

# EE204

## Lecture 02

### Kirchhoff's Current and Voltage Laws

**Kirchoff's Current Law (KCL).**

The sum of currents *entering* a node is equal to the sum of currents *leaving* that node.

$$i_1 + i_4 = i_2 + i_3 + i_5$$

Equivalent statement of KCL:

The *algebraic* sum of currents *entering* a node is equal to zero.

$$i_1 - i_2 - i_3 + i_4 - i_5 = 0$$

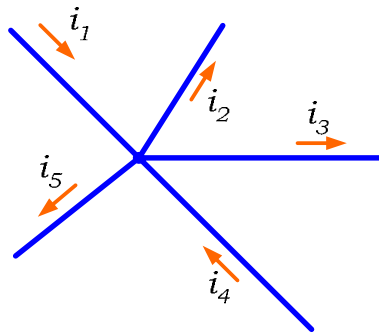


Figure 8

**Example 4:**

Calculate the unknown currents in the following circuits.

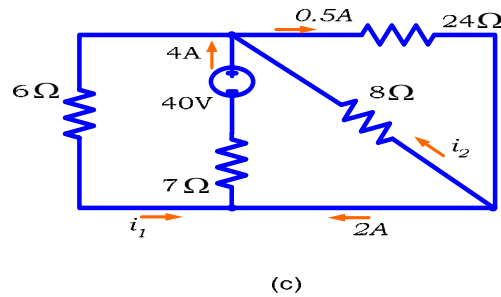
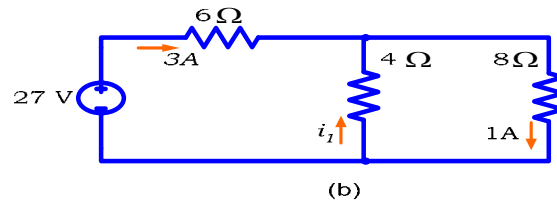
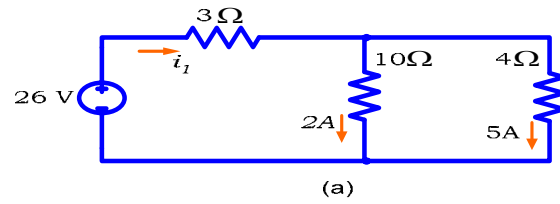


Figure 9

**Solution:**

a) KCL at node (a)  $\Rightarrow i_1 = 2 + 4 = 6A$

b) KCL at node (a)  $\Rightarrow 3 + i_1 = 1 \Rightarrow i_1 = -2A$

Alternatively

KCL at node (a)  $\Rightarrow 3 + i_1 - 1 = 0 \Rightarrow i_1 = -2A$

c) KCL at node (b)  $\Rightarrow i_1 - 4 + 2 = 0 \Rightarrow i_1 = 2A$

KCL at node (c)  $\Rightarrow 0.5 - i_2 - 2 = 0 \Rightarrow i_2 = -1.5A$

Check KCL at node (a)  $\Rightarrow$   
 $-i_1 + 4 + i_2 - 0.5 = -(2) + 4 + (-1.5) - 0.5 = -4 + 4 = 0$

KCL is also applicable to a *closed* area (super node).

The algebraic sum of currents entering a super node is equal to zero.

$$i_1 + i_2 - i_3 + i_4 - i_5 = 0$$

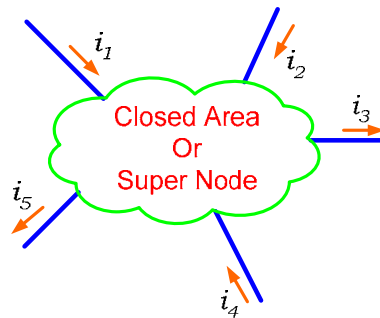


Figure 10

**Example:**

Calculate the currents  $i_1$  and  $i_2$  in the circuit shown below:

