

KING FAHD UNIVERSITY OF PETROLEUM & MINERALS

ELECTRICAL ENGINEERING DEPARTMENT

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EE 463

MAJOR EXAM # 1

March 29, 2006

11:45am - 1:00 pm

Key Solution

Section:

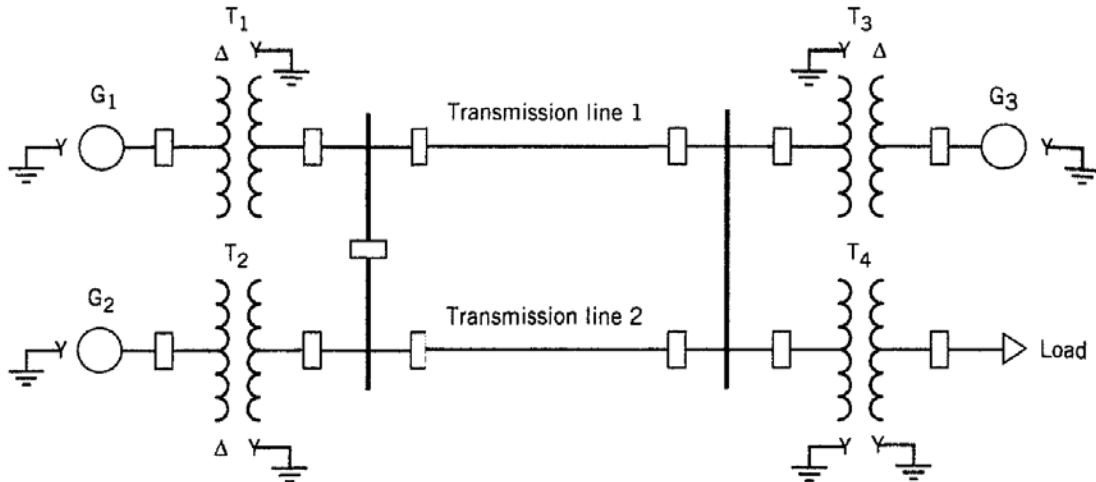
Student Name:

Student I.D.#

Serial #:

| | |
|---------------------|--|
| Question # 1 | |
| Question # 2 | |
| Question # 3 | |
| Total | |

Q. 1) The one-line diagram of a 2-bus power system is shown below.



The reactance of each transmission line is $X = 20 \text{ Ohm}$. The generators and transformers are rated as follows:

- G1: 20 MVA, 12 kV, $X = 1.20$ per unit
- G2: 60 MVA, 13.8 kV, $X = 1.40$ per unit
- G3: 50 MVA, 13.2 kV, $X = 1.40$ per unit
- T1: 25 MVA, 12/69 kV, $X = 0.08$ per unit
- T2: 75 MVA, 13.8/69 kV, $X = 0.16$ per unit
- T3: 60 MVA, 13.2/69 kV, $X = 0.14$ per unit
- T4: 75 MVA, 13.8/69 kV, $X = 0.16$ per unit

- a) Choose a power base of 100 MVA and a voltage base of 12 kV in the circuit of generator G1, and assume that the circuit breaker between transformer 4 and the load is open. Draw the reactance diagram showing all the values in per units according to the new selected base values.
- b) Form the bus admittance matrix Y_{bus} .

(50 Marks)

Solution:

a)

$$X_{G1} = 1.2 (100 / 20) = 6.0 \text{ p.u.}$$

$$X_{G2} = 1.4 (100 / 60) = 2.333 \text{ p.u.}$$

$$X_{G3} = 1.4 (100 / 50) = 2.8 \text{ p.u.}$$

$$X_{T1} = 0.08 (100 / 25) = 0.32 \text{ p.u.}$$

$$X_{T2} = 0.16 (100 / 75) = 0.213 \text{ p.u.}$$

$$X_{T3} = 0.14 (100 / 60) = 0.233 \text{ p.u.}$$

$$X_{T4} = 0.16 (100 / 75) = 0.213 \text{ p.u.}$$

$$X_{TL1} = X_{TL2} = 20 / (69^2 / 100) = 0.42 \text{ p.u.}$$

a)

$$X_{G1} = 1.2 \left(\frac{100}{20} \right) = 6$$

$$X_{G2} = 1.4 \left(\frac{100}{60} \right) = 2.333$$

$$X_{G3} = 1.4 \left(\frac{100}{50} \right) = 2.8$$

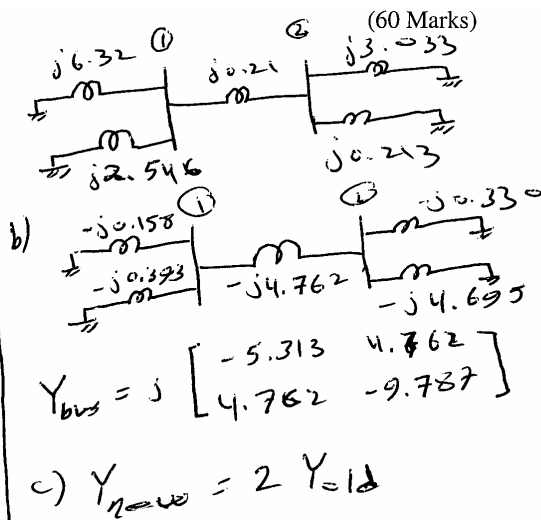
$$X_{T1} = 0.08 \left(\frac{100}{25} \right) = 0.32$$

$$X_{T2} = 0.16 \left(\frac{100}{75} \right) = 0.213$$

$$X_{T3} = 0.14 \left(\frac{100}{60} \right) = 0.233$$

$$X_{T4} = 0.16 \left(\frac{100}{75} \right) = 0.213$$

$$X_{TL1} = X_{TL2} = \frac{20}{(69)^2 / 100} = 0.42$$



b) $Y_{bus} = j \begin{bmatrix} -5.313 & 4.762 \\ 4.762 & -9.787 \end{bmatrix}$

Q.2) Write down the equations of the 7th iteration, using Gauss-Seidel Iterative method with acceleration factor, of a nine-bus system for the following busses:

