 $\frac{\partial^2 f}{\partial^2 x} = f(x+1) + f(x-1) - 2f(x)$

Simply takes into account the values both before and after the current value

2nd Derivative (cont...)





Using Second Derivatives For Image Enhancement

The 2nd derivative is more useful for image enhancement than the 1st derivative

- Stronger response to fine detail
- Simpler implementation
- We will come back to the 1st order derivative later on

The first sharpening filter we will look at is the Laplacian

Isotropic

One of the simplest sharpening filters

— We will look at a digital implementation

The Laplacian



The Laplacian is defined as follows:

$$\nabla^2 f = \frac{\partial^2 f}{\partial^2 x} + \frac{\partial^2 f}{\partial^2 y}$$

where the partial 1^{st} order derivative in the x direction is defined as follows:

$$\frac{\partial^2 f}{\partial^2 x} = f(x+1, y) + f(x-1, y) - 2f(x, y)$$

and in the y direction as follows:
$$\frac{\partial^2 f}{\partial^2 y} + f(x, y+1) + f(x, y-1) - 2f(x, y)$$

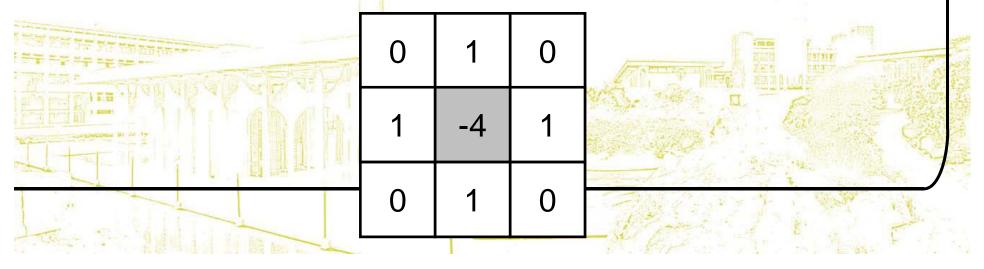
The Laplacian (cont...)



So, the Laplacian can be given as follows:

$$\nabla^2 f = [f(x+1, y) + f(x-1, y) + f(x, y-1)] + f(x, y+1) + f(x, y-1)] - 4f(x, y)$$

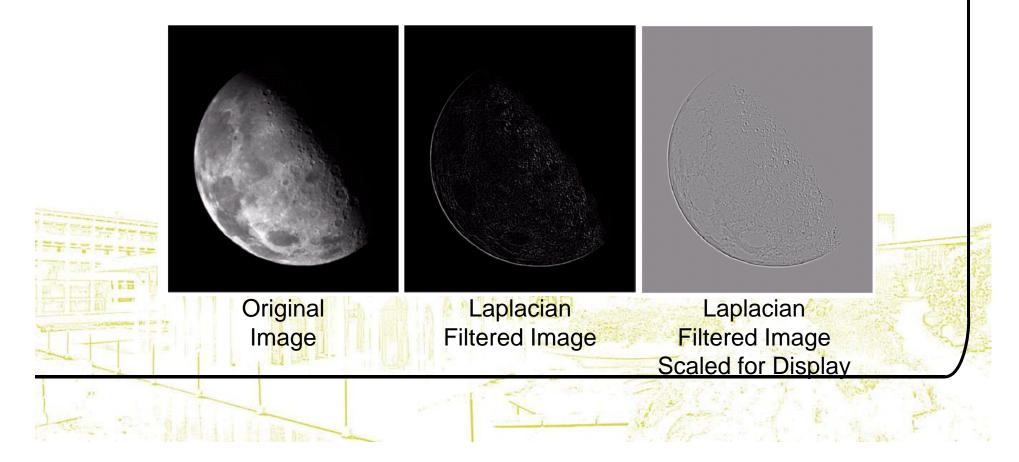
We can easily build a filter based on this



The Laplacian (cont...)



Applying the Laplacian to an image we get a new image that highlights edges and other discontinuities



But That Is Not Very Enhanced!

