
SEC 595: Special Topics in Information Assurance & Security

Encrypted Computing

(or Computing on Encrypted Data)

Lecture 1: Introduction

Instructor: Muhamad Felemban



Why A Course on Data Privacy?

Personal Information is Everywhere



INDUSTRY / ELECTRONICS

5,922 views | Mar 12, 2010, 12:35pm

Forbes

Netf 3,615,859 views | Feb 16, 2012, 11:02am

Can How Target Figured Out A
Girl Was Pregnant Before
Father Did



Kashmir Hill Former Staff
Tech

Welcome to The Not-So Private Parts where technology & privacy collide

POLICY \ TECH \ FACEBOOK \

**FTC hits Facebook with \$5 billion fine and new
privacy check**

The largest penalty ever levied

By Makena Kelly | @kellymakena | Jul 24, 2018



Cybernews Team

Updated on: 27 July 2022

9

Apple Apologizes Over Siri Recordings and
Issues New Privacy Protections Moving
Forward

After a whistleblower pointed out
recordings, Apple has made ame

The New York Times

*YouTube Said to Be Fined
Up to \$200 Million for
Children's Privacy Violations*

Scraped data of 500 million LinkedIn users being sold online, 2 million records leaked as proof
n Street View privacy

Netflix Recommendation



"Our personal data is being used against us in ways that we don't understand and it could bring down severe harm on us."

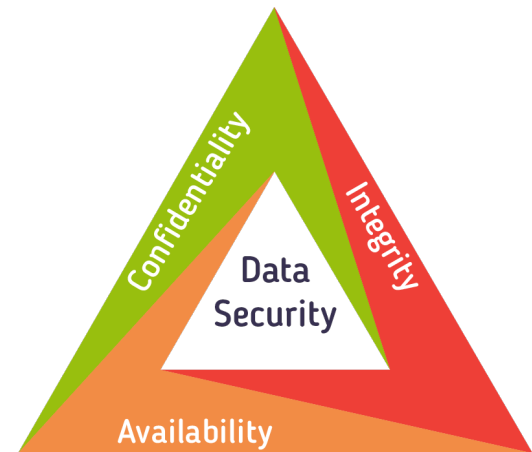
"So, as individuals, we can limit the flood of data that we're leaking all over the place. But there's no silver bullet. **There's no way to go off the grid. So, you have to understand how your data is affecting your life.** Our dignity as humans is at stake. But the hardest part in all of this is that all of these wreckage sites and crippling division begins with **the manipulation of one individual then the other then the other.** So I can't help but to ask myself: can I be manipulated? Can you?"

– David Carroll



What Is Security?

- Security is about protecting data/systems from external or internal forces by preserving the three “pillars” of security
 - Confidentiality
 - Access to systems or data is limited to authorized parties
 - Integrity
 - When you receive data, you get the “right” data
 - Availability
 - The system (or data) is “available” when you need it



What Is Privacy?

- Before we define privacy, allow me to ask you two questions
 - Who enjoys using all the features provided by tech. companies in return for the data we share?
 - Example: Google maps, Fitbit programs, etc.
 - Who gets paranoid about his privacy and keeps the share data features off all the times?
 - Example: customized ads, shared location, incognito mode, etc.
- What Is Privacy?
 - Let's hear from you!



Security Vs. Privacy

- What Is Privacy?
- The terms are often used interchangeably
 - In this course, hopefully you will be able to distinguish between the two
- Two widely accepted definitions of privacy
 - "The right to be let alone"
 - "The fair use of information"
- Privacy is relative to individuals, families, societies, countries, etc.



COE 426/526: Data Privacy

Data Privacy:
Definition and terminologies

Data Privacy Policies, Laws, and Regulations

Privacy Enhancing Technologies

Non-Cryptographic

Anonymization

Differential
Privacy

Cryptographic

Homomorphic
Encryption

Secure
Multiparty
computation

Communication

Anonymous
Network

Privacy-Preserving Enhancing Technologies

Centre for the
Fourth Industrial
Revolution

In collaboration
with Frontiers

Top 10 Emerging Technologies of 2024

FLAGSHIP REPORT
JUNE 2024

WORLD
ECONOMIC
FORUM

1- AI for Scientific Discovery

2- Privacy-Enhancing Technologies

3- Reconfigurable Intelligent Surfaces

4- High Altitude Platform Stations

5- Integrated Sensing and Communication

6- Immersive Technology for the Built World

7- Elastocalorics

8- Carbon-capturing Microbes

9- Alternative Livestock Feeds

10- Genomics and Transplants

The steering group was then presented with a curated list of 70 technologies from which the final 10 were selected. The group reviewed and selected the technologies based on the following criteria:

- **Novelty:** The technology is emerging and at an early stage of development but is not yet widely used.
- **Applicability:** The technology is potentially of significant use and benefit to societies and economies.
- **Depth:** The technology is being developed by more than one company, with the focus of increasing investment interest and excitement.
- **Power:** The technology is potentially game-changing to established ways and industries.



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SEC595: Encrypted Computing

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Computing on Encrypted Data

Nigel Smart  | KU Leuven and Zama

“The ability to compute on encrypted data is fast becoming a practical reality. We discuss the progress in four technologies which enable this:”

