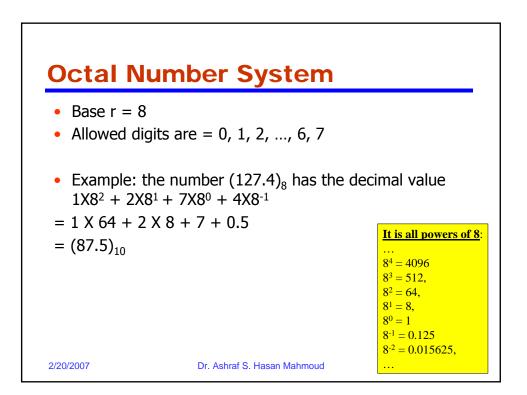


A Very Useful Table									
 To represent decimal numbers from 0 till 15 (16 numbers) we need FOUR binary digits B₃B₂B₁B₀ In general to represent 									
N numbers, we need	Decimal	Binary	Decimal	Binary					
$\left\lceil \log_2 N \right\rceil$ bits	0	0000	8	1000					
• Note than:	1	0001	9	1001					
 B₀ flipped or COMPLEMENTED 	2	0010	10	1010					
at every increment	3	0011	11	1011					
 B₁ flipped or COMPLEMENTED 	4	0100	12	1100					
 every 2 steps B₂ flipped or COMPLEMENTED 	5	0101	13	1101					
every 4 steps	6	0110	14	1110					
• B ₃ flipped or COMPLEMENTED	7	0111	15	1111					
2/20/2007 every 8 steps Dr. Ashraf S. H	lasan Mahmou	d		10					

A Very Useful Ta	able -	- con	t'd	
 Note that zeros to the left its value 	of the nu	ımber do	not add t	0
• When we need DIGITS				
beyond 9, we will use	Decimal	Binary	Decimal	Binar
the alphabets as shown	0	0000	8	1000
in Table	1	0001	9	1001
 Example: base 16 system 	2	0010	10 → A	1010
has 16 digits; these are: 0, , 1, 2, 3,, 8, 9, A, B, C,	3	0011	11 → B	1011
D, E, F	4	0100	12 → C	1100
 This is referred to as 	5	0101	13 → D	1101
HEXADECIMAL or HEX	6	0110	14 → E	1110
number system	7	0111	15 → F	1111
2/20/2007 Dr. Ashraf S. H	lasan Mahmou	d		11

Decimal to Binary Fractions	Conve	ersion	of	
• Example: $(0.234375)_{10} = (?)_2$	No	NoX2	Integer	Part
 Solution: We use the following procedure 	0.234375	/ 0.46875	0	-
• <u>Note:</u>	0.46875	/ 0.9375	0	MSE
 The binary digits are the integer part of the multiplication process 	0.9375	1.875	1	
The process stops when the	0.875	1.75	1	
number is 0 There are situations where the 	0.75 📕	1.5	1	
process DOES NOT end – See next slide	0.5	1.0	1	-
• Therefore $(0.234375)_{10} =$	0			LSD
$(0.001111)_2$ • To check: $(0.001111)_2 = 1X2^{-3}$ +1X2 ⁻⁴ +1X2 ⁻⁵ +1X2 ⁻⁶ = 2/20/2(0.234375) ₁₀ Dr. Ashraf S.	In general: to to its equivale above procedu	nt in base r w	ve use the	n 12

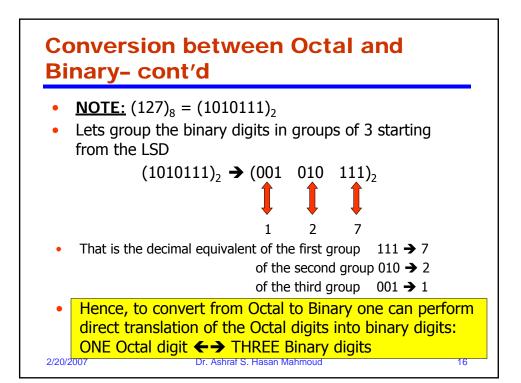
Decimal to Binary Con Fractions - cont'd	versio	on of	
• Example: $(0.513)_{10} = (?)_2$	No	NoX2	Integer Part
 Solution: As in previous slide 	0.513	1.026	1
	0.026	0.052	0
	0.052	0.104	0
Therefore $(0.513)_{10} = (0.100000110)$) ^{0.104}	0.208	0
) ₂	0.208	0.416	0
	0.416	0.832	0
If we chose to round to 1 significant	- ^{0.832}	1.664	1
5	0.664	1.328	1
figure \rightarrow (0.1) ₂	0.328	0.656	0
Or to 7 significant figures \rightarrow (0.1000001) ₂			
Etc.			
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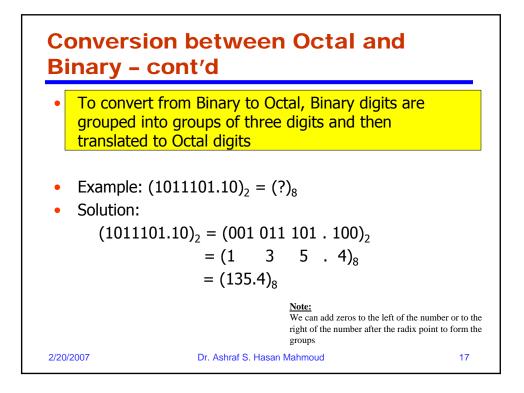