- The result of a Laplacian filtering is not an enhanced image
- We have to do more work in order to get our final image
- Subtract the Laplacian result from the original image to generate our final sharpened enhanced image

 $g(x, y) = f(x, y) - \nabla^2 f$

Laplacian Filtered Image Scaled for Display

Laplacian Image Enhancement Original Laplacian Sharpened **Filtered Image** Image Image In the final sharpened image edges and fine detail are much more obvious



Simplified Image Enhancement

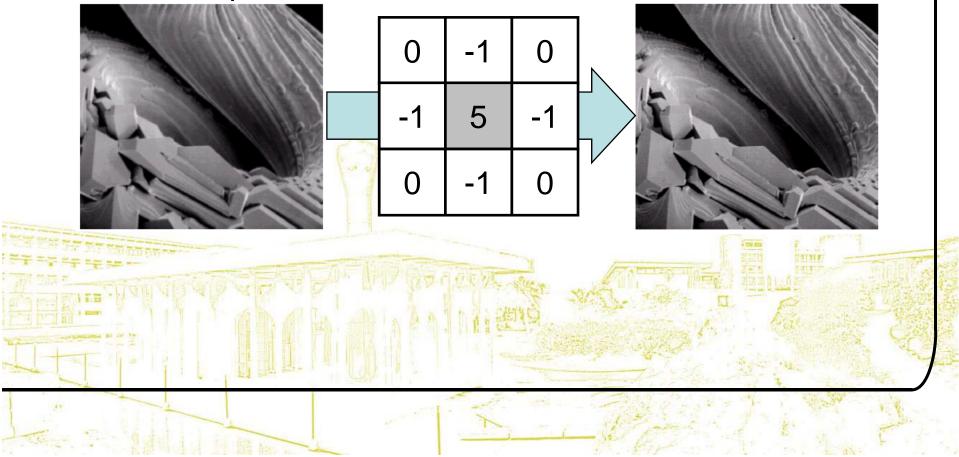


The entire enhancement can be combined into a single filtering operation $g(x, y) = f(x, y) - \nabla^2 f$ = f(x, y) - [f(x+1, y) + f(x-1, y)]+ f(x, y+1) + f(x, y-1)-4f(x, y)] =5f(x, y) - f(x+1, y) - f(x-1, y)-f(x, y+1) - f(x, y-1) - f(x

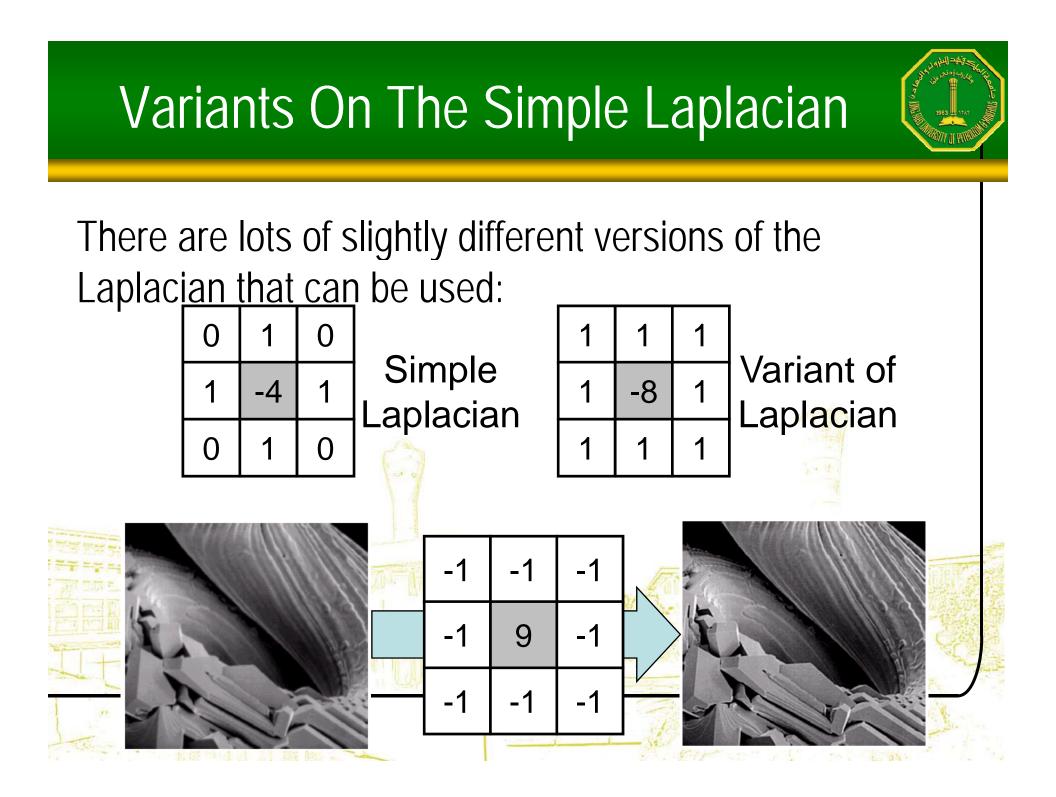
Simplified Image Enhancement (cont...)