**Trusted
Execution
Environments**

**Fully
Homomorphic
Encryption**

**Multi-Party
Computation**

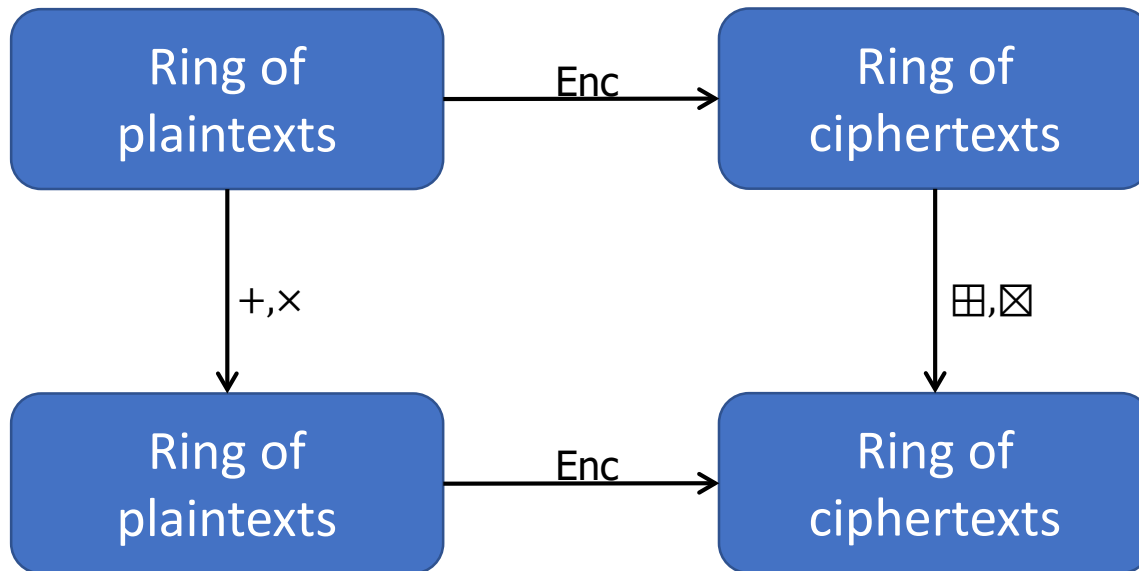
**Zero-
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Proofs.**

<https://www.computer.org/csdl/magazine/sp/2023/04/10194492/1P4BEqduz9C>



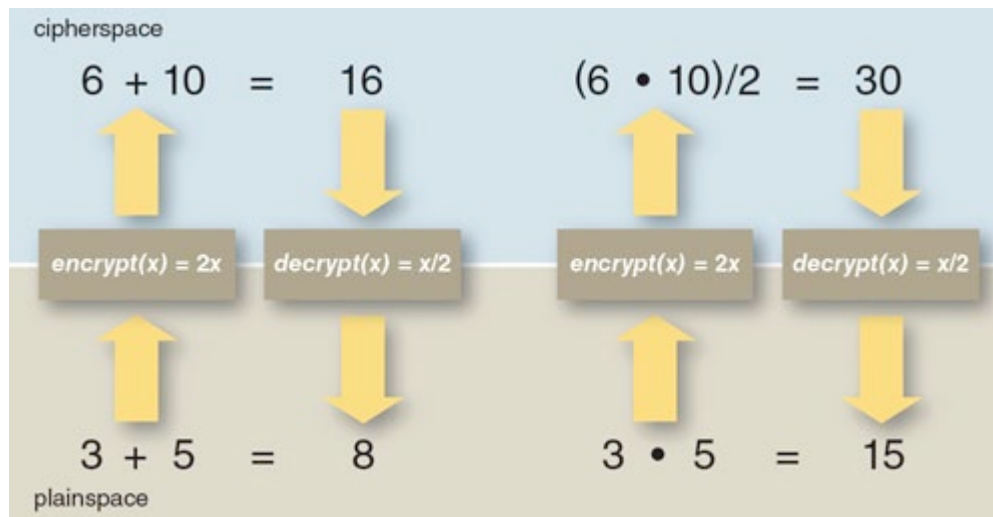
Homomorphic Encryption

- Name inspired by ring-homomorphism



A Toy HE Scheme

- Encryption: Double the plaintext. $x \rightarrow 2x$
- Decryption: Halve the ciphertext. $x \rightarrow x/2$



