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## Grid Routing

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## INTRODUCTION

- The phase following cell placement.
- Routing is accomplished using computer programs (routers).
- Consists of precisely defining paths that carry electrical signals run.
- Takes up almost $30 \%$ of design time and a large percentage of layout area.
- Routing algorithms were first applied to design of PCBs.
- The main application of automatic routers has been in the automated design of VLSI circuits.


## Maze Routers

- Consider the layout as a maze.
- Finding a path is similar to finding a path in the maze.
- The layout floor is assumed to be made up of a rectangular array of grid cells.
- Functional cells fill up some slots in the grid and constitute the obstacles of the maze.
- The most popular algorithm is the Lee algorithm.
- Running time of maze algorithms is large and memory requirement is high.
- Maze routers based on the Lee algorithm connect a pair of points at a time.
- Multi-pin nets can be connected in a spanningtree like fashion.


## Problem Definition

## Given:

- a set of cells with ports (inputs, outputs, clock, power and ground pins) on the boundaries,
- a set of signal nets,
- locations of cells on the layout floor, and
- geometrical constraints and number of routing layers.

Goal: find suitable paths on the available layout space, that is those paths that minimize the given objective functions, subject to constraints.
Constraints may be:

- imposed by the designer,
- the implementation process, or
- layout strategy and design style.

Examples of constraints are:

- minimum separation between adjacent wires,
- minimum width of routing wires,
- number of available routing layers,
- timing constraints, etc.

Examples of objective functions include:

- reduction of wire length, and
- avoidance of timing problems.


## Routing Material

- The connections are made by first uniformly depositing metal on a carrier surface.
- Then unwanted metal is etched away.
- In PCBs this surface is usually fiberglass. While in VLSI it is silicon.
- In VLSI design, polysilicon is also used to carry signals.
- In 2-layer VLSI routing, the 2 layers are separated by an oxide insulating layer.
- Holes in this insulating layer called contact-cuts (or vias) connect conductors between two layers.
- Certain VLSI technologies allow three layers for routing. (2 layers in metal and the 3rd layer in polysilicon)


## Illustration of general routing



## Cost functions and Constraints

- Reduction of wiring area.
- Improvement in performance.
- Improve yield (by reducing cuts).
- Two possible paths connecting a pair of points are shown below. (a) The shortest path. (b) A longer path with more bends.

(a)

(b)


## Geometrical Constraints

- Minimal geometries must be maintained, (minimum width and spacing dictated by the technological process).
- Must be able to consider all geometrical constraints abolishing the need for DRC.
- For routing purposes, only those design rules must be considered which define geometries of wires and contact holes.
- Commonly, this is achieved by using a proper equidistant grid.
- Wires are represented by lines and restricted to grid line positions.
- Wire widths and separation between wires is constant for all nets and design rules are avoided.


## Illustration of grid cell size



## Maze Routing Algorithms

- The entire routing surface is represented as a rectangular array of grid cells.
- All ports, wires, and edges of bounding boxes that enclose the cells are aligned on the grid.
- Segments on which wires run are also aligned with the grid lines.
- The size of grid cells is defined such that wires belonging to other nets can be routed without violating the width/spacing rules of wires.
- Two points are connected by finding a sequence of adjacent cells from one point to the other.
- Maze routers connect a single pair of points at a time.


## Lee Algorithm

- Most widely known maze routing method for finding a path in a maze.
- An excellent characteristic is that if a path exists then it is surely found.
- In addition it is guaranteed to be the shortest available one.
- The algorithm can be divided into three phases.
- The first phase consists of labeling the grid, and is called the filling or wave propagation phase.
- It is analogous to dropping a pebble in a still pond and causing waves to ripple outward.
- The second phase of the algorithm is called the retrace phase.
- The final phase is called label clearance. In this phase all labeled cells except those used for the path just found are cleared for subsequent interconnections.


## Filling in Lee Algorithm


(a)

(b)

- The filling phase begins by entering a ' 1 ' in all empty cells adjacent to the source cell $S$.
- Next, $2 s$ are entered in all empty cells adjacent to those containing 1s. Then, 3 s are entered adjacent to $2 s$ and so on.
- This process continues and is terminated when one of the three conditions occurs.