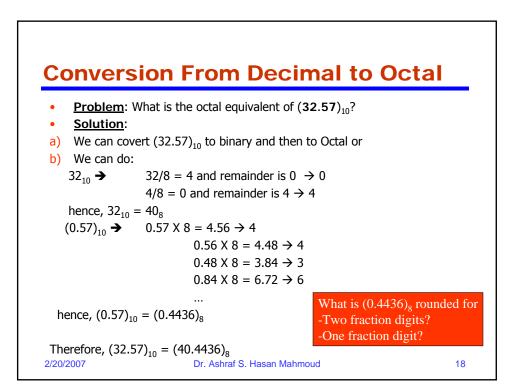
Conversion between Octal and Binary

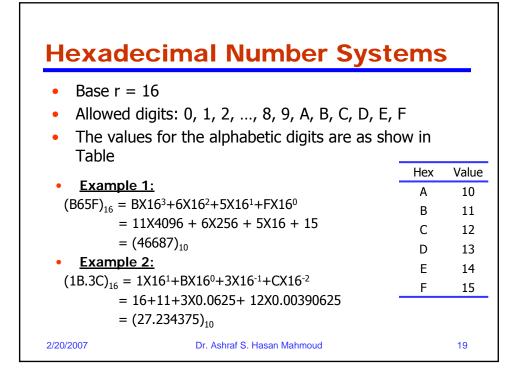
• **Example:** $(127)_8 = (?)_2$

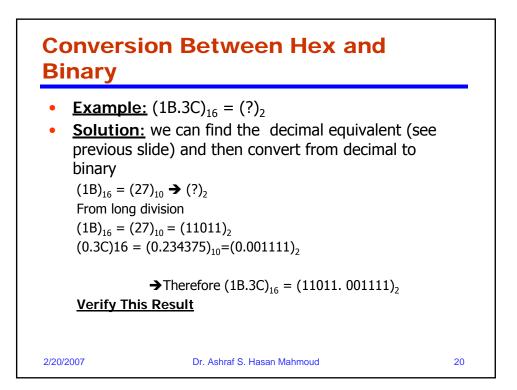
	we can find the decin lide) and then convert	•		•
(127) ₈ = (8	7) ₁₀ → (?) ₂	No	No/2	Remainder
From long o	livision	87	43	1
$(127)_8 = (8)$	$7)_{10} = (1010111)_2$	43	21	1
To check:		21	10	1
1X2 ⁶ +1X2	$2^{4}+1X2^{2}+1X2^{1}+1X2^{0}$	10	5	0
= 64 + 16 ·	+ 4 + 2 + 1	5	2	1
= 87		2	1	0
		1	0	1
2/20/2007	Dr. Ashraf S. Hasan Mahmo	bud		15