<https://www.americanscientist.org/article/alice-and-bob-in-cipherspace>

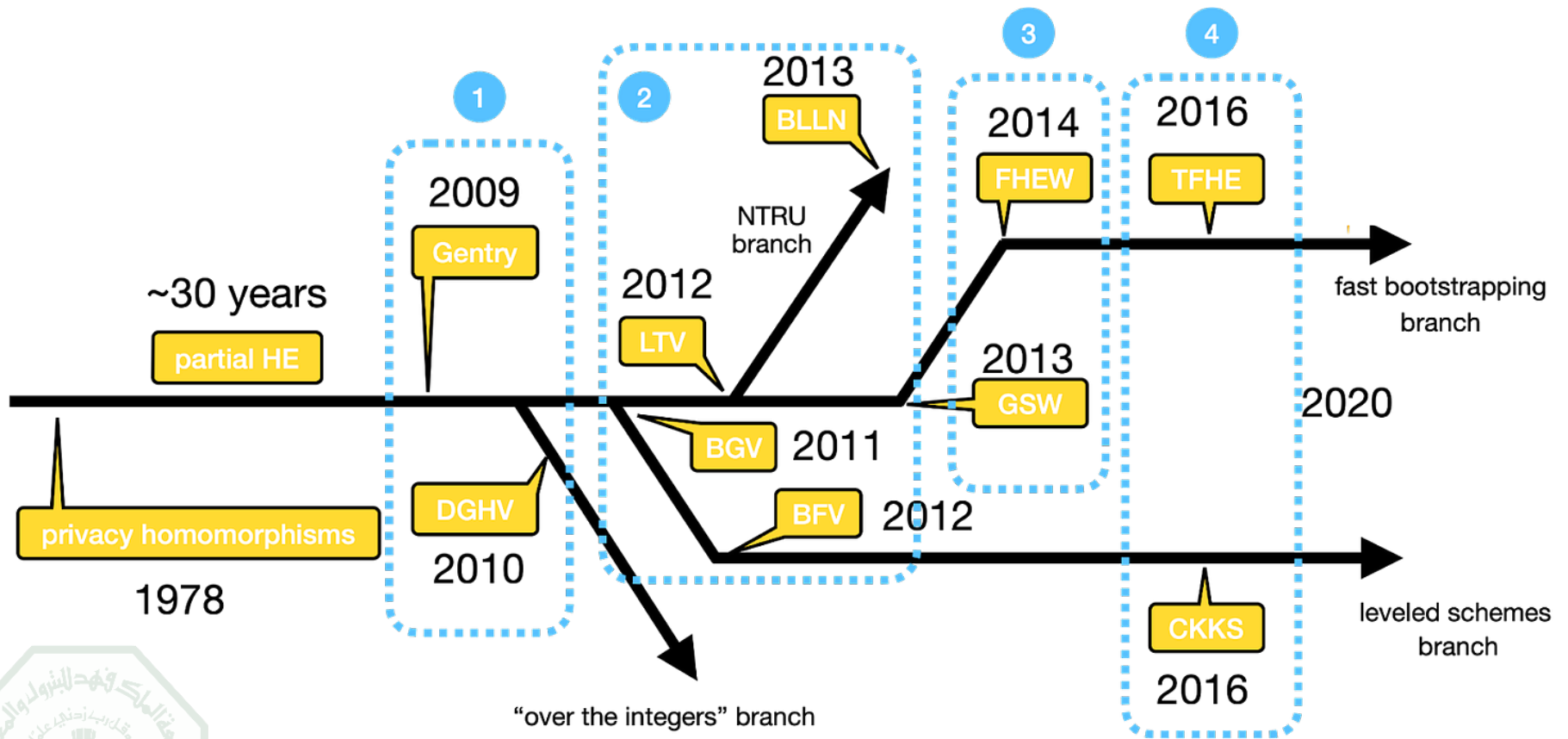


An Analogy

- Alice wants workers to assemble raw materials into jewelry
- But Alice is worried about theft:
 - She wants workers to process raw materials without having access.
- Alice puts raw materials in locked glovebox.
- Workers assemble jewelry inside glovebox, using the gloves.
- Alice unlocks box to get “results”.



Evolution of FHE Schemes



Examples of Homomorphic Encryption

- "Unpadded" RSA is a **multiplicative** homomorphic encryption scheme
 - Recall $E_{PK}(x) = x^e \bmod n$
 - $E_{PK}(x) \cdot E_{PK}(y) = x^e \bmod n \cdot y^e \bmod n$
 $= (x \cdot y)^e \bmod n = E_{PK}(x \cdot y)$
 - How about $E_{PK}(x + y)$?



Examples of Homomorphic Encryption

- Paillier cryptosystem is an **additive** homomorphic encryption scheme

- $E_{PK}(x) = g^x \cdot r^n \bmod n^2$

- $E_{PK}(x) \cdot E_{PK}(y) = (g^x r_1^n) \bmod n^2 \cdot (g^y r_1^n) \bmod n^2$
 $= g^{x+y} (r_1 r_2)^n \bmod n^2 = E_{PK}(x + y)$

- How about $E_{PK}(x \cdot y)$?



Homomorphic Encryption Types

Partially Homomorphic Encryption (PHE)

- Can evaluate functions with very limited operations (+ or *)



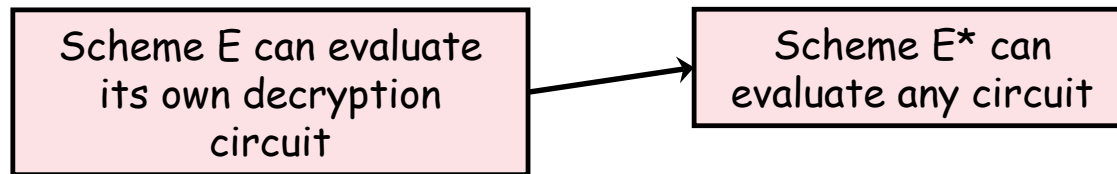
Fully Homomorphic Encryption (FHE)

- Arbitrary functions with any operations



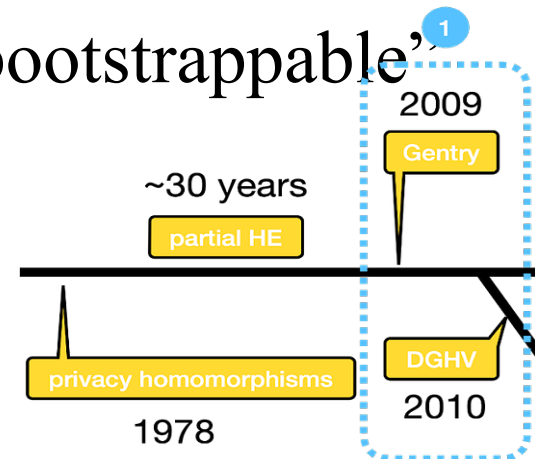
Towards FHE

- Gentry09: A bootstrapping technique
Somewhat homomorphic \rightarrow Fully homomorphic



- Gentry also described a candidate “bootstrappable” scheme

- Based on ideal lattices
- Then extended to integer values



A homomorphic symmetric encryption

- Shared secret key: odd number p
- To encrypt a bit m :
 - Choose at random large q
 - Output $c = pq + 2r + m$
 - Ciphertext is close to a multiple of p
 - $m = \text{LSB}$ of distance to nearest multiple of p
- To decrypt c :
 - Output $m = (c \bmod p) \bmod 2$
$$m = c - p \cdot [c/p] \bmod 2$$
$$= c - [c/p] \bmod 2$$
$$= \text{LSB}(c) \text{ XOR } \text{LSB}([c/p])$$

$2r+m$ much smaller than p



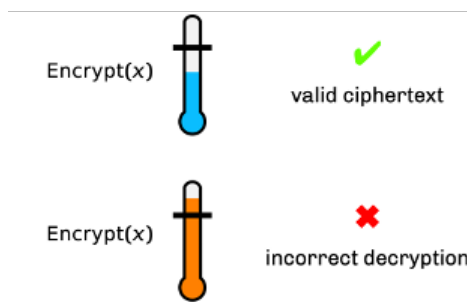
Why is this homomorphic?

- $c_1 = q_1p + 2r_1 + m_1$, $c_2 = q_2p + 2r_2 + m_2$
Distance to nearest multiple of p
- $c_1 + c_2 = (q_1 + q_2)p + 2(r_1 + r_2) + (m_1 + m_2)$
 - $2(r_1 + r_2) + (m_1 + m_2)$ still much smaller than p
 - $c_1 + c_2 \bmod p = 2(r_1 + r_2) + (m_1 + m_2)$
- $c_1 \times c_2 = (c_1q_2 + q_1c_2 - q_1q_2)p + 2(2r_1r_2 + r_1m_2 + m_1r_2) + m_1m_2$
 - $2(2r_1r_2 + \dots)$ still much smaller than p
 - $c_1 \times c_2 \bmod p = 2(2r_1r_2 + \dots) + m_1m_2$



How homomorphic is this?