This gives us a new filter which does the whole job for us in one step



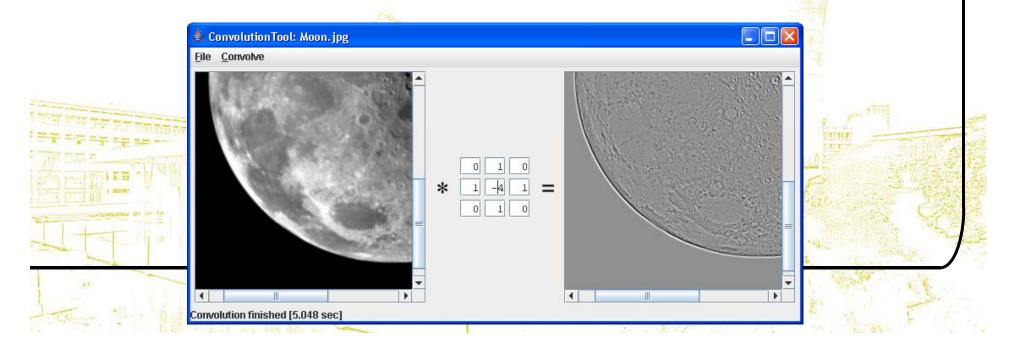
Simplified Image Enhancement (cont...) -



Simple Convolution Tool In Java

A great tool for testing out different filters

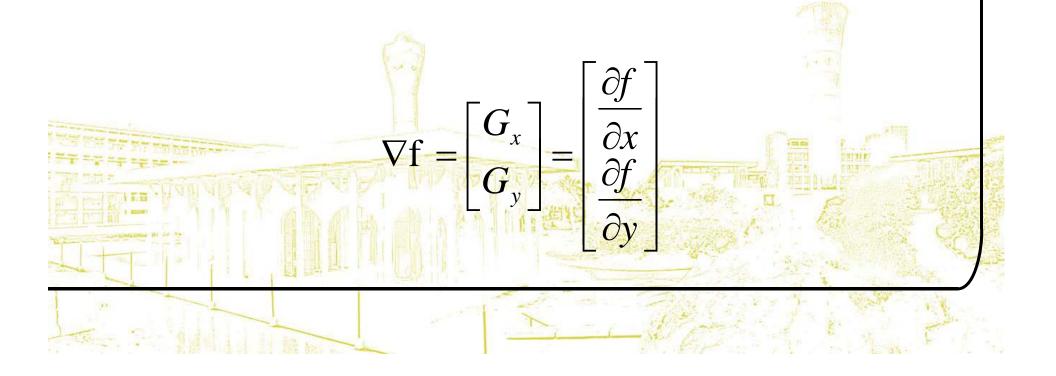
- From the book "Image Processing tools in Java"
- Available from webCT later on today
- To launch: java ConvolutionTool Moon.jpg



1st Derivative Filtering



Implementing 1st derivative filters is difficult in practice For a function f(x, y) the gradient of f at coordinates (x, y) is given as the column vector:



1st Derivative Filtering (cont...)