## Filling \& Retrace in Lee Algorithm

Filling continues until:
a. the grid cell $T$ is reached; or
b. $T$ is not reached and at step $i$ there are no empty grid cells adjacent to cells labeled $i-1$; or
c. $T$ is not reached and $i$ equals $M$, where $M$ is the upper bound on a path length.

The Retrace procedure is the reverse of filling. The actual shortest path is found as follows:

- If grid cell $T$ was reached in step $i$, then there exists at least one grid cell adjacent to it which contains $i-1$.
- Likewise, a grid cell containing $i-2$ will be adjacent to one containing label $i-1$ and so on.
- By tracing the numbered cells in descending order from $T$ to $S$, the desired shortest path is found.
- The cells of the retraced path for the filled grid of Figure (a) are shaded in Figure (b).
- Once the desired path is found, the cells used for the route connecting $S$ and $T$ are regarded as obstacles for subsequent interconnections.


## Time/Space Complexity of Lee Algorithm

- The processing time for filling is proportional to $L^{2}$, ( $L$ is the length of the path)
- The processing time for retrace is proportional to $L$
- Therefore, the algorithm has a time complexity of $O\left(L^{2}\right)$ for each path
- In addition, for an $N \times N$ grid plane, the algorithm requires $O\left(N^{2}\right)$ memory
- Also, some amount of storage is required to store positions of cells on the wavefront
- The worst case running time is also of $\mathrm{O}\left(N^{2}\right)$
- Extensions to reduce running time and storage have been proposed


# Coding Schemes to Reduce Memory 

- A non-trivial storage problem is that a unit of memory space is needed for every grid cell.
- In a filled grid we observe that for each cell labeled $k$, all adjacent cells are labeled either $k-1$ or $k+1$.
- Therefore, during retrace, it is sufficient if we can distinguish the predecessor cells from the successor cells.
- Labeling schemes based on this idea are widely used. Two are listed below.


## Coding Schemes to Reduce Memory

- In the first scheme
- Labeling sequence is $1,2,3,1,2,3 \ldots$
- Only three bits per memory cell are required since a grid cell may be in one of the 5 states.
- The second scheme proposed by Akers
- Labeling sequence is $1,1,2,2,1,1,2,2 \ldots$.
- This scheme is most economical, since each cell will be in one of the four states: empty, blocked, labeled with 1, or labeled with 2.
- Independent of the grid size, two bits per memory cell are sufficient.


## Filling Sequences That Reduce Memory Requirement

(a) Sequence $1,2,3,1,2,3 \ldots$ (b) Sequence 1,1 , 2,2, 1,1, 2,2....

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  | 2 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 2 | 1 | 2 |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 2 | 1 | 3 | 1 | 2 |  |  |  |  |
|  |  |  |  |  |  |  |  | 1 | 3 | 2 | 3 | 1 | 2 |  |  |  |
|  |  |  |  |  |  | $\mathbf{T}$ | 1 | 3 | 2 | 1 | 2 | 3 | 1 | 2 |  |  |
|  |  |  |  |  | 2 | 1 | 3 | 2 | 1 | 3 | 1 | 2 | 3 | 1 | 2 |  |
|  |  |  |  | 2 | 1 | 3 | 2 | 1 | 3 | 2 | 3 | 1 | 2 | 3 | 1 | 2 |
|  |  |  | 2 | 1 | 3 | 2 | 1 | 3 | 2 | 1 |  |  | 3 | 1 | 2 |  |
|  |  |  | 3 | 2 | 1 | 3 | 2 | 1 | $\mathbf{S}$ |  |  |  | 2 |  |  |  |
|  |  |  |  |  | 3 | 2 | 1 | 3 | 2 | 1 |  |  |  |  |  |  |
|  |  |  |  | 2 | 1 | 3 | 2 | 1 | 3 |  |  |  |  |  |  |  |
|  |  |  |  |  | 2 | 1 | 3 | 2 | 1 | 2 |  |  |  |  |  |  |
|  |  |  |  |  | 2 | 1 | 3 | 2 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 2 | 1 | 3 | 1 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 2 | 1 | 2 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 2 |  |  |  |  |  |  |  |

(a)