- Can keep adding and multiplying until the “noise term” grows larger than $q/2$
 - Noise doubles on addition, squares on multiplication



- We choose $r \sim 2^n$, $p \sim 2^{n^2}$ (and $q \sim 2^{n^5}$)
 - Can compute polynomials of degree $\sim n$ before the noise grows too large



Homomorphic Public-Key Encryption

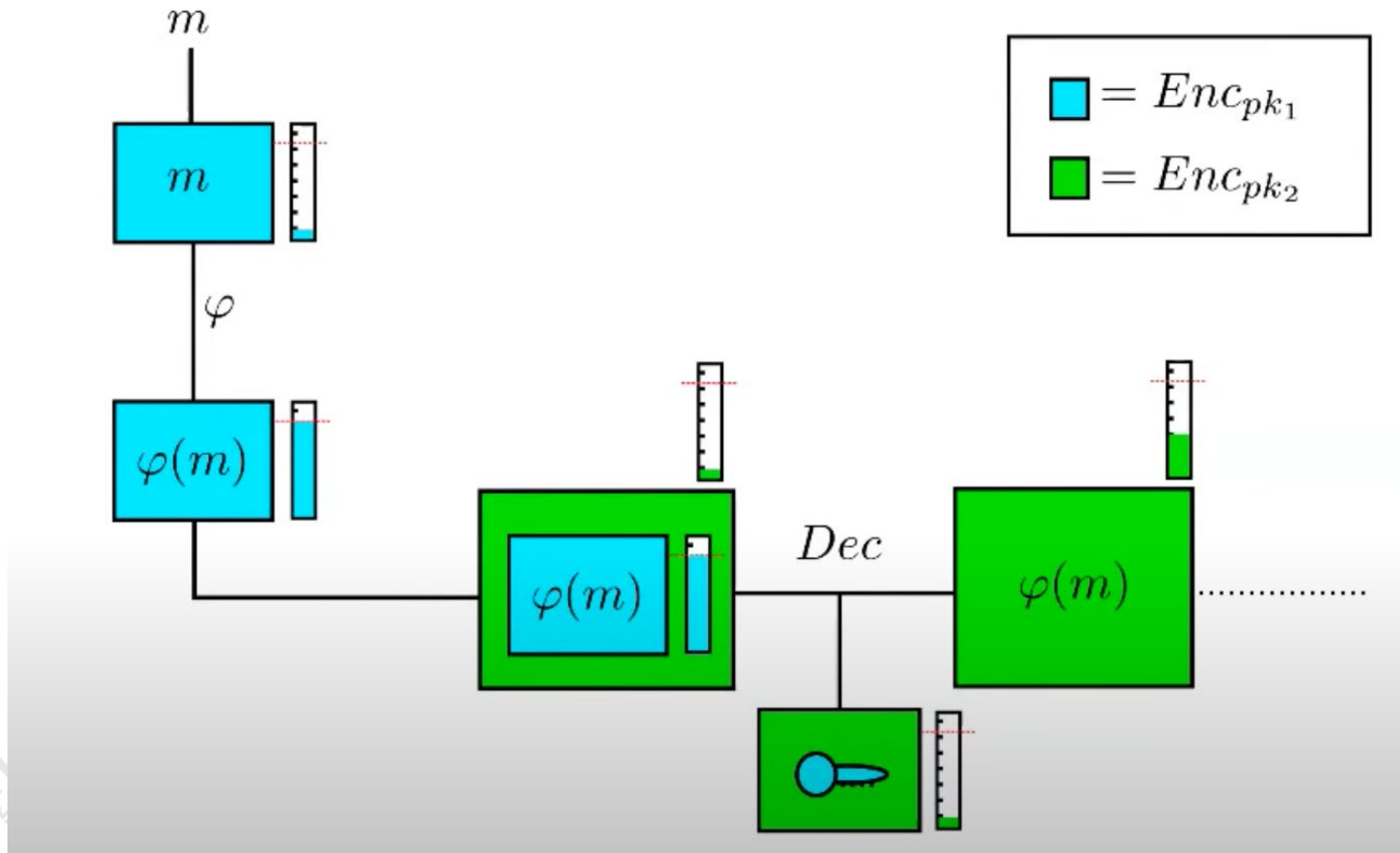
- Secret key is an odd p as before
- Public key is many “encryptions of 0”
 - $x_i = q_i p + 2r_i$
- $\text{Enc}_{pk}(m)$: Choose a random subset $S \subseteq \{1, 2, \dots, \tau\}$ and a random integer r and output