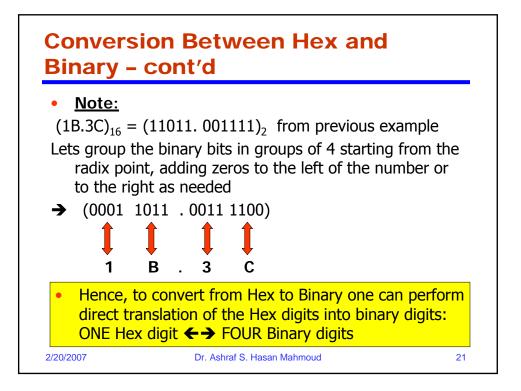


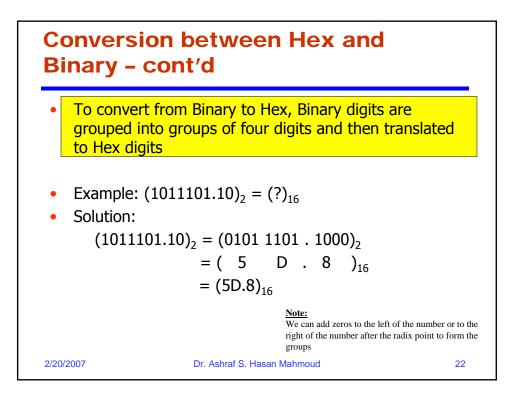




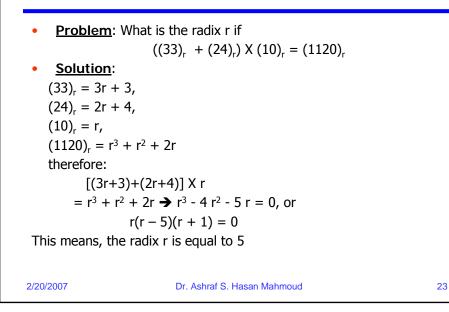


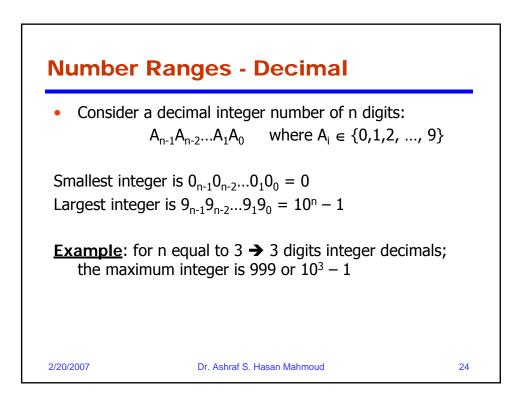


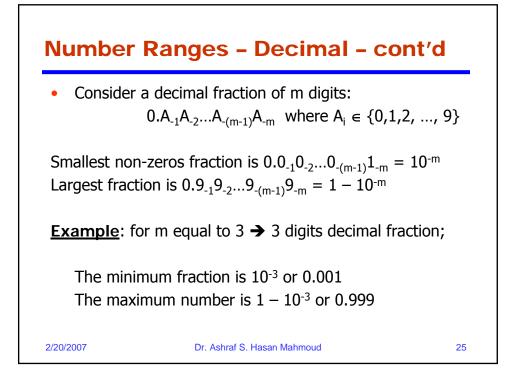


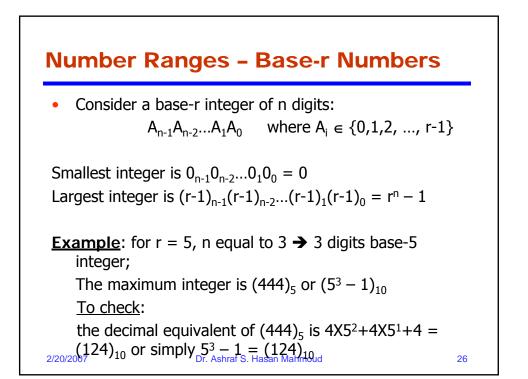


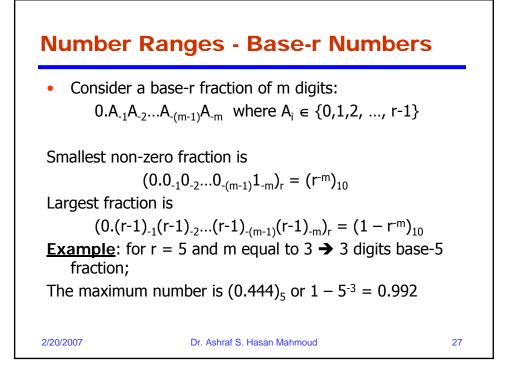




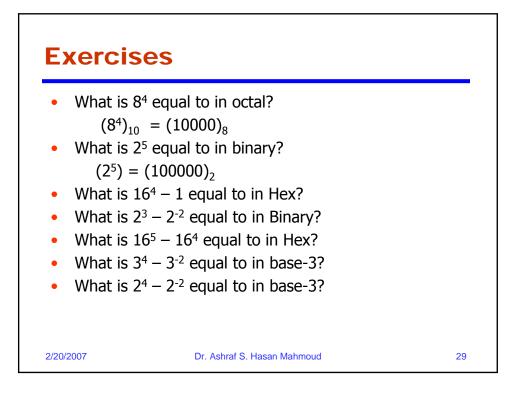


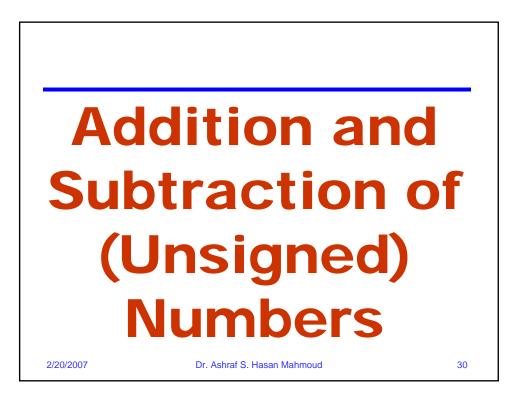


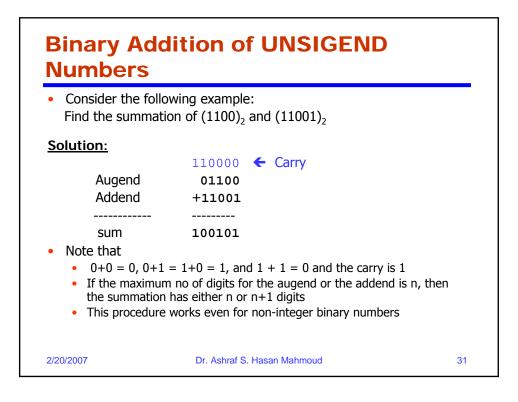


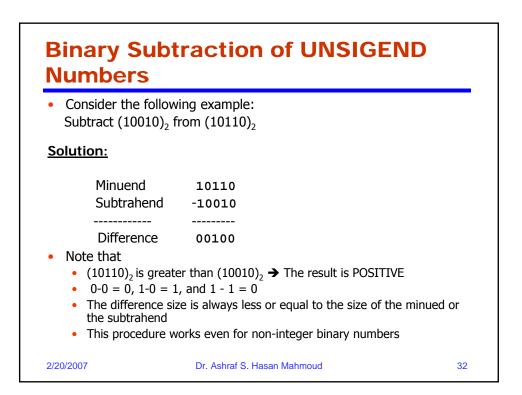


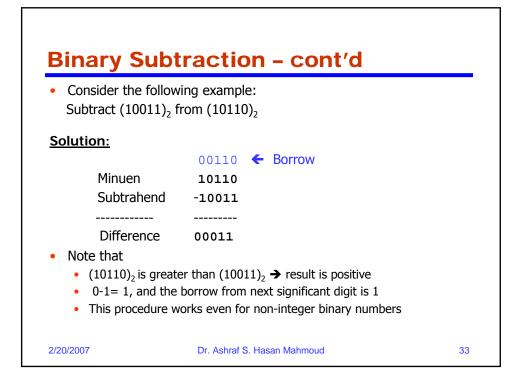
	umb ont/o	oer Rango d	es - Base	e-r Numb	ers –
		Decimal (r=10)	Binary (r = 2)	Octal (r = 8)	Hex (r = 16)
Integer	Min	$0_{n-1}0_{n-2}0_{1}0_{0}$ = 0	$0_{n-1}0_{n-2}0_{1}0_{0}$ = 0	$0_{n-1}0_{n-2}0_{1}0_{0}$ = 0	$0_{n-1}0_{n-2}0_{1}0_{0}$ = 0
	Мах	$9_{n-1}9_{n-2}9_{1}9_{0}$ = 10 ⁿ - 1	$(1_{n-1}1_{n-2}1_{1}1_{0})_{2} = (2^{n}-1)_{10}$	$(8_{n-1}8_{n-2}8_18_0)_8 = (8^n - 1)_{10}$	$(F_{n-1}F_{n-2}F_1F_0)_{16} = (16^n - 1)_{10}$
fraction	Min	$\begin{array}{l} 0.0_{\text{-1}}0_{\text{-2}}0_{\text{-(m-1)}}1_{\text{-m}} \\ = 10^{\text{-m}} \end{array}$	$(0.0_{-1}0_{-2}0_{-(m-1)}1_{-m})_2 = (2^{-m})_{10}$	$(0.0_{-1}0_{-2}0_{-(m-1)}1_{-m})_8 = (8^{-m})_{10}$	$(0.0_{-1}0_{-2}0_{-(m-1)}1_{-m})_{16} = (16^{-m})_{10}$
	Мах	$\begin{array}{l} 0.9_{\cdot 1}9_{\cdot 2}9_{\cdot (m\cdot 1)}9_{\cdot m} \\ = 1-10^{\cdot m} \end{array}$	$\begin{array}{l} (0.1_{\cdot 1}1_{\cdot 2}1_{\cdot (m \cdot 1)}1_{\cdot m})_2 \\ = (1 - 2^{\cdot m})_{10} \end{array}$	$(0.7_{.1}7_{.2}7_{-(m-1)}7_{-m})_8 = (1 - 8^{-m})_{10}$	$(0.F_{-1}F_{-2}F_{-(m-1)}F_{-m})_{16} = (1 - 16^{-m})_{10}$
2/20/2	2007	Dr	. Ashraf S. Hasan Mahr	noud	28