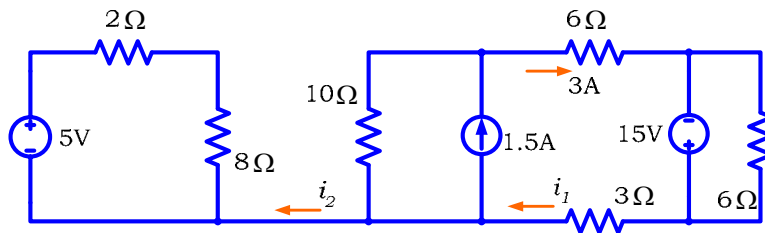


Figure 11

**Solution:**

$$\text{KCL at super node 1} \Rightarrow 3 - i_1 = 0 \Rightarrow i_1 = 3\text{A}$$

$$\text{KCL at super node 2} \Rightarrow i_2 = 0 \Rightarrow i_2 = 0\text{A}$$

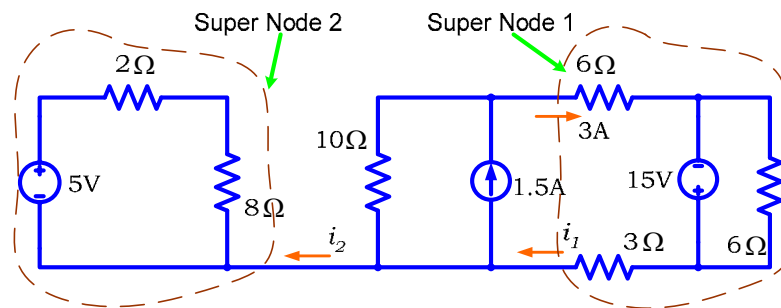


Figure 12

### Kirchoff's Voltage Law (KVL):

The *algebraic* sum of voltages around *any closed* circuit is equal to zero.

$$\text{KVL around circuit 1 (CW)} \quad \Rightarrow \quad -v_1 - v_2 + v_3 - v_4 + v_5 = 0 \quad (1)$$

$$\text{KVL around circuit 1 (CCW)} \quad \Rightarrow \quad +v_1 + v_2 - v_3 + v_4 - v_5 = 0 \quad (2) \text{ [same as (1)]}$$

CW = clockwise & CCW = counterclockwise

$$\text{KVL around the outer circuit (CW)} \quad \Rightarrow \quad -v_6 + v_8 + v_3 - v_4 + v_5 = 0 \quad (3)$$

$$\text{KVL around circuit 2 (CW)} \quad \Rightarrow \quad -v_6 + v_7 = 0 \quad \Rightarrow \quad v_6 = v_7 \quad (\text{parallel elements})$$

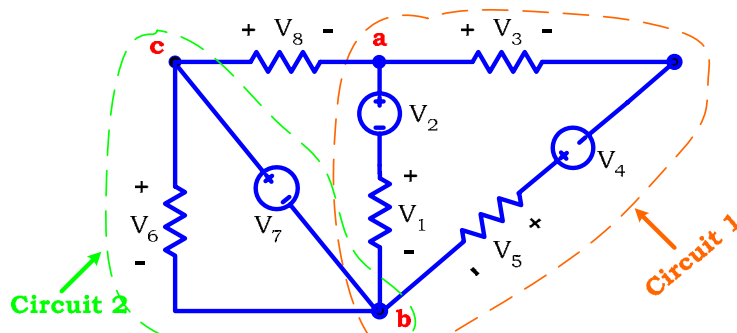


Figure 1

### Alternative KVL Statement:

The *algebraic* sum of voltages between two nodes is *independent* of the path taken from the first node to the second node.

$$\text{KVL } \text{Node } a \xrightarrow{\text{path1\&2}} \text{Node } b \quad \Rightarrow \quad +v_2 + v_1 = +v_3 - v_4 + v_5 \quad (4) \text{ [same as (1)]}$$

$$\text{KVL } \text{Node } a \xrightarrow{\text{path2\&3}} \text{Node } b \quad \Rightarrow \quad +v_3 - v_4 + v_5 = -v_8 + v_6 \quad (5) \text{ [same as (3)]}$$

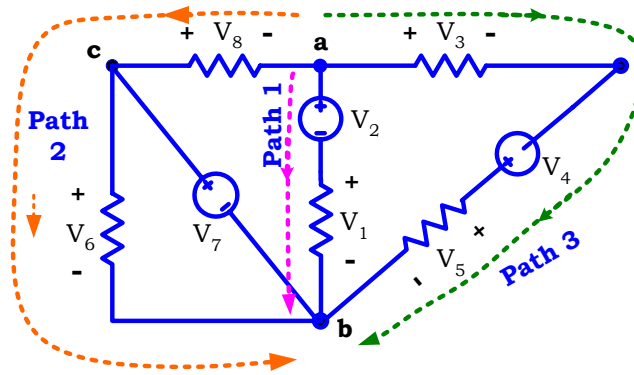


Figure 2

**Example:**

Calculate the unknown voltages in the given circuit.