$$c \leftarrow \left[m + 2r + 2 \sum_{i \in S} x_i \right]_{x_0}$$

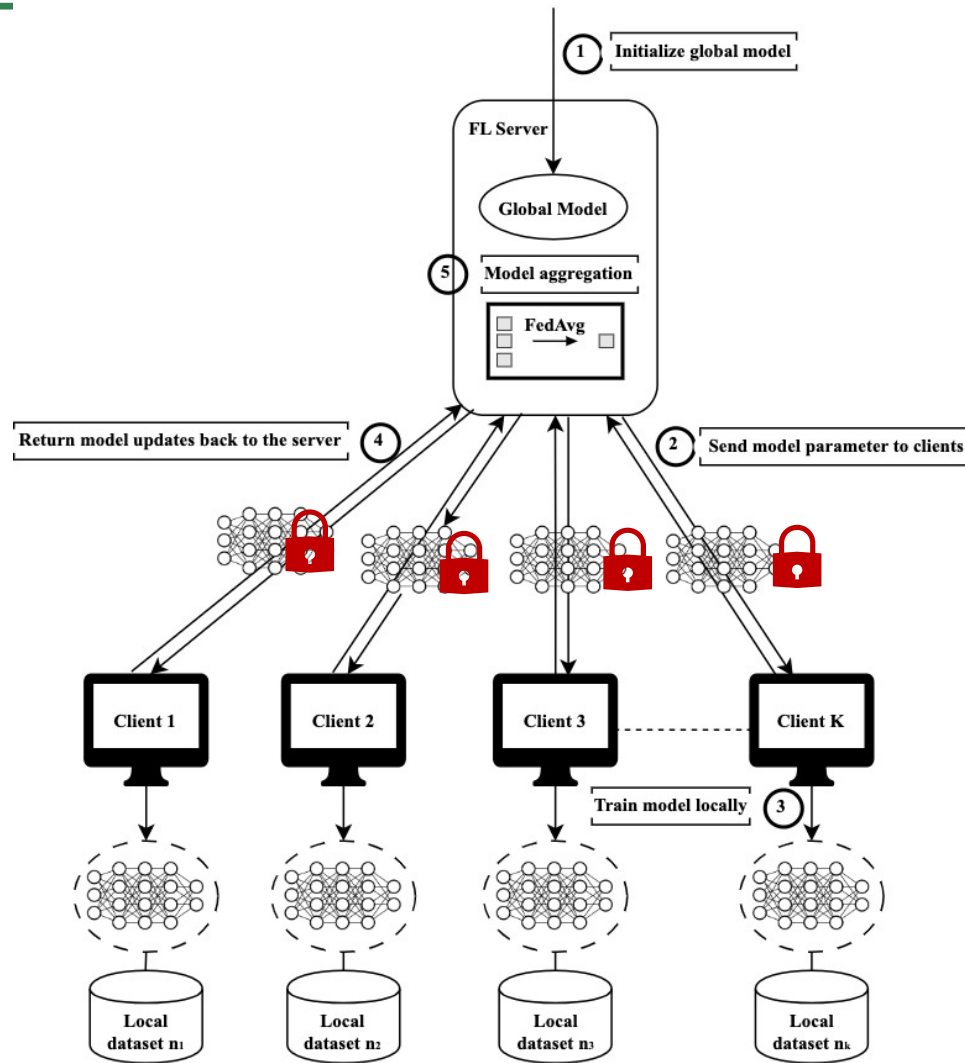
- $\text{Dec}_{sk}(c) = (c \bmod p) \bmod 2$
- Eval as before



Bootstrapping



Use case



Speeding Up Bootstrapping

Cheetah: Optimizing and Accelerating Homomorphic Encryption for Private Inference

Brandon Reagen^{*1,2}, Woo-Seok Choi^{*3}, Yeongil Ko⁴, Vincent T. Lee⁵
Hsien-Hsin S. Lee², Gu-Yeon Wei⁴, David Brooks⁴

NTT Architecture for a Linux-Ready RISC-V Fully-Homomorphic Encryption Accelerator

Rogério Paludo[Ⓜ], *Student Member, IEEE*, and Leonel Sousa[Ⓜ], *Senior Member, IEEE*

GPU Acceleration of High-Precision Homomorphic Computation Utilizing Redundant Representation

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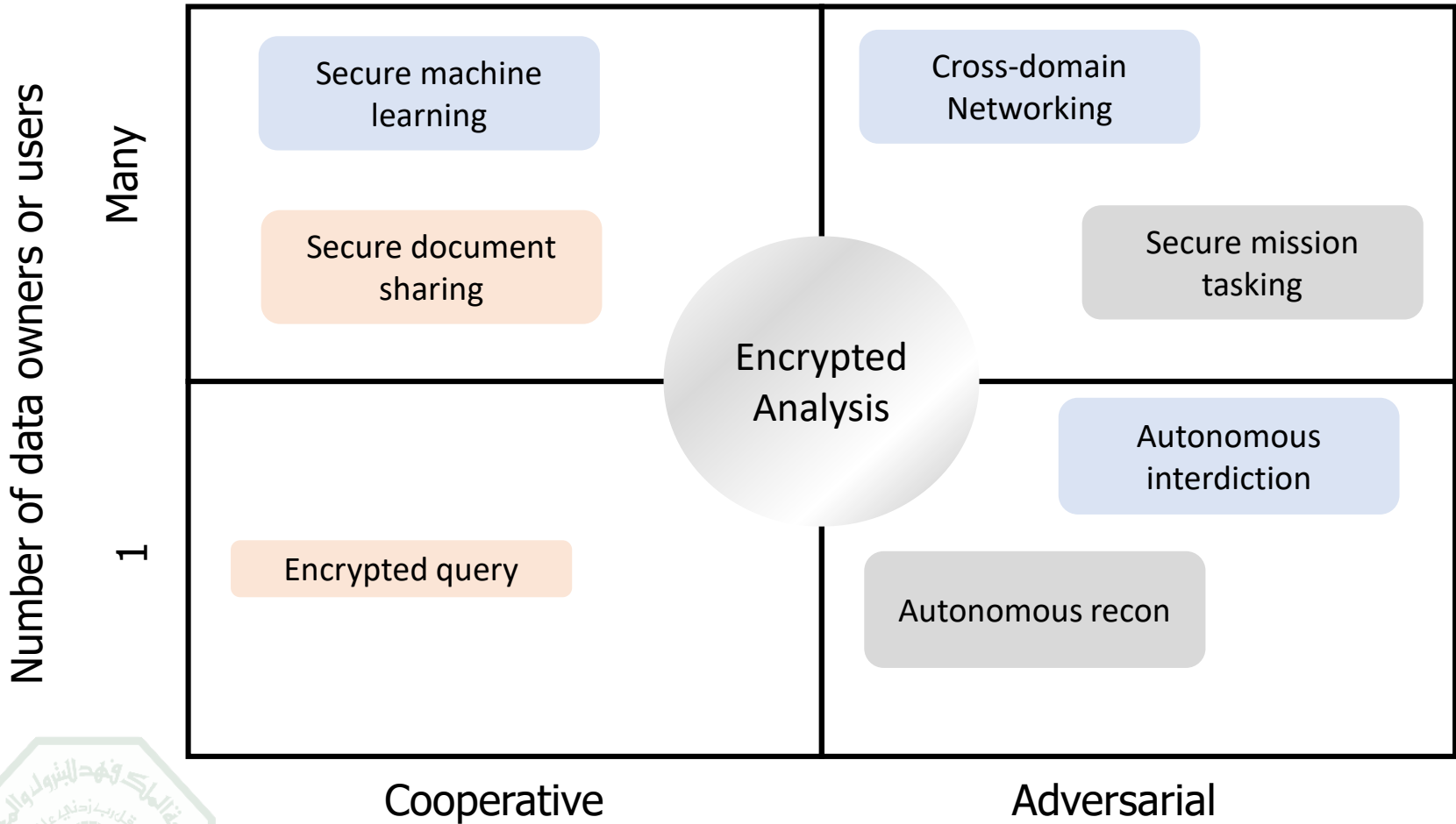
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FHE Application Space