 $= \left[G_{x}^{2} + G_{y}^{2} \right]^{\frac{1}{2}}$

 $= \left[\left(\frac{\partial f}{\partial x} \right)^2 + \left(\frac{\partial f}{\partial y} \right)^2 \right]^{\frac{1}{2}}$

The magnitude of this vector is given by:

 $\nabla f = mag(\nabla f)$

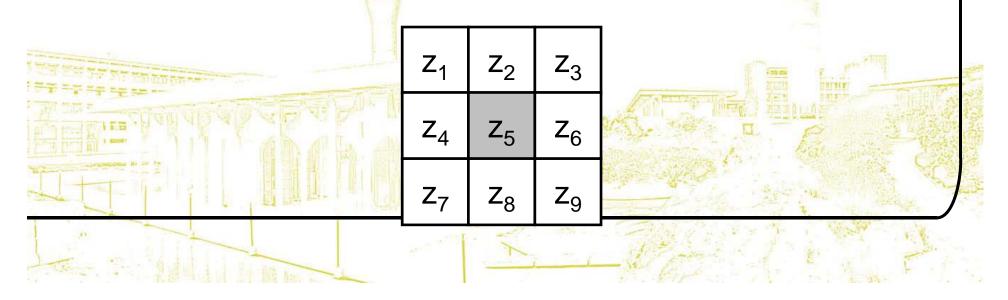
For practical reasons this can be simplified as: $\nabla f \approx |G_x| + |G_y|$

1st Derivative Filtering (cont...)

There is some debate as to how best to calculate these gradients but we will use:

$$7f \approx |(z_7 + 2z_8 + z_9) - (z_1 + 2z_2 + z_3)| + |(z_3 + 2z_6 + z_9) - (z_1 + 2z_4 + z_7)|$$

which is based on these coordinates



Sobel Operators



Based on the previous equations we can derive the *Sobel Operators*

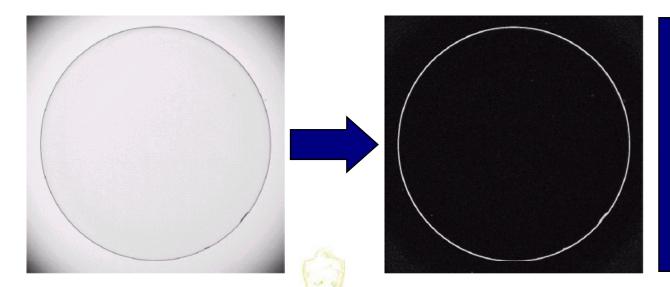
-1	-2	-1
0	0	0
1	2	1

-1	0	1
-2	0	2
-1	0	1

To filter an image it is filtered using both operators the results of which are added together

Sobel Example





An image of a contact lens which is enhanced in order to make defects (at four and five o'clock in the image) more obvious

Sobel filters are typically used for edge detection

1st & 2nd Derivatives



Comparing the 1st and 2nd derivatives we can conclude the following:

- 1st order derivatives generally produce thicker edges
- 2nd order derivatives have a stronger response to fine detail e.g. thin lines.
- 1st order derivatives have stronger response to grey level step

 2nd order derivatives produce a double response at step changes in grey level

Summary



In this lecture we looked at:

- Sharpening filters
 - 1st derivative filters
 - 2nd derivative filters
- Combining filtering techniques