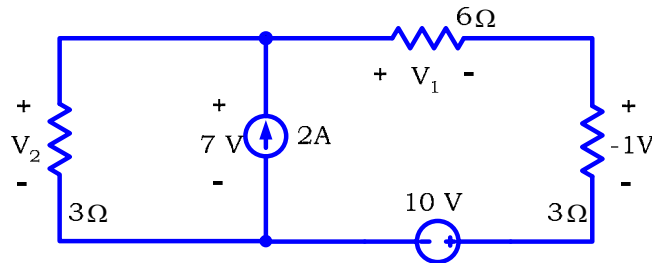


Figure 3

**Solution:**

Applying KVL:

$$\text{Right-hand circuit (CW)} \Rightarrow -(7) + v_1 + (-1) + 10 = 0 \Rightarrow v_1 = -2V$$

$$\text{Right-hand circuit (CCW)} \Rightarrow +(7) - (10) - (-1) - v_1 = 0 \Rightarrow v_1 = -2V$$

$$\text{Node } a \xrightarrow{\text{path1\&2}} \text{Node } b \Rightarrow +v_1 = +(7) - (10) - (-1) \Rightarrow v_1 = -2V$$

Same answer in all cases.

$$\text{Left-hand circuit (CW)} \Rightarrow +(7) - (v_2) = 0 \Rightarrow v_2 = 7V$$

$$\text{Node } a \xrightarrow{\text{path3\&4}} \text{Node } c \Rightarrow +v_2 = +7 \Rightarrow v_2 = 7V$$

Same answer in both cases.

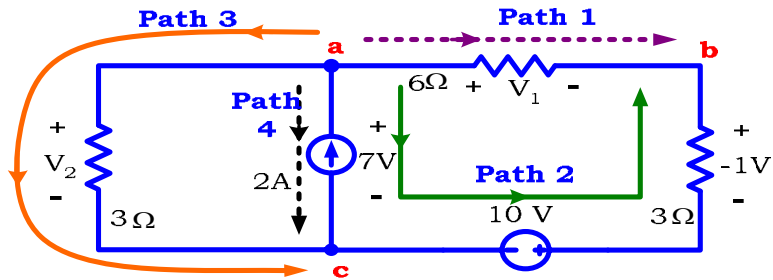
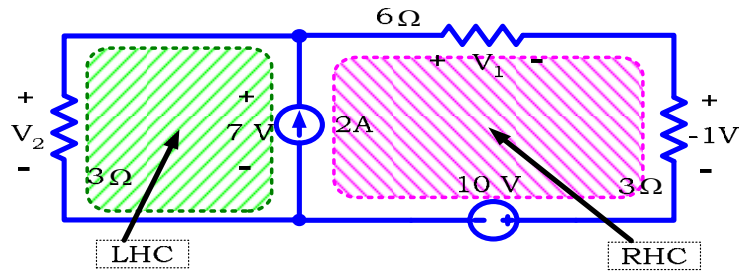
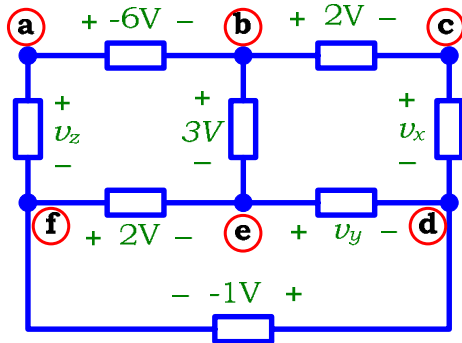


Figure 4

**Example: (KVL)**

Determine voltages  $v_x$ ,  $v_y$ ,  $v_z$  in the circuit of fig....by applying KVL.



**Solution:**

KVL around the loop abcfa

$$-v_z + (-6) + 3 - 2 = 0$$

$$\Rightarrow v_z = -6 - 2 + 3 = -5V \quad (1)$$

KVL around the loop fedef

$$2 + v_y + (-1) = 0$$

$$\Rightarrow v_y = -2 + 1 = -1V \quad (2)$$

KVL around the loop bcdeb

$$-3 + 2 + v_x - v_y = 0 \quad (3)$$

To get  $v_x$  we can substitute  $v_y$  from (2) into (3) to get:

$$v_x = +3 - 2 + v_y = 1 + (-1) = 0$$

$$\Rightarrow v_x = 0V$$

Note: We can also apply KVL around the loop febcdf to get  $v_x$  directly:

$$2 - 3 + 2 + v_x + (-1) = 0$$

$$\Rightarrow v_x = -2 + 3 - 2 + 1 = 0V$$