*Source: DARPA DPRIVE presentati



Computing on Encrypted Data

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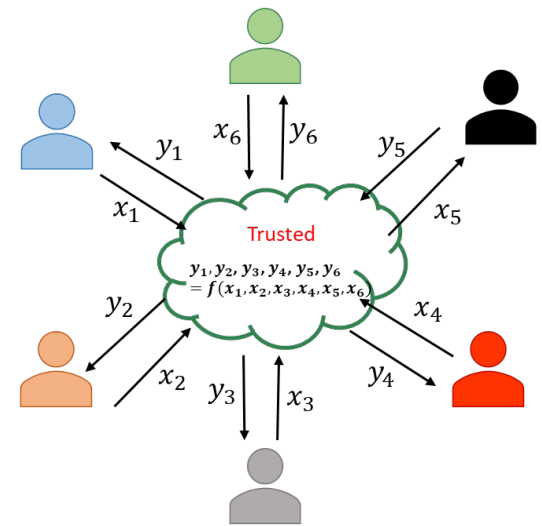
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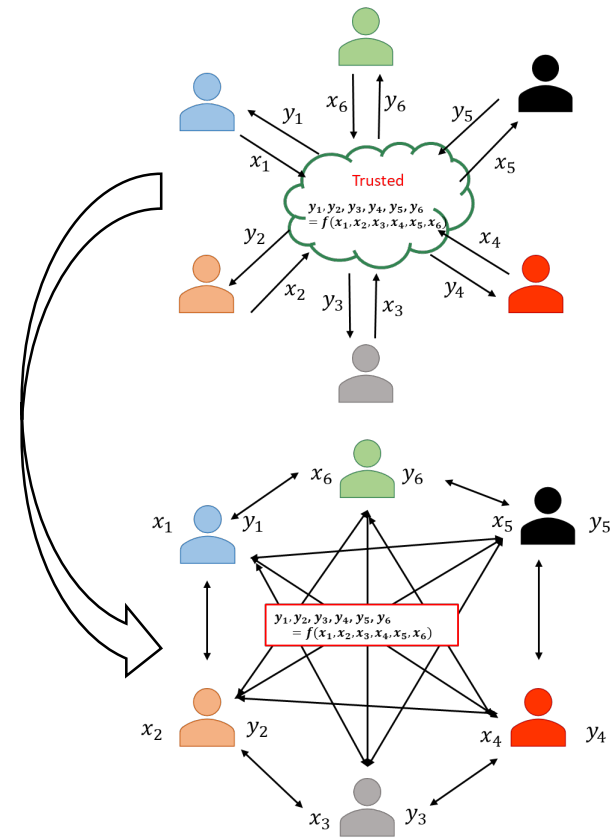
Secure Multiparty Computation (SMPC or MPC)

- Secure multiparty computation is a subfield of encrypted computation
- MPC involves multiple parties (who do not trust each other) agreeing to compute a joint function of their inputs but only if the data is encrypted
- Parties wish to preserve
 - **Privacy:** parties can't observe each others' inputs
 - **Correctness:** the function gives the correct results
- Privacy must be preserved in the face of adversarial behavior by
 - One (or some) of the participants, or
 - An external party



A Couple of Observations

- In all cases, we are dealing with distributed multi-party protocols
 - A protocol describes how parties are supposed to exchange messages on the network
- All these tasks can be easily computed by a **trusted third party**
- The goal of secure multi-party computation is to achieve the same result **without involving a trusted third party**



Yao's Millionaire Problem

- Yao's Millionaire Problem is another example of
- Two millionaires, Alice and Bob want to know who of them is richer without revealing their actual wealth
- This problem is analogous to a more general problem where there are two numbers A and B and the goal is to solve the inequality $A > B$ without revealing the actual values of A and B
- We will see a solution to Yao's Millionaire problem using encrypted computing

I am more rich

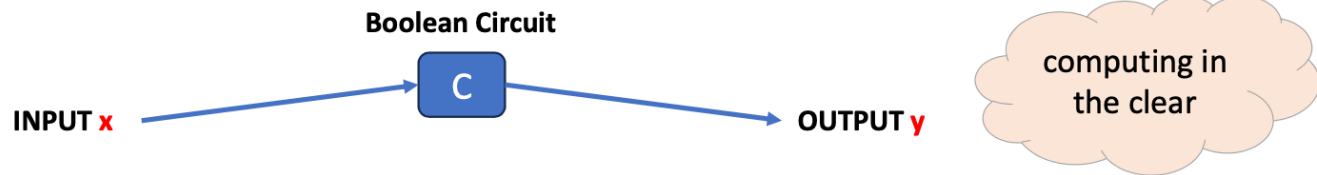


I am rich



Garbled Circuit

- A “**garbled**” version of a Boolean circuit
 - Also known as **encrypted** circuit, or **scrambled** circuit
- Overview



