

Homework 6
EE 306: Electromechanical Devices - Semester 161

Ref: Principles of Electric Machines and Power Electronics, 3rd Edition

Solve the following Exercise Problems from your text book (Page 271):

Problem 5.3

Problem 5.6

Problem 5.7

Problem 5.9

Problem 5.12

Solution Problem 5.3

$$(a) \quad 0.03 = \frac{1200 - n}{1200}, \quad n_s = \frac{120 \times 60}{6} = 1200 \text{ rpm.}$$

$n = 1164 \text{ rpm} \rightarrow$ direction same as the rotating field.

$$(b) \quad f_2 = 0.03 \times 60 = 1.8 \text{ Hz}$$

$$(c) \quad 1200 \text{ rpm}$$

$$(d) \quad 1200 \text{ rpm}$$

$$(e) \quad (i) \quad n_M = 0.03 \times 1200 = 36 \text{ rpm} \rightarrow \text{direction same as the rotor motion.}$$

$$(ii) \quad 1200 \text{ rpm}$$

$$(iii) \quad 0 \text{ rpm}$$

Solution Problem 5.6

$$(a)(i) \quad n_s = \frac{120 \times 60}{6} = 1200 \text{ rpm}$$

$$s = \frac{1200 - 1140}{1200} = 0.05$$

$$(ii) \quad E_{2s} = s E_2 = s \frac{E_1}{a}$$

$$a = \frac{1}{0.5} = 2.0$$

$$E_{2s} = 0.05 \times \frac{1}{2.0} \times \frac{208}{\sqrt{3}} = 3 \text{ V}$$

$$f_2 = 0.05 \times 60 = 3 \text{ Hz}$$

$$(iii) \text{ - slip rpm } n_2 = s n_s = 0.05 \times 1200 = 60 \text{ rpm}$$

- with respect to stator \rightarrow 1200 rpm.

(b) Inverted induction motor

(i) opposite

$$(ii) \quad E_{1s} = s E_1 = s a E_2 = 0$$

$$s = \frac{1200 - 1164}{1200} = 0.03$$

$$E_{1s} = 0.03 \times 2 \times \frac{208}{\sqrt{3}} = 7.2 \text{ V}$$

$$f_1 = 0.03 \times 60 = 1.8 \text{ Hz}$$

Solution Problem 5.7

$$(a) \quad P_{ag} = P_{in} - P_{core} - P_{cu, \text{stator}} = \sqrt{3} \times 460 \times 25 \times 0.9 - 900 - 1100 \\ = 17926.2 - 900 - 1100 = 15926.2 \text{ W}$$

$$(b) \quad P_{mech} = P_{ag} - P_{cu, \text{rotor}} = 15926.2 - 550 = 15376.2 \text{ W}$$

$$(c) \quad P_{out} = 15376.2 - 300 = 15076.2 \text{ W}$$

$$\text{HP} = \frac{15076.2}{746} = 20.2$$

$$(d) \quad \text{Eff} = \frac{15076.2}{17926.2} \times 100\% = 84.1\%$$

Solution Problem 5.9

- (a) $n_s = \frac{120 \times 60}{2} = 3600 \text{ rpm}$
 $s = \frac{3600 - 3546}{3600} = 0.015 \text{ or } 1.5\%$
- (b) $T_{\text{dev}} = \frac{20 \times 10^3}{3546/60 \times 2\pi} = 53.86 \text{ N} \cdot \text{m}$
 $n = 1800 \times (1 - 0.0345) = 1737.9 \text{ rpm}$
- (c) If torque is doubled, slip is doubled,
 $s = 0.03$
 $n = 3600 \times (1 - 0.03) = 3492 \text{ rpm}$
- (d) $T = 2 \times 53.86 = 107.72 \text{ N} \cdot \text{m}$
 $\omega = 3492 \times 2\pi$
 $P = T \cdot \omega = 107.72 \times \frac{3492}{60} \times 2\pi \times 10^{-3} \text{ kW} = 39.39 \text{ kW}$

Solution Problem 5.12

$$P_{\text{out}} = 2.5 \times 746 = 1865 \text{ W}$$
$$n_s = \frac{120 \times 60}{4} = 1800 \text{ rpm}$$
$$s = \frac{1800 - 1700}{1800} = 0.0555$$
$$P_{\text{mech}} = 1865 + 150 = 2015 \text{ W}$$
$$P_{\text{ag}} = \frac{2015}{1 - 0.0555} = \frac{2015}{0.9445} = 2133.4 \text{ W}$$
$$P_{\text{cu2}} = 0.0555 \times 2133.4 = 118.4 \text{ W}$$
$$3 \times I_2^2 R_2 = 118.4 \text{ W} \rightarrow I_2 = \sqrt{\frac{118.4}{3 \times 0.025}} = 39.73 \text{ A}$$

~~End of homework problems~~