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**Example 8 - Generating Exponential r.v.** Problem: Generating exponential random variables with parameter  $\lambda$ Answer: To generate an exponentially distributed r.v. X with parameter  $\lambda$  (i.e. its mean is 1/ $\lambda$ ), we need to find  $F_X(x)$  and invert it.  $F_{\chi}(x) = 1 - e^{-\lambda x}$  (see example 1) Therefore,  $F_{x}^{-1}(x)$  is equal to  $X = -(1/\lambda) \ln(1-U)$ where ln(t) is the natural logarithm of t while U is a uniform r.v. between 0 and 1. Note that the above expression can be simplified to be  $X = -(1/\lambda) \ln(U)$ This is because 1-U is also a uniform random r.v. between 0 and 1 10/3/2004 Dr. Ashraf S. Hasan Mahmoud 58



















 <u>Problem</u>: The number of bytes N in a message has a geometric distribution with parameter p. The message is broken into packets of maximum length M bytes. Let Q be the number of full packets in a message and let R be the number of bytes left over. Find the join pmf and the marginal pmfs of Q and R.

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## Example 14:

 Problem: The number of customers that arrive at a service station during a time t is a Poisson random variable with parameter βt. The time required to service each customer is exponentially distributed with parameter α. Find the pmf for the number of customers N that arrive during the service time T of a specific customer. Assume the customer arrivals are independent of the customer service time.

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