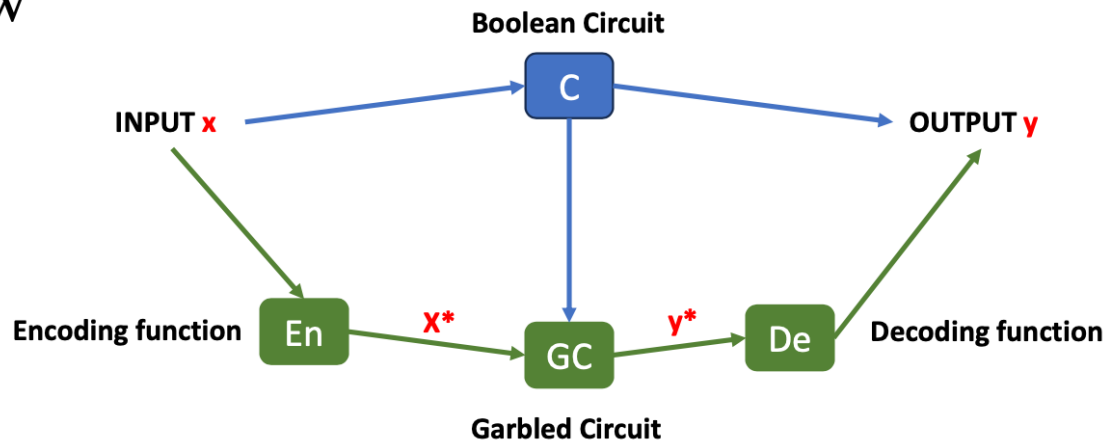
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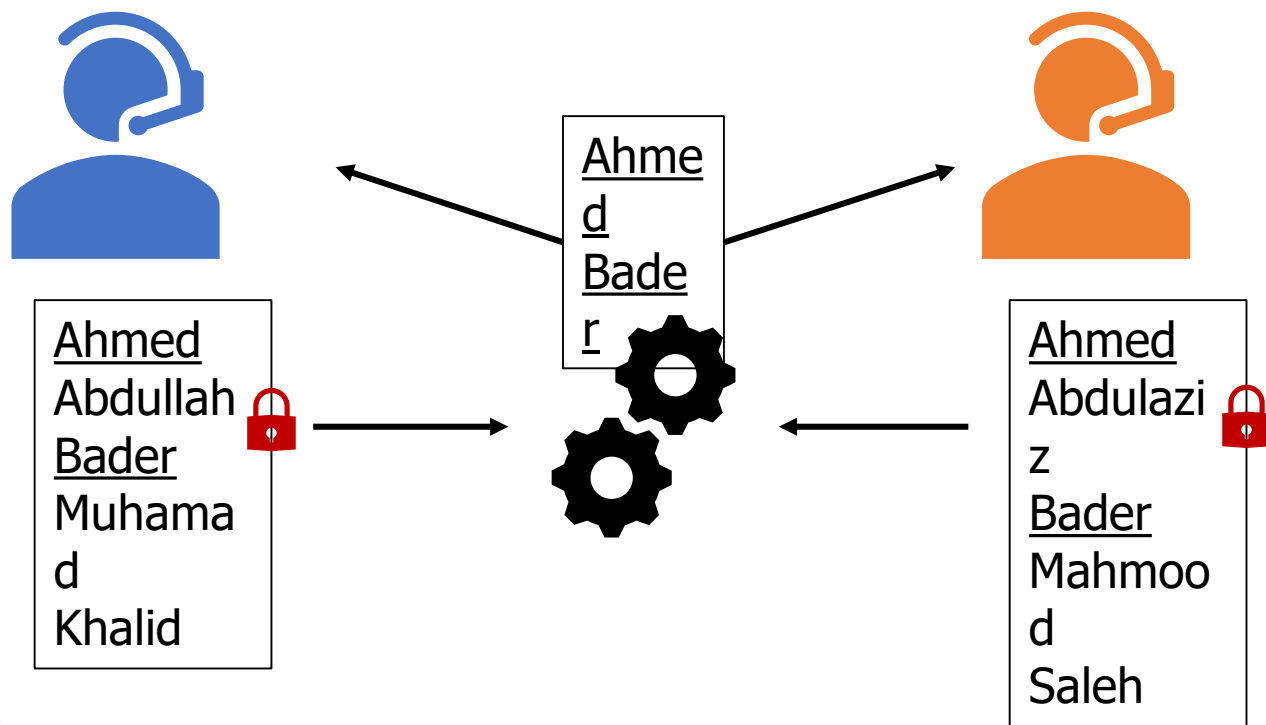


computing in
“secure” way

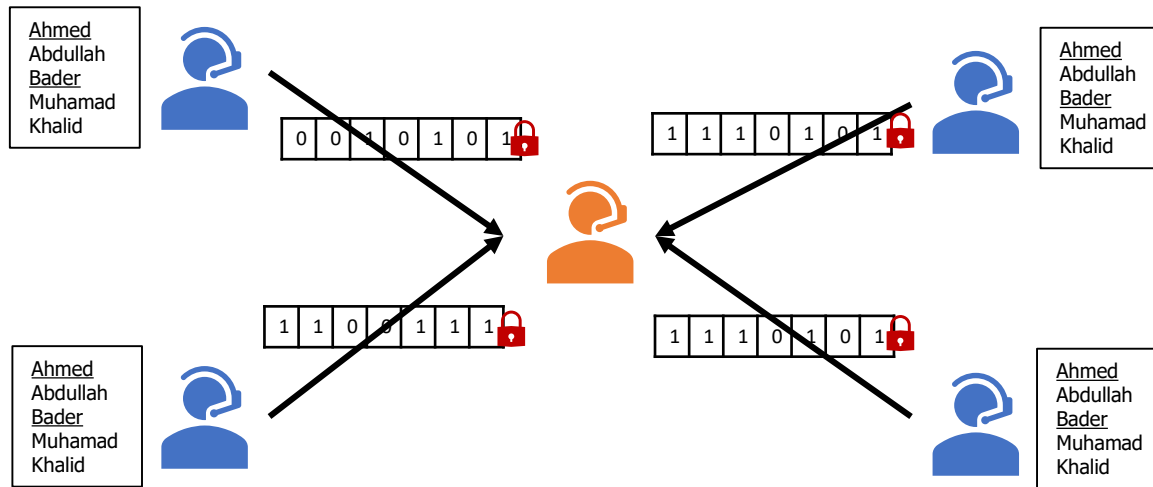
Bellare, Mihir, Viet Tung Hoang, and Phillip Rogaway. "Foundations of garbled circuits." *Proceedings of the 2012 ACM conference on Computer and communications security*. 2012.