- a) bus-3 (PQ-bus) connected to bus-1 (PQ-bus), bus-2 (slack-bus) and bus-6 (PV-bus).
 b) bus-6 (PV-bus) connected to bus-2 (slack-bus), bus-3 (PQ-bus), bus-4 (PV-bus), and bus-9 (PQ-bus).

(Notice: define the voltage of a calculated PV-bus as V_{corr} , and an accelerated voltage as V_{acc})
 (30 Marks)

Solution:

$$a) \quad V_3^7 = \frac{1}{Y_{33}} \left[\frac{P_3 - jQ_3}{V_{3acc}^{6*}} - (Y_{31}V_{1acc}^7 + Y_{32}V_2 + Y_{36}V_{6corr}^6) \right]$$

$$\Delta V_3^7 = V_3^7 - V_{3acc}^6$$

$$V_{3acc}^7 = V_{3acc}^6 + \alpha \Delta V_3^7$$

$$b) \quad V_6^7 = \frac{1}{Y_{66}} \left[\frac{P_6 - jQ_{6cal}}{V_{6corr}^{6*}} - (Y_{62}V_2 + Y_{63}V_{3acc}^7 + Y_{64}V_{4corr}^7 + Y_{69}V_{9acc}^6) \right]$$

where

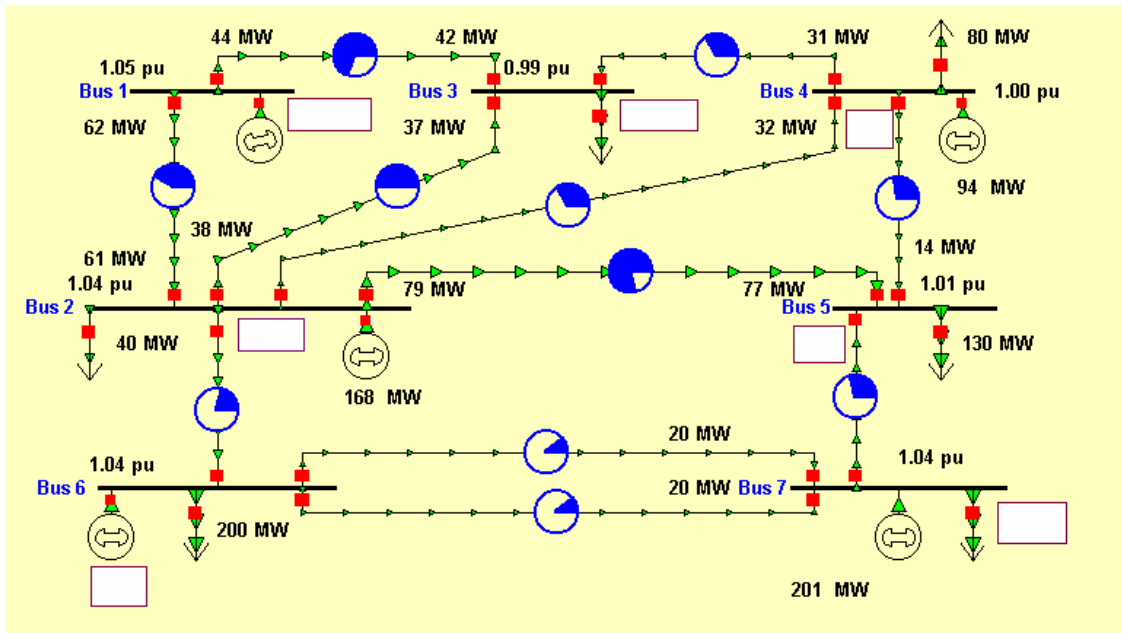
$$Q_{6cal} = -\text{Im} \left[V_{6corr}^{6*} (Y_{62}V_2 + Y_{63}V_{3acc}^7 + Y_{64}V_{4corr}^7 + Y_{66}V_{6corr}^6 + Y_{69}V_{9acc}^6) \right]$$

$$\Delta V_6^7 = V_6^7 - V_{6corr}^6$$

$$V_{6acc}^7 = V_{6corr}^6 + \alpha \Delta V_6^7$$

$$V_{6corr}^7 = |V_6^7| \angle \theta_{6acc}^7$$

Q.3) The power flow of a 7-bus system is shown below



Assuming the following line losses :

| Line | Real Power Loss (MW) |
|------|----------------------|
| 2-4 | 0 |
| 2-6 | 0 |
| 3-4 | 0 |
| 5-7 | 1 |
| 6-7 | 0 |
| 6-7 | 0 |

Find the real power in MW at the locations indicated with the empty rectangular boxes

(20 Marks)

Solution:

| | | | |
|-----|---|-----|----|
| G1 | = | 106 | MW |
| G6 | = | 200 | MW |
| L3 | = | 110 | MW |
| L7 | = | 201 | MW |
| 2-6 | = | 40 | MW |
| 4-5 | = | 15 | MW |
| 7-5 | = | 39 | MW |