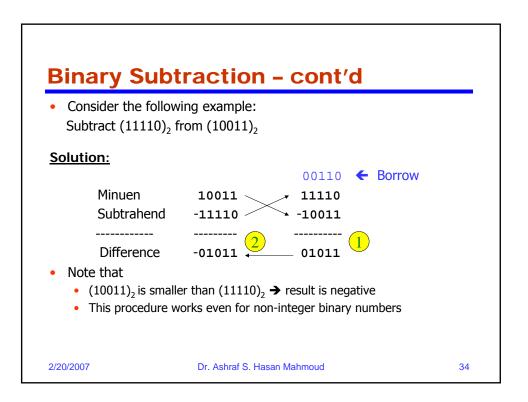




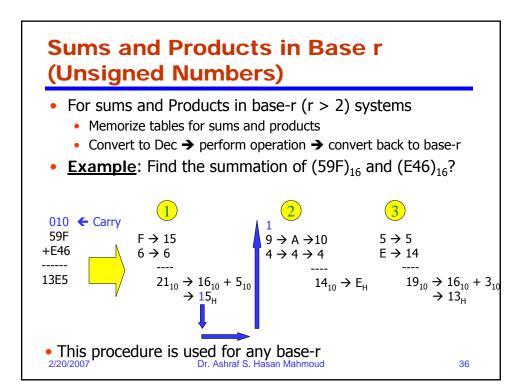


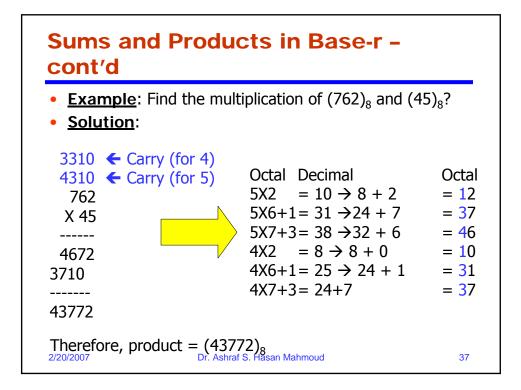


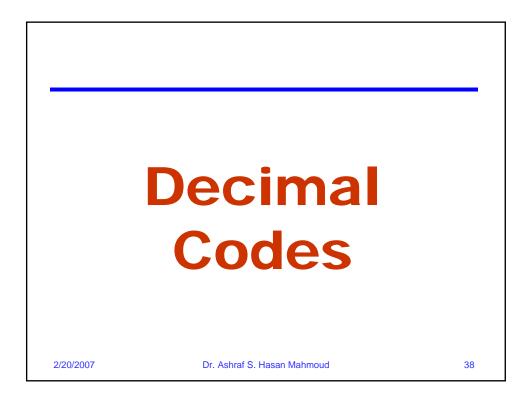


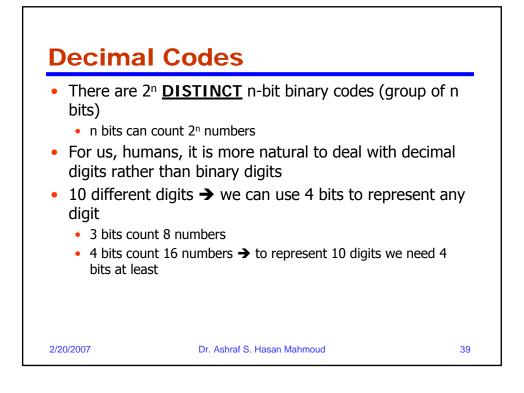


Consider the follo Multiply (1011), b		
Solution:		
Multiplicand	1011	
Multiplier	X 101	
	1011	
	0000	
	1011	
Product	110111	
2/20/2007	Dr. Ashraf S. Hasan Mahmoud	35

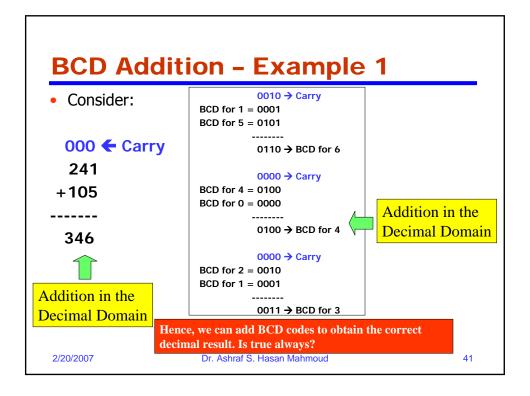


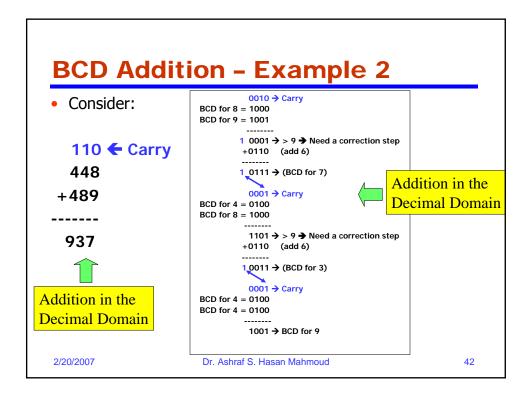


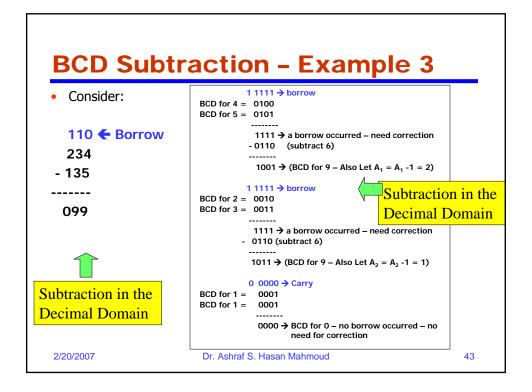


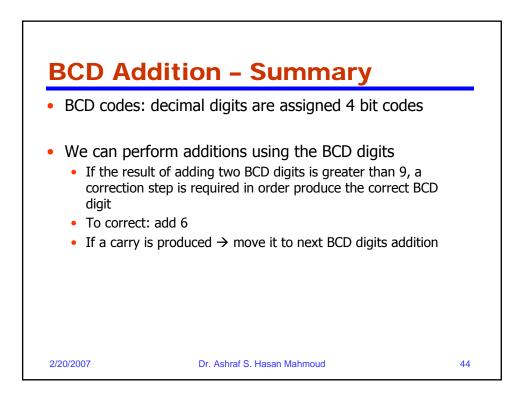


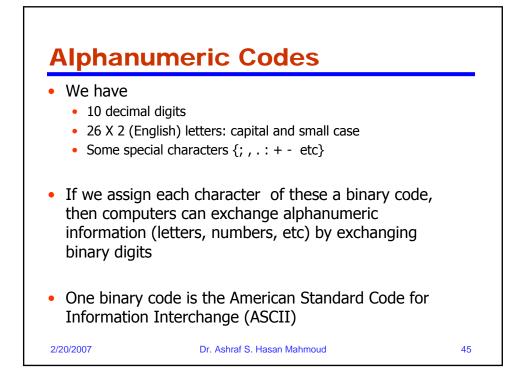
Binary Coded D	ecim	al (B	CD)				
 Let the decimal digits be coded as show in table 	Decimal Digit	Binary Code	Decimal Digit	Binary Code			
T he second second second the	0	0000	5	0101			
 Then we can write numbers as 	1	0001	6	0110			
	2	0010	7	0111			
	3	0011	8	1000			
	4	0100	9	1001			
$(396)_{10} = (0011\ 1001\ 0110)_{BCD}$ Since $3 \rightarrow 0011$, $9 = 1001$, $6 = 0110$							

