

8-5

$$a) \quad n_s = \frac{n}{1-s} = \frac{855}{(1-0.05)} = 900 \text{ rpm}$$

$$b) \quad p = \frac{120f}{n_s} = \frac{(120)(60)}{900} = 8 \text{ poles}$$

$$c) \quad f_r = sf = (0.05)(60) = 3 \text{ Hz}$$

8-11 Refer to Fig. 8-8

$$a) \quad n_s = \frac{120f}{p} = \frac{(120)(60)}{4} = 1800 \text{ rpm}$$

$$n = (1-s)n_s = (1-0.05)(1800) = 1710 \text{ rpm}$$

$$b) \quad V_1 = \frac{220}{\sqrt{3}} \angle 0^\circ = 127 \angle 0^\circ$$

$$I_2 = \frac{V_1}{(R_1 + \frac{R_2}{s}) + j(X_1 + X_2)} = \frac{127 \angle 0^\circ}{(0.3 + \frac{0.2}{0.05}) + j(0.5 + 0.5)} = 28.77 \angle -13.1^\circ \text{ A}$$

$$I_m = \frac{V_1}{jX_m} = \frac{127 \angle 0^\circ}{j15} = 8.47 \angle -90^\circ \text{ A}$$

$$I_1 = I_2 + I_m = 28.77 \angle -13.1^\circ + 8.47 \angle -90^\circ = 31.78 \angle -28.1^\circ \text{ A}$$

$$c) \quad PF_1 = \cos \theta = \cos 28.1^\circ = 0.882 \text{ lagging}$$

$$d) \quad P_{in} = 3V_1 I_1 \cos \theta = (3)(127)(31.78) \cos 28.1^\circ = 10,680 \text{ W}$$

$$P_{ag} = 3 I_2^2 \frac{R_2}{s} = (3)(28.77)^2 \left(\frac{0.2}{0.05} \right) = 9932.6 \text{ W}$$

$$P_{dev} = (1-s) P_{ag} = (1-0.05)(9932.6) = 9435.9 \text{ W}$$

$$P_{out} = P_{dev} - P_{rot} = 9435.9 - 500 = 8935.9 \text{ W}$$

$$\omega_m = \frac{2\pi n}{60} = \frac{2\pi(1710)}{60} = 179.1 \text{ rad/s}$$

$$T_{out} = T_{shaft} = \frac{P_{out}}{\omega_m} = \frac{8935.9}{179.1} = 49.9 \text{ N-m}$$

$$e) \quad \eta = \frac{P_{out}}{P_{in}} = \frac{8935.9}{10,680} \times 100\% = 83.7\%$$

8-17

$$R_1 = \frac{1}{2} \left(\frac{V_{DC}}{I_{DC}} \right) = \frac{1}{2} \left(\frac{8}{50} \right) = 0.08 \, \Omega$$

$$R_{nl} = \frac{P_{nl}}{3 I_{nl}^2} = \frac{3800}{(3)(38)^2} = 0.877 \, \Omega$$

$$Z_{nl} = \frac{V_{nl}}{\sqrt{3} I_{nl}} = \frac{440}{\sqrt{3} (38)} = 6.685 \, \Omega$$

$$X_{nl} = \sqrt{Z_{nl}^2 - R_{nl}^2} = \sqrt{(6.685)^2 - (0.877)^2} = 6.627 \, \Omega$$

$$R_{b1} = \frac{P_{b1}}{3 I_{b1}^2} = \frac{4800}{(3)(110)^2} = 0.132 \, \Omega$$

$$Z_{b1} = \frac{V_{b1}}{\sqrt{3} I_{b1}} = \frac{80}{\sqrt{3} (110)} = 0.42 \, \Omega$$

$$X_{b1, test} = \sqrt{Z_{b1}^2 - R_{b1}^2} = \sqrt{(0.42)^2 - (0.132)^2} = 0.40 \, \Omega$$

$$X_{b1} = \left(\frac{f_{rated}}{f_{test}} \right) X_{b1, test} = \left(\frac{60}{15} \right) (0.40) = 1.60 \, \Omega$$

$$X_1 = X_2 = \frac{1}{2} X_{b1} = \frac{1}{2} (1.60) = 0.80 \, \Omega$$

$$X_m = X_{nl} - X_1 = 6.627 - 0.80 = 5.827 \, \Omega$$

$$R_2 = R_{b1} - R_1 = 0.132 - 0.08 = 0.052 \, \Omega$$

8-23 Refer to Fig. 8-8 : $V_1 = \frac{440}{\sqrt{3}} \angle 0^\circ = 254 \angle 0^\circ \, V$

$$\textcircled{a} \, I_2 = \frac{V_1}{R_1 + \frac{R_2}{s} + j(X_1 + X_2)} = \frac{254 \angle 0^\circ}{0.12 + \frac{0.10}{0.035} + j(0.25 + 0.2)} = 84.36 \angle -8.6^\circ \, A$$

$$I_m = \frac{V_1}{jX_m} = \frac{254 \angle 0^\circ}{j15} = 16.93 \angle -90^\circ$$

$$I_1 = I_2 + I_m = 84.36 \angle -8.6^\circ + 16.93 \angle -90^\circ = 88.5 \angle -19.5^\circ \, A$$

$$PF_1 = \cos 19.5^\circ = 0.943 \text{ lagging}$$

$$\textcircled{b} \, P_{ag} = 3 I_2^2 \frac{R_2}{s} = (3)(84.36)^2 \left(\frac{0.10}{0.035} \right) = 61,000 \, W$$

$$\textcircled{c} \, P_{conv} = P_{dev} = (1-s) P_{ag} = (1-0.035)(61,000) = 58,865 \, W$$

$$\textcircled{a} \quad P_{out} = 20 \text{ kW}$$

$$P_{dev} = P_{out} + P_{rotational} = 20 + 1.5 = 21.5 \text{ kW}$$

$$P_{ag} = \frac{P_{dev}}{1-s} = \frac{21.5}{1-0.045} = 22.5 \text{ kW}$$

$$\textcircled{b} \quad n_s = \frac{120f}{p} = \frac{(120)(60)}{6} = 1200 \text{ rpm}$$

$$n = (1-s)n_s = (1-0.045)(1200) = 1146 \text{ rpm}$$

$$\omega_m = \frac{2\pi n}{60} = \frac{2\pi(1146)}{60} = 120 \text{ rad/s}$$

$$T_{out} = \frac{P_{out}}{\omega_m} = \frac{20,000}{120} = 166.7 \text{ N-m}$$

$$\textcircled{c} \quad T_{dev} = \frac{P_{dev}}{\omega_m} = \frac{21,500}{120} = 179.2 \text{ N-m}$$