Use case: Private Set Intersection



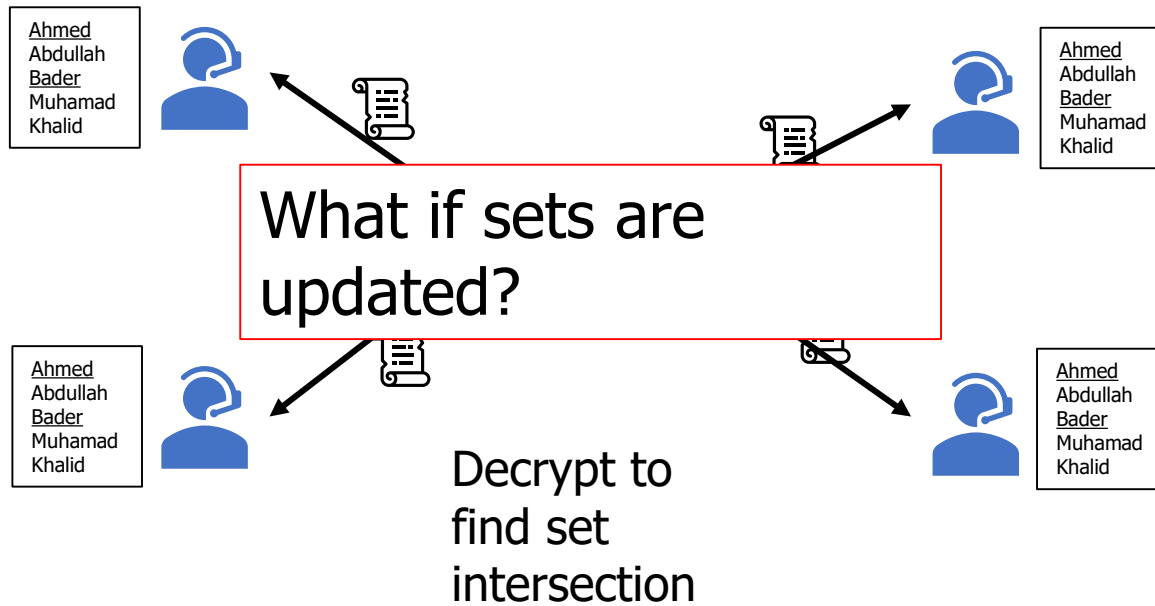
Practical Multi-Party Private Set Intersection Protocols



Bay, Asli, et al. "Practical multi-party private set intersection protocols." *IEEE Transactions on Information Forensics and Security* 17 (2021): 1-15



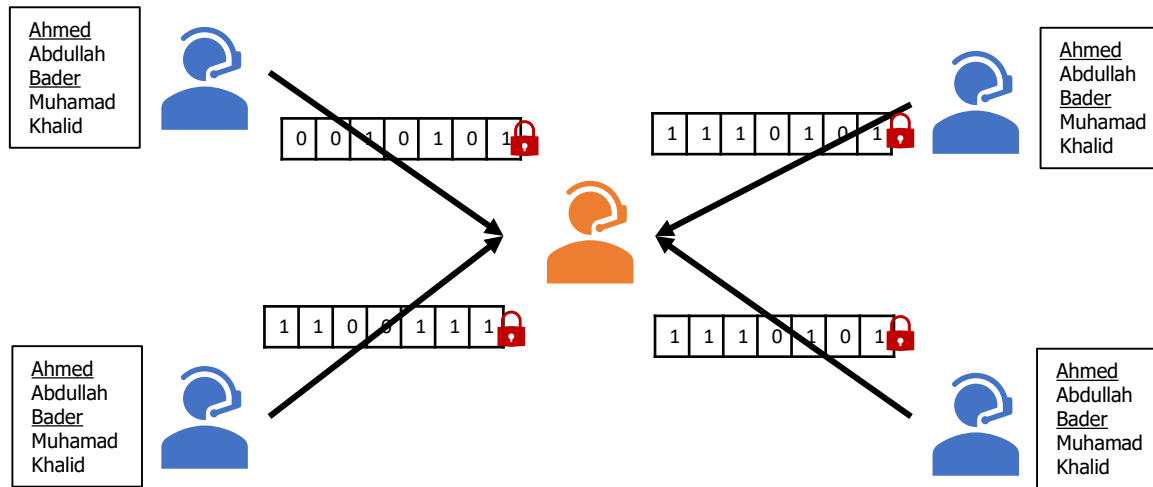
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"Updatable" Multi-Party Private Set Intersection Protocols



Exciting News!!

NIST Announces Post-Quantum Cryptography Standards › Three security standards are ready for use, with a fourth on the way

BY [DINA GENKINA](#) | 13 AUG 2024 | 5 MIN READ | 

Dina Genkina is the computing and hardware editor at IEEE Spectrum



Course Objectives

- The objective of this course is to
 - i. Introduce the students to the emerging field of encrypted computing.
 - ii. Expose students to the state-of-the-art algorithms in homomorphic encryption and secure multiparty computation



Course Learning Outcomes

After taking this course, you will be able to

1. Explain various encrypted computing techniques and algorithms.
2. Identify the advantages and challenges of different encrypted computing algorithms.
3. Apply appropriate encrypted computing techniques based on the application's requirements.
4. Design new encrypted computing techniques and protocols.



Logistics

- Lectures: Sunday & Tuesday, 6:45-8:00 PM
- Office hours: UT 8:00-9:00 PM
 - Office# 22-214
 - Teams (or send me on Teams and I will try to accommodate your Qs online)
- Web page:
 - Blackboard page



Logistics

- Evaluation

- Paper Presentation 10 %
- Term Project 30%
- Major Exam 30%
- Final Exam 30%



Logistics

- Course Project:
 - Teams of 2-3 (if you want to work alone, please let me know ahead of time)
 - Project proposal: 0.5-1 page (TBA)
 - Deliverable Part I: 1-2 page Progress report (TBA)
 - Deliverable Part II: Written report: 4-8 pages (TBA)
 - In-class presentations (Week 15)

