

KING FAHD UNIVERSITY OF PETROLEUM AND MINERALS

ELECTRICAL ENGINEERING DEPARTMENT

SECOND SEMESTER 2006/2007

EE 340 (01) MAJOR EXAM I

LOCATION: 7-122

TIME: 6:30 -8:00 P.M.

DATE: SUNDAY 1-APRIL-2007

Student's Name:.....

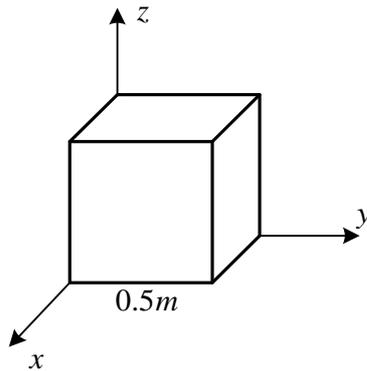
Student's I.D. Number: .....

|                  | <b>Maximum Score</b> | <b>Score</b> |
|------------------|----------------------|--------------|
| <b>Problem 1</b> | <b>25</b>            |              |
| <b>Problem 2</b> | <b>25</b>            |              |
| <b>Problem 3</b> | <b>25</b>            |              |
| <b>Problem 4</b> | <b>25</b>            |              |
| <b>Total</b>     | <b>100</b>           |              |

Problem 1 [25 points]

The electrostatic potential  $V = 10e^{-(x+2y+3z)}$  [V] exists in free space.

- Calculate the volume charge density in  $C/m^3$  at point  $P$  whose rectangular coordinates are  $(1,0,0)$ .
- Calculate the maximum electrostatic energy density in Joule per cubic meter.
- Calculate the total stored *electrostatic energy* inside the cubic volume  $0.50[m]$  on the side (see figure).

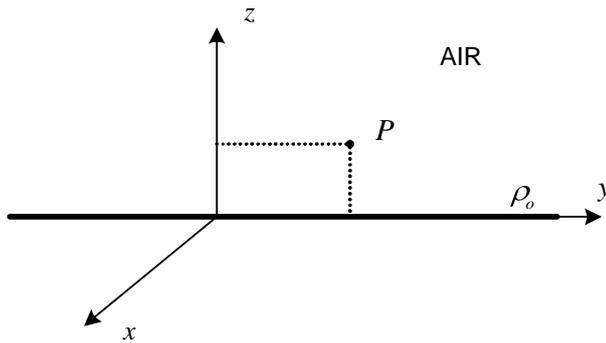


Problem 2 [25 points]

An infinitely long line of charge of uniform density  $\rho_L = \rho_o$  is placed on the entire  $y$  axis as shown in the diagram. The surrounding medium is air. Consider the point  $P$  which is situated in the  $y-z$  plane [i.e.  $P = P(0, y, z)$ ].

a) Develop an expression for the electric field intensity vector  $\vec{E}$  at point  $P$ .

b) Now consider the two points  $A$  and  $B$  with rectangular coordinates  $(0, 2, 4)$  and  $(0, 6, 9)$ , respectively. Calculate the resulting potential difference  $V_{AB}$  for  $\rho_o = -3[nC/m]$ .

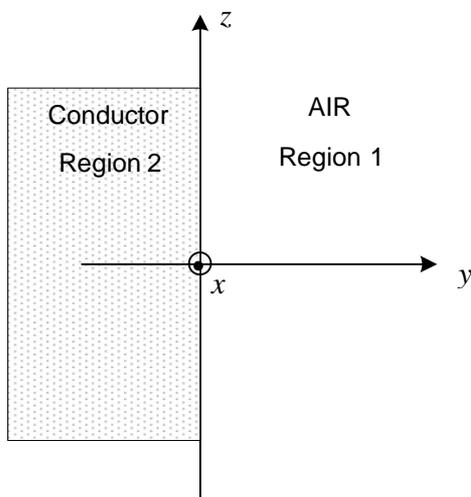


Problem 3 [25 points]

The plane boundary  $y = 0$  separates two the semi infinite regions, region 1 ( $y > 0$ ) and region 2 ( $y < 0$ ). Region 1 is an air region and region 2 is a conductor.

Consider the electrostatic field:  $\vec{E}_1 = -2xy\vec{a}_x - x^2\vec{a}_y + y\vec{a}_z$  [V/m], which exists in air.

- Find the electrostatic field on the conductor/air boundary.
- Find the surface charge density  $\rho_s$  on the conductor/air boundary.
- Calculate the total charge  $Q$  residing on the square area ( $0 \leq x \leq 1$ ,  $y = 0$ ,  $0 \leq z \leq 1$ ).



Problem 4 [25 points]

A spherical shell of inner radius  $a$  and outer radius  $b$  exists in free space. This shell contains a uniform volume charge density  $\rho_v = \rho_o$ . Derive an expression for the electric flux density vector  $\vec{D}$  in the regions:

- a)  $r < a$ .
- b)  $b > r > a$ .
- c)  $r > b$ .