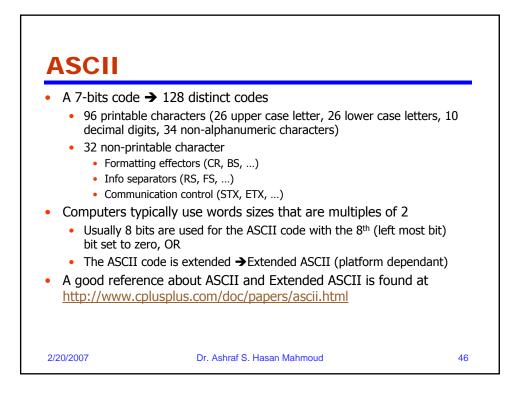


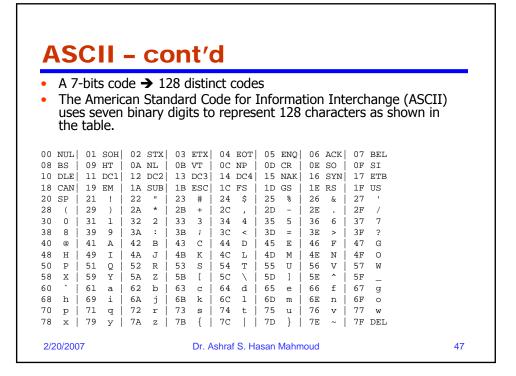




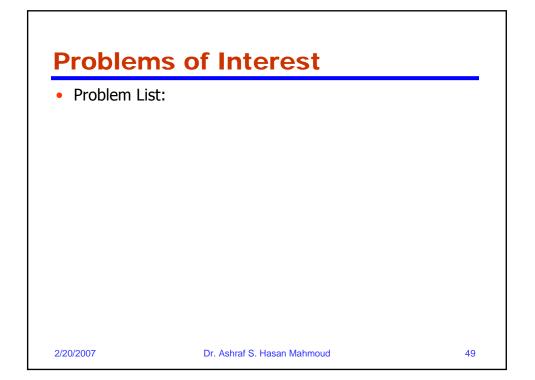


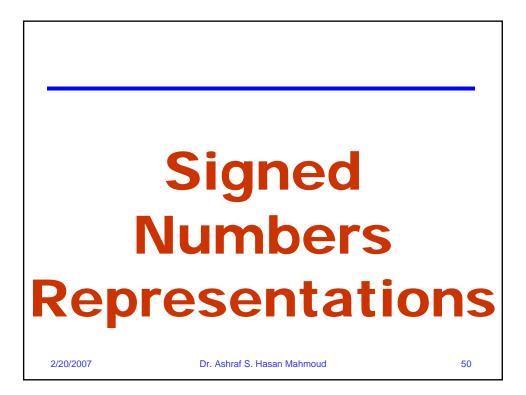


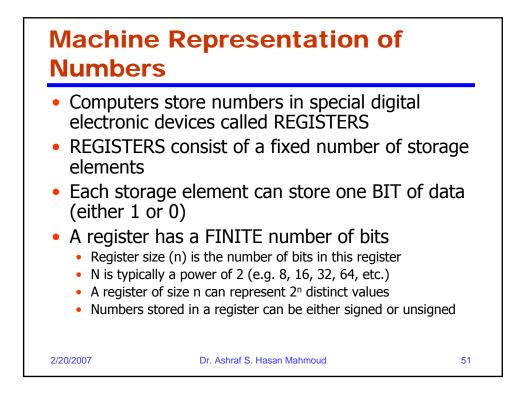


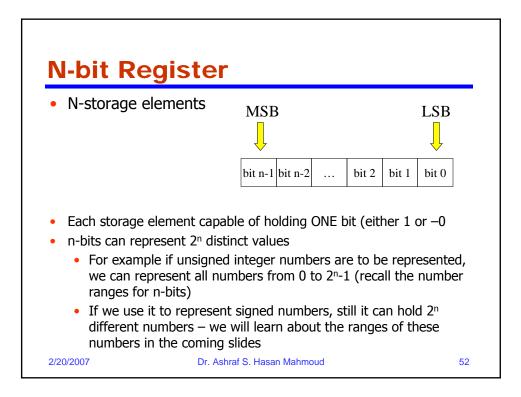


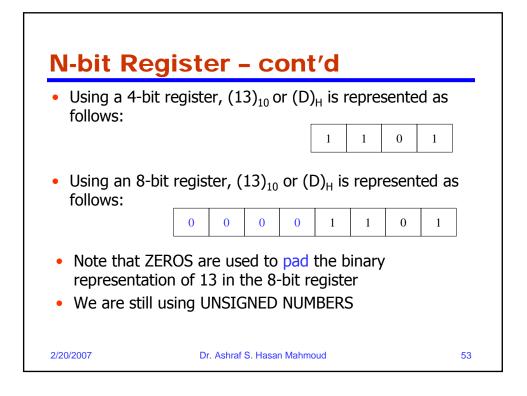
Ini	co														
Unico	ode de	scribe	<u>а</u> са	16	-hi	t ct	andar	d cod	a for r	onroc	ont	ina	cvr	nhc	١c
and i	deogra	anhc	for t	-10 hba		vrld	'e lan			epies	ent	ing	Syı	noc	15
	-	-		une	vvc	лu	5 1011	Juage	5.						
First 25	6 Codes fo	r Unicod	ya.												
Co	ntrol			AS	CI			Co	ntrol			Latir	n 1		
000	001	002	003	004	005	006	007	008	009	00A	00B	00C	00D	00E	00F
0 CTRL	CTRL	SPACE	0	@	Р		D	CTRL	CTRL	NB SP	0	À	Ð	à	D
I CTRL	CTRL	· · · · ·	1	A	Q	а	r q	CTRL	CTRL		±	Á	Ñ	á	ñ
2 CTRL	CTRL		2	В	R	Ь	г	CTRL	CTRL	ć	2	Â	Ò	â	ò
3 CTRL	CTRL	#	3	С	S	с	S	CTRL	CTRL	£	3	Ã	Ó	ã	ó
4 CTRL	CTRL	SS	4	D	Т	d	t	CTRL	CTRL	п	<i>,</i>	Ä	Ô	ä	ô
5 CTRL	CTRL	%	5	Е	U	е	u	CTRL	CTRL	¥¥	μ	Å	Õ	å	õ
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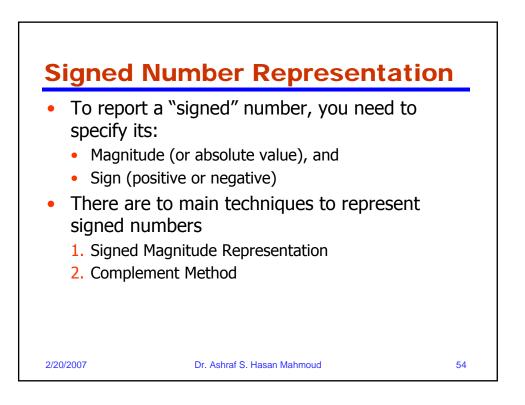