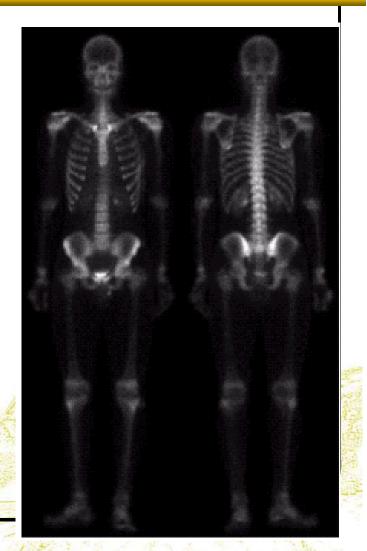
Combining Spatial Enhancement Methods



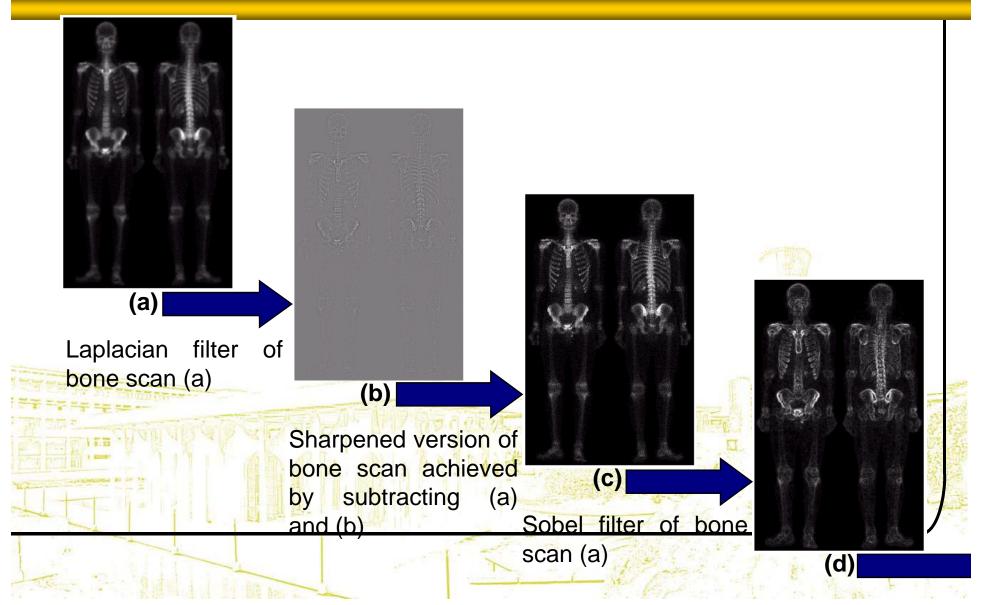
Successful image enhancement is typically not achieved using a single operation

Rather we combine a range of techniques in order to achieve a final result

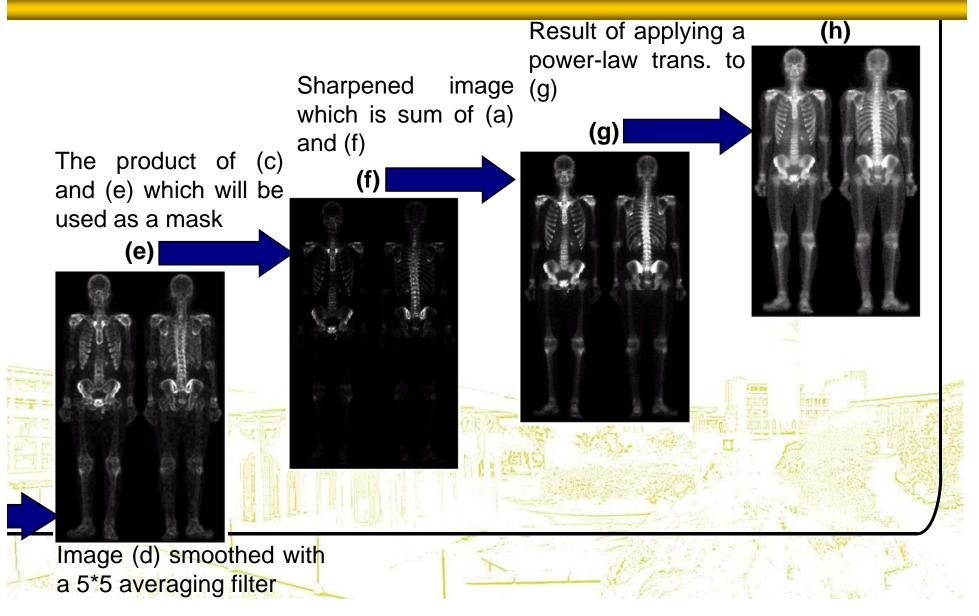
This example will focus on enhancing the bone scan to the right



Combining Spatial Enhancement Methods (cont...)



Combining Spatial Enhancement Methods (cont...)



Combining Spatial Enhancement Methods (cont...)

Compare the original and final images