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 2 |  | 2 | 2 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 2 | 2 |  | 1 | 2 | 2 |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 2 | 1 |  | 1 | 1 | 2 |  | 2 |  |  |  |
|  |  |  |  |  | T | 2 |  | 1 | 1 |  | 2 | 1 | 1 |  | 2 | 2 |  |  |
|  |  |  |  | 2 | 2 | 1 |  | 1 | 2 |  | 2 | 2 | 1 | 1 | 1 | 2 | 2 |  |
|  |  |  | 2 | 2 | 1 | 1 |  | 2 | 2 |  | 1 | 2 | 2 |  | 1 | 1 | 2 | 2 |
|  |  | 2 | 2 | 1 | 1 | 2 |  | 2 | 1 |  | 1 |  |  |  | 1 | 2 | 2 |  |
|  |  |  | 1 | 1 | 2 | 2 |  | 1 | 1 |  | S |  |  |  |  | 2 |  |  |
|  |  |  |  | 1 | 1 | 2 |  | 2 | 1 |  | 1 |  |  |  |  |  |  |  |
|  |  |  | 2 | 2 | 1 | 1 |  | 2 | 2 |  |  |  |  |  |  |  |  |  |
|  |  |  |  | 2 | 2 | 1 |  | 1 | 2 |  | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  | 2 | 2 |  | 1 | 1 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | 2 |  | 2 | 1 |  | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 2 | 2 |  | 2 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 2 |  |  |  |  |  |  |  |  |  |

(b)

## Reducing Running Time

- Running time is proportional to the number of cells searched in the filling phase.
- The following speed-up techniques are used.
(a) Starting point selection.
(b) Double fan-out.
(c) Framing.

(a)

(b)

(c)


## Connecting Multi-point Nets

- Lee algorithm as seen above connects two pins
- A multi-pin net consists of three or more pins to be connected.
- The optimal connection of these pins resulting in the least wirelength is termed as the Steiner tree problem.
- This problem has been proven to be NP-hard
- A sub-optimal solution to connect a multipoint net can be obtained using Lee algorithm


## Example of Routing a Multipoint Net

(a) Five points of a net. (b) Interconnection tree found by repeated application of modified Lee algorithm. (c) A shorter interconnection found by deleting an edge and re-routing.

(a)

(b)

(c)

## Finding More Desirable Paths

- Often practical situations require a more desirable path, not necessarily the shortest
- An example is of finding a path that will cause least amount of difficulty for subsequent paths
- The filling phase of the Lee Algorithm can be modified to accommodate such constraints.
- The requirement of any filling phase is that the desired path be unambiguously traced back.
- Akers observed that a path running along obstructions would leave more room for subsequent ones
- Suppose that a net $x$ has been routed as shown below. The standard Lee Algorithm will result in the shortest path $z$. while the longer path $y$ could be more preferable.



## Finding More Desirable Paths

- If the objective is to accomplish the desired path such as $y$, then the required path selection can be accomplished by preparing a weighted array as shown in Figure below.
- The desired path may be generated by routing a net so as to minimize the total weight of used cells.
- For path $y$ this weight is 13 , and for path $z$ it is 15 .
- The wave propagation phase in Lee Algorithm is modified to minimize the total weighted sum of grid points.
- The modified procedure is shown in the following slide with an example.

| 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  | 2 |
|  |  | 1 | 2 | 2 | 2 | 2 | 2 | 1 | 3 |
|  |  | 1 | 3 | 3 | 3 | 3 | 2 | 5 | 2 |
| 2 | 1 | T | 2 | 3 | 3 | 3 | 3 | 2 | 3 |
| 3 | 3 | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |

## Example of Finding Desirable Paths


(c)

(e)

(g)

(b)

(d)

(f)

(h)

## Further Speed Improvements

- The filling phase of Lee Algorithm is similar to the breadth first search
- It can also be thought of as construction of a tree with each node having at most 4 children.
- the running time for a particular instance of source-target pairs is proportional to the number of cells being searched until the target is reached.
- One idea behind speed-up techniques is to advance the wavefront with a higher priority towards the target direction.
- Two techniques are presented in the following slides; Hadlock's algorithm and Soukup's algorithm.