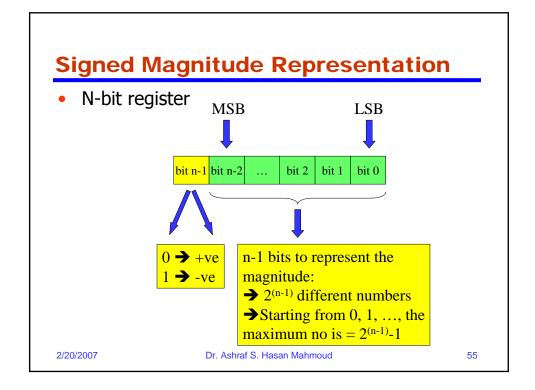


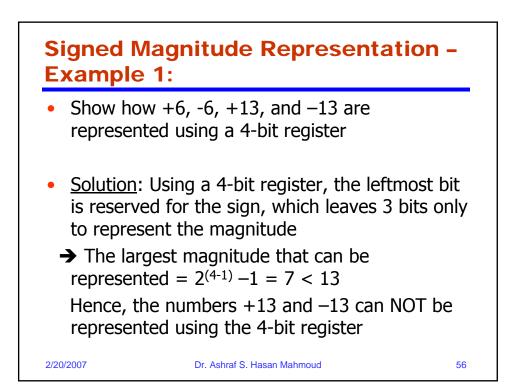


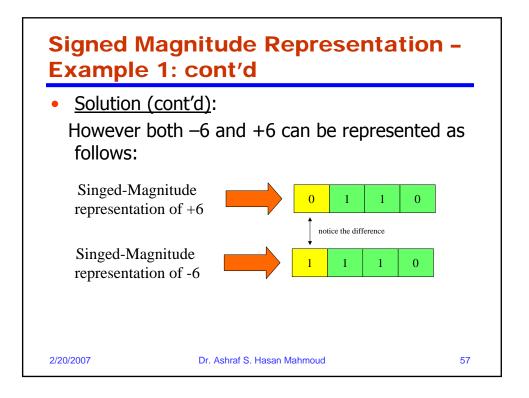


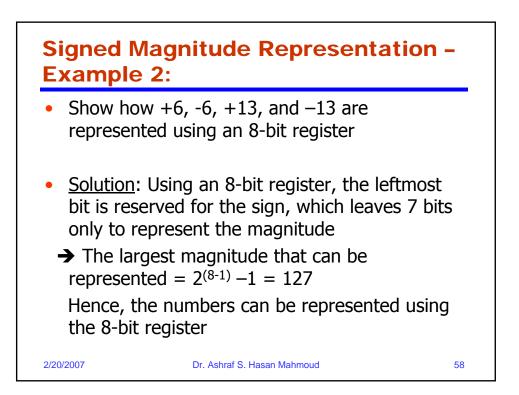


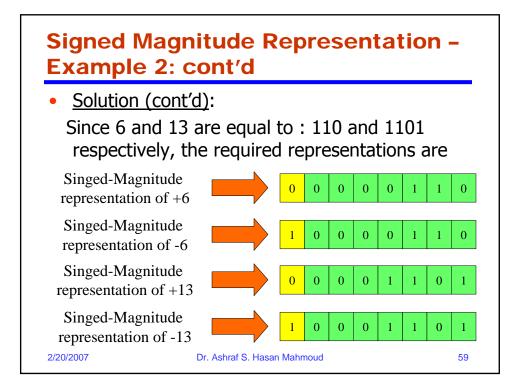


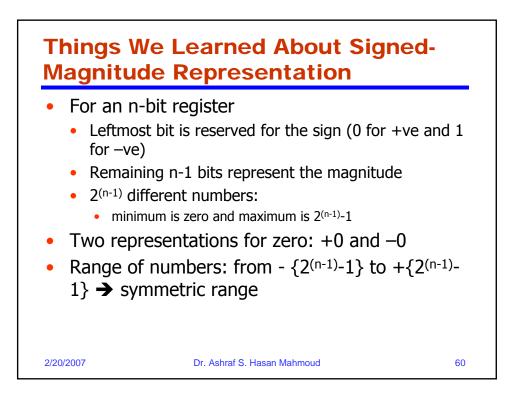


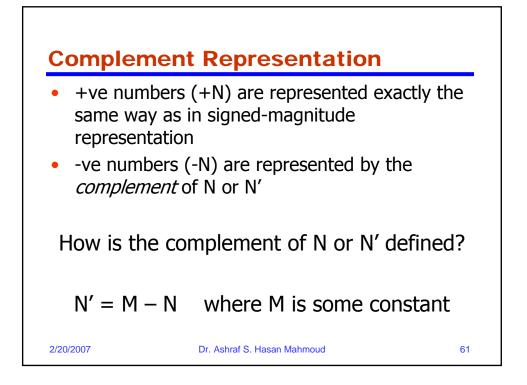


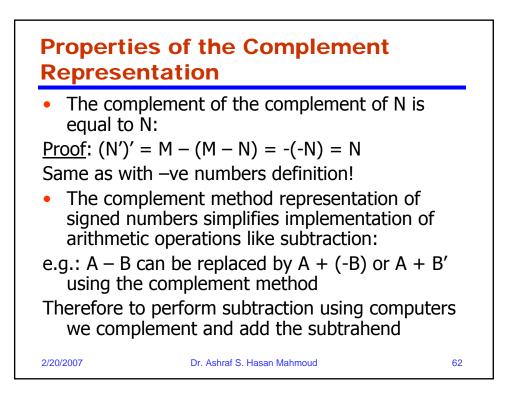


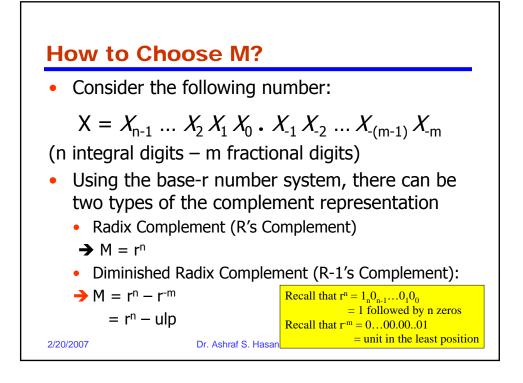


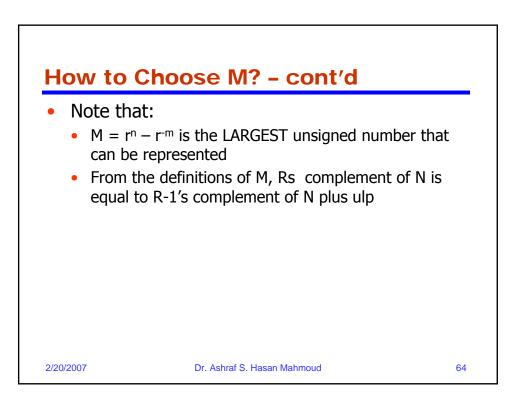






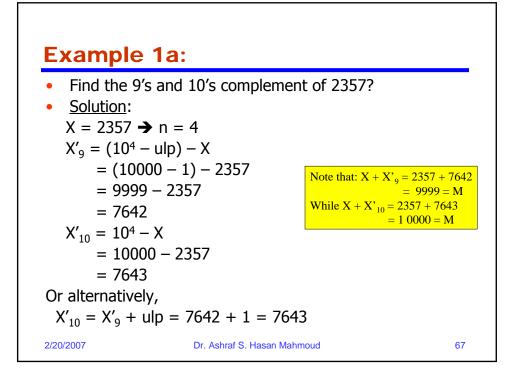


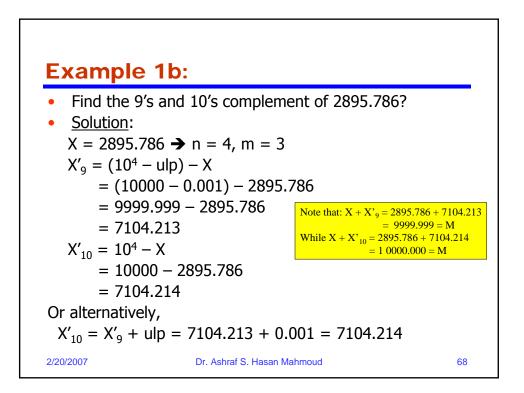


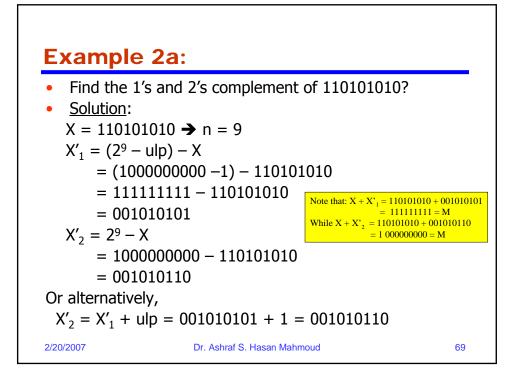


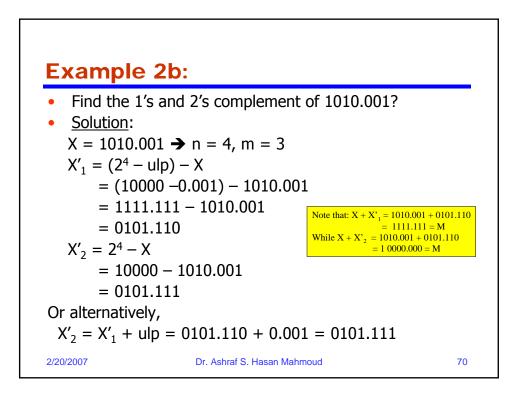
R's Complement:						
Number System	R's Complement	Complement of X				
