

- Write the *sum-of-minterms* **and** *product-of-maxterms* expressions **for both** the *true* and the *complement* form of the following Boolean expressions:

- $\bar{X}\bar{Z} + Y\bar{Z} + XYZ$
- $\bar{A}\bar{B} + A\bar{C}\bar{D} + \bar{B}C + \bar{A}B\bar{C}\bar{D}$

- Write the *sum-of-minterms* **and** *product-of-maxterms* expressions **for both** the *true* and the *complement* form of the following Boolean expressions:

- $\bar{X}\bar{Z} + Y\bar{Z} + XYZ$

X	Y	Z	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

$$F(X, Y, Z) = \sum(0, 2, 6, 7) = \prod(1, 3, 4, 5)$$

$$\bar{F}(X, Y, Z) = \sum(1, 3, 4, 5) = \prod(0, 2, 6, 7)$$

or through algebraic manipulation:

$$\begin{aligned} F(X, Y, Z) &= \bar{X}\bar{Z} + Y\bar{Z} + XYZ \\ &= \bar{X}(\bar{Y} + Y)\bar{Z} + (\bar{X} + X)Y\bar{Z} + XYZ \\ &= \bar{X}\bar{Y}\bar{Z} + \bar{X}Y\bar{Z} + X\bar{Y}\bar{Z} + XYZ \\ &= m_0 + m_2 + m_6 + m_7 = \sum(0, 2, 6, 7) = \prod(1, 3, 4, 5) \end{aligned}$$

- $\bar{A}\bar{B} + A\bar{C}D + \bar{B}C + \bar{A}BC\bar{D}$

A	B	C	D	F
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$$F(A, B, C, D) = \sum(0, 1, 2, 3, 4, 9, 10, 11, 13) = \prod(5, 6, 7, 8, 12, 14, 15)$$

$$\bar{F}(A, B, C, D) = \sum(5, 6, 7, 8, 12, 14, 15) = \prod(0, 1, 2, 3, 4, 9, 10, 11, 13)$$

Again, the above can be found through algebraic manipulation.