## Detour Numbers

- Hadlock's algorithm is a shortest path algorithm with a new method for cell labeling called detour numbers
- It is a goal directed search method.
- The detour number $d(P)$ of a path $P$ connecting two cells $S$ and $T$ is defined as the number of grid cells directed away from its target $T$.
- If $M D(S, T)$ is the Manhattan distance between $S$ and $T$, then it can be proved that the length $l(P)$ of a path $P$ is given by

$$
\begin{equation*}
l(P)=M D(S, T)+2 \times d(P) . \tag{1}
\end{equation*}
$$

- An example of path length and detour numbers is shown in Figure below.

$\mathrm{O}=$ Directed away
from the target

$$
\begin{aligned}
& \mathrm{d}(\mathrm{P})=4 \\
& \mathrm{MD}(\mathrm{~S}, \mathrm{~T})=7 \\
& l(\mathrm{P})=7+2^{*} 4=15
\end{aligned}
$$

## Hadlock's Algorithm

- Figure in previous slide illustrates how path length is represented by the detour number.
- Note that in Eqn (1) $M D(S, T)$ is fixed, independent of the path connecting $S$ and $T$.
- Based on this idea, the filling phase of the Lee Algorithm is modified as follows:
a. Instead of filling a cell with a number equal to the distance from the source, the detour numbers with respect to a specified target are entered.
b. Cells with smaller detour numbers are expanded with higher priority.
- Figure (a) shows the filling of a grid. Observe that for any cell filled with $i$, if the adjacent cell is towards the target, then it is filled with the same number, and if it is away from the target then it is filled with $i+1$.
- Path retracing is slightly different from the standard Lee algorithm
- The number of grid units filled is considerably smaller than in Lee algorithm.
- Therefore speed improvement is remarkable.


## Filling in Hadlock's and Soukup's Algorithms


(a)

(b)

## Soukup's Algorithm

- The previous algorithm performed filling in a breadth first manner.
- Soukup suggested adding depth to the search.
- In Soukup's algorithm a line segment from the source is initially extended toward target.
- The cells on this line segment are searched first. The line segment is extended without changing direction unless it is necessary.
- When the line hits an obstacle, Lee algorithm is applied to search around the obstacle.
- During the search, once a cell in the direction of the target is found, another line segment starting from there is extended toward target.
- The darkened circles in the figure indicate the cells directed towards the target.
- Soukup's algorithm finds a path if one exists, but does not guarantee that it is the shortest.
- Its disadvantage is that it generates sub-optimal paths (both in terms of length and \# of bends).
- However, it is extremely fast, especially when the routing space is not congested.
- It is claimed that it is $10-50$ times faster than the Lee Algorithm on typical two-layer routing problems.


## Line Search Algorithms

- Line search algorithms overcome the drawback of Lee algorithm.
- The idea is to draw lines passing through $S$ (source) and $T$ (target). The two lines when intersect give a Manhattan path between $S$ and $T$.
- Line search algorithms perform a depth-first search.
- Because of their depth-first nature, line search algorithms do not guarantee finding the shortest path, and may need several backtrackings.
- Produce completion rates similar to Lee algorithm, with the difference that both memory requirements and execution times are considerably reduced.
- This is because the entire routing space is not stored as a matrix.
- The routing space and paths are represented by a set of line segments.
- Line search algorithms were first proposed by Mikami-Tabuchi and Hightower.


## Mikami-Tabuchi's Algorithm

- Let $S$ and $T$ be a pair of terminals of a net located on some intersection of an imaginary grid.
- The first step is to generate four lines (two horizontal and two vertical) passing through $S$ and $T$.
- These lines are extended until they hit obstructions (a placed cell for example) or the boundary of the layout.
- If a line generated from $S$ intersects a line generated from $T$ then a connecting path without any bend or with one bend has been found.
- If the four generated lines do not intersect, then they are identified as trial lines of level zero and stored in temporary storage.
- Then at each iteration $i$ the following operations are done.
(1). Trial lines of level $i$ are picked and along each of its grid points (base-points) and traced.
Starting from these base-points new trial lines are generated perpendicular to trial line $i$.
Let the generated line segments be identified as trial lines of level $i+1$.
(2). If trial line of level $(i+1)$ intersects a trial line (of any level) originated from the other terminal point, then the required path is found by backtracking from the point of intersection to both points $S$ and $T$.
Otherwise all trial lines of level $(i+1)$ are added to the temporary storage and the procedure is repeated from Step 1.
- The above algorithm guarantees to find a path if one exists.