Decimal	10's Complement	$X'_{10} = 10^n - X$				
Binary	2's Complement	$X'_{2} = 2^{n} - X$				
Octal	8's Complement	$X'_{8} = 8^{n} - X$				
Hexadecimal	16's Complement	$X'_{16} = 16^{n} - X$				

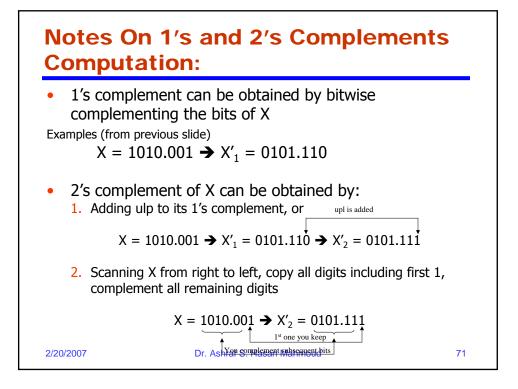
cont'd	Summary of Complement Method – cont'd R-1's Complement:									
Number System	R-1's Complement	Complement of X								
Decimal	9's Complement	$X'_{9} = (10^{n} - 10^{-m}) - X$ = 9999.9999 - X								
Binary	1's Complement	$X'_{1} = (2^{n}-2^{-m}) - X$ = 1111.1111 - X								
Octal	7's Complement	$X'_7 = (8^n - 8^{-m}) - X$ = 7777.7777 - X								
Hexadecimal	$X'_{-} = (16^{n} - 16^{-m}) - X$									
2/20/2007										

