# KING FAHD UNIVERSITY OF PETROLEUM & MINERALS ELECTRICAL ENGINEERING DEPARTMENT

## **EE 306 – Term 182**

**HW # 6: Induction Motors** 

Due Date: (UT-Classes, April 14th, 2019; MW-Classes, April 15th, 2019)

# **Key Solutions**

#### Problem #1:

A three-phase, four-pole, 30-hp, 220-V, 60-Hz, Y-connected induction motor draws a current of 77-A from the supply line at a power factor of 0.88. At this operating condition, the motor losses are known to be the following:

Stator copper losses = 1033 W; Rotor copper losses = 1299 W

Core loss = 485 W; Mechanical losses (friction & windage) = 540 W

Determine:

- a) the power transferred across the air gap
- b) the internally developed torque in Newton-meters
- c) the slip expressed in percentage
- d) the mechanical power developed in watts
- e) the horsepower output
- f) the motor speed in rpm
- g) the torque at the output shaft
- h) the efficiency of operation

(a) 
$$\sqrt{3} = \frac{15}{100}$$
,  $W_s = \frac{2 \times n_s}{60}$ ,  $n_s = \frac{120 \times 1}{9} = \frac{120 \times 60}{4} = \frac{1800}{1900}$   
 $W_s = \frac{7 \times 11800}{60} = \frac{1895}{60} \text{ rad/scc}$   
 $\sqrt{3} = \frac{128.9}{60} = \frac{1299}{5} = \frac{1299$ 

# Problem # 2:

A 3-phase, Y-connected, 220-V, 10-HP, 60-Hz, 6-pole induction motor has the following parameters in ohms.

$$R_1 = 0.294 \Omega$$
,  $R_2 = 0.144 \Omega$ ,  $X_1 = 0.503 \Omega$ ,  $X_2 = 0.209 \Omega$ ,  $X_m = 13.25 \Omega$ 

The total friction, windage and core losses may be assumed to be constant at 403 W, independent of load. For a slip of 3%, determine:

- (a) the rotor current, developed torque and developed power.
- (b) the maximum developed torque and the corresponding speed.
- (c) the starting torque and starting current.
- (d) How much resistance must be inserted in the rotor circuit to bring the motor speed at maximum torque down to 900 rpm?
- (e) the new starting torque.

$$R_{1} = 3 I_{2}^{2} (1-5) R_{1} = 3 (24.7)^{2} (4.60) \Rightarrow P_{2} = 8.52 kd$$

$$N_{1} = (1-5) N_{2} = (1-0.03) + 1200 \Rightarrow N = 1164 \text{ rpm}$$

$$T_{1} = \frac{P_{2}}{Q_{1}} = \frac{P_{2}}{2 \times N} = \frac{8.52 + 10^{3}}{2 \times (1164)} \Rightarrow T_{2} = 69.9 \text{ N-m}$$

$$T_{2} = \frac{3 V_{1}^{2}}{2 \times Q_{2}^{2}} \cdot \frac{1}{[R_{1} + 1 R_{1}^{2} + (X_{1} + X_{1}^{2})^{2}]} = \frac{3 \cdot (12.7)^{2}}{2 (2 \times 10^{2})^{2}} \cdot \frac{1}{2 \times (12.7)^{2}}$$

$$T_{1} = 151.9 \cdot 6 \cdot \frac{158.5}{13.25} \cdot \frac{1}{190} = \frac{127}{(R_{1} + R_{1}^{2})^{2} + (X_{1} + X_{1}^{2})^{2}} = \frac{3}{(R_{1} + R_{1}^{2})^{2}} \cdot \frac{1}{(R_{1} + R_{1}^{2})^{2} + (X_{1} + X_{1}^{2})^{2}} = \frac{3}{(R_{1} + R_{1}^{2})^{2}} \cdot \frac{1}{(R_{1} + R_{1}^{2})^{2}} = \frac{3}{(R_{1$$

# Problem 3

A 3-phase, 460 V, 60 Hz, 20 kW induction machine draws 25 A at a power factor of 0.9 lagging when connected to a 3-phase, 460 V, 60 Hz power supply. The core loss is 900 W, stator copper loss is 1100 W, rotor copper loss is 550 W, and friction and winding loss is 300 W. Calculate

- (a) The air gap power,  $P_{ag}$ .
- (b) The mechanical power developed, P<sub>mech</sub>.
- (c) The output horse power.
- (d) The efficiency.

## **Solution:**

(a) 
$$P_{ag} = P_{in} - P_{core} - P_{cu,stator} = \sqrt{3} \times 460 \times 25 \times 0.9 - 900 - 1100$$
  
= 17926.2 - 900 - 1100 = 15926.2 W

(b) 
$$P_{\text{mech}} = P_{\text{ag}} - P_{\text{cu,rotor}} = 15926.2 - 550 = 15376.2 \text{ W}$$

(c) 
$$P_{\text{out}} = 15376.2 - 300 = 15076.2 \text{ W}$$
  
 $HP = \frac{15076.2}{746} = 20.2$ 

(d) Eff = 
$$\frac{15076.2}{17926.2} \times 100\% = 84.1\%$$