## Mikami-Tabuchi's Algorithm ...



- In this example the trial line of level 1 originating from $T$ intersects a trial line of level 2 generated from $S$.


## Hightower's Algorithm

- It is similar to the Mikami-Tabuchi's algorithm.
- The difference is that instead of generating all line segments perpendicular to a trial line, Hightower algorithm considers only those lines that are extendable beyond the obstacle which blocked the preceding trial lines.
- Example.

- The shaded regions $p, q$, and $r$ constitute obstacles around which the path is to be found. The procedure begins by constructing horizontal and vertical lines from the source and target.


## Notes

- When the routing area is not congested, the above algorithms are expected to run fast.
- Particularly, Hightower algorithm is expected to run in time proportional to the number of bends.
- A conservative estimate of running time in a complicated maze is $O\left(N^{4}\right)$
- Thus the memory saving in line search algorithm is dramatic, but the running time does not improve very much.
- We might also need to backtrack from dead ends (resulting from bad sequences of trial lines).


## Other Issues

- Multi Layer Routing
- Three-Dimensional Grid

Three dimensional cellular array for two layer routing is shown below.


- Two Planar Arrays. Figure below illustrates two layer routing using two arrays. (a) Layer-1. (b) Layer-2. (c) Retrace path.

| 3 | 2 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 1 | S | 1 | 2 | 3 |
| 3 | 2 | 1 | 2 | 3 | 4 |
| 4 | 3 | 2 | 3 | 4 | 5 |
| 5 | 4 | 3 | 4 | 5 | 6 |
| 6 | 5 | 4 | 5 | 6 | 7 |
| 7 | 6 | 5 | 6 | 7 | 8 |
|  |  |  |  |  |  |
| 9 | 8 | 7 | 8 | 9 | $\mathbf{T}$ |

(a)

(b)


- Layer-1
...... Layer-2
- Via or cut
- Ordering of Nets.

(a)

(d)

(b)

(e)

(c)

(f)
- Non-transitivity of three 2-point nets.

- Four 2-point nets to be ordered.

(a)

(b)
- (a) Optimal routing of $a$ prevents routing of $b$. (b) Optimal routing of $b$ prevents routing of $a$. (c) Non-optimal routing of nets $a$ and $b$.

(a)

(b)

(c)
- Rip-up and Rerouting
- Power and Ground Routing
(a) Topological trees for power and ground nets. (b) Actual widths of routing layers.

(a)

(b)


## Summary

- In this chapter we examined two types of grid routers, the maze router and line-search router.
- The maze router uses a physical grid, and line search routers use an imaginary grid.
- The basic grid router that uses Lee algorithm has a large memory requirement and also may require a large amount of running time.
- Techniques to reduce the running time and memory requirement were discussed in detail.
- Other algorithms that modify the filling phase of Lee Algorithm to reduce the running time are Hadlock's algorithm and Soukup's algorithm.
- Their techniques were illustrated with examples. Line search algorithms overcome the high memory requirement of Lee algorithm.
- Two line search heuristics, one due to Mikami and Tabuchi, and the other due to Hightower were presented.
- Maze running algorithms guarantee finding a shortest path if one exists, even if it is the most expensive in terms of the number of vias.
- Line search algorithms guarantee finding a path if one exist; (not necessarily the shortest ${ }_{35}$
- But they may require several backtracks for all dead ends that are reached.
- In practice however line search algorithms can be significantly faster than maze running algorithms.
- The major advantage for which maze running algorithms are preferred over line search algorithms is that the former are grid-cell oriented.
- This gives more flexibility to the weighting of routing area of the chip.
- This is of extreme importance since proper weighting of cells enables finding superior routes.
- Both the maze router and line-search router connect a single net at a time.
- Modifications to the basic routing technique to accommodate multi-point nets are needed.


## Algorithm Constraint_Graph_Compaction; 1. Construct the constraint graph $G(V, E)$; <br> 2. Apply the critical path algorithm and find for each ve 3. Move each element to within its range of tolerance; <br> End.