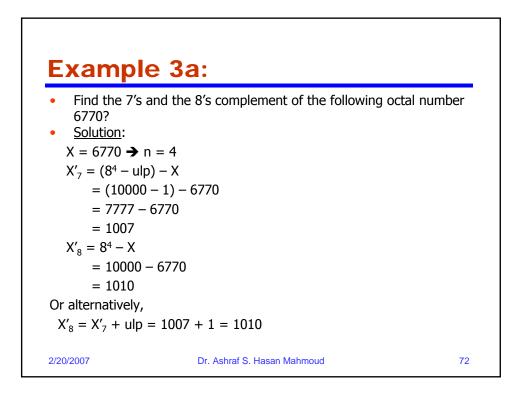


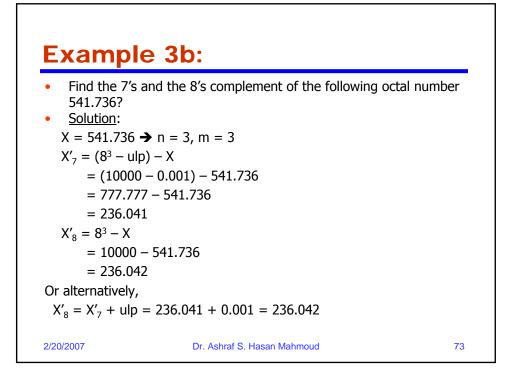


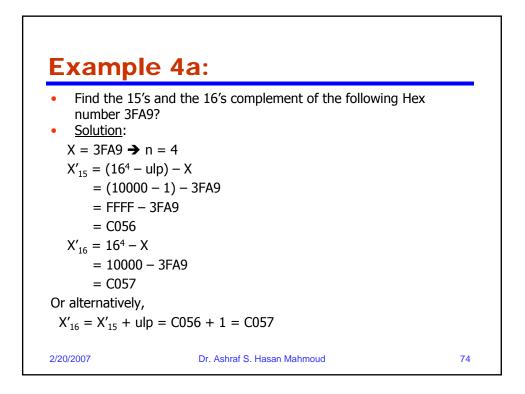


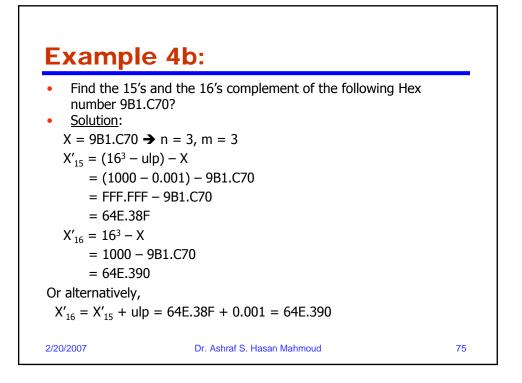


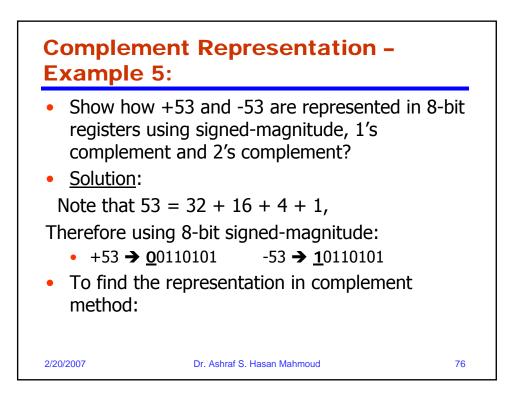


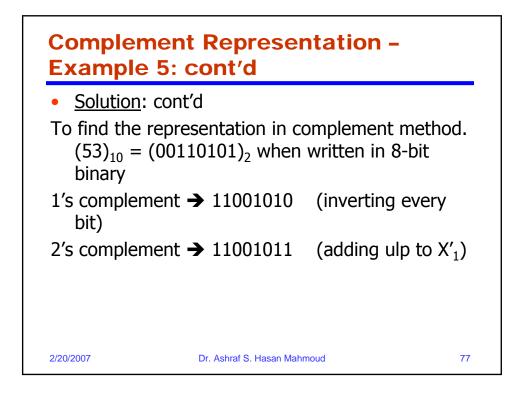


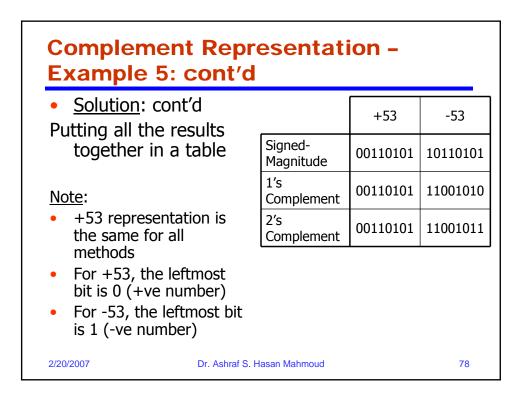


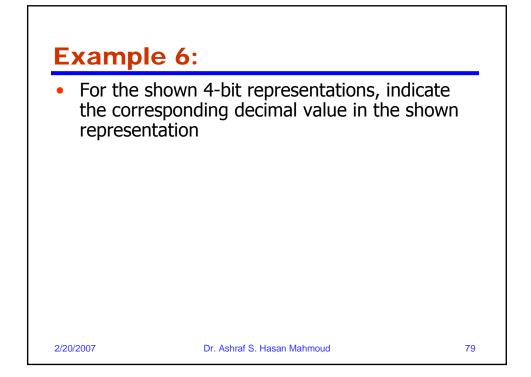






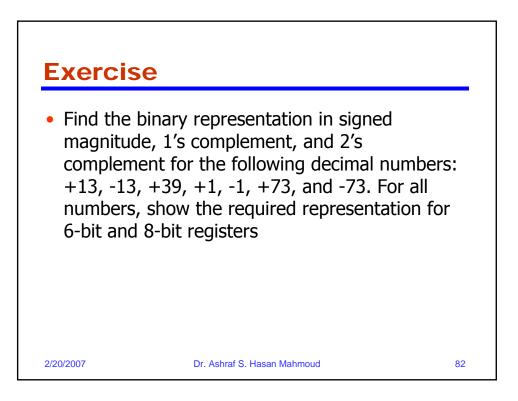






Example 6	· co	nt'd			
		int d			
Signed-Magnitude					
and 1's complement		Unsigned	Signed- Magnitude	1's Complement	2's Complement
are symmetrical	0000	0	0	0	0
representations with TWO representations	0001	1	1	1	1
for ZERO	0010	2	2	2	2
	0011	3	3	3	3
 Range from signed- magnitude and 1's 	0100	4	4	4	4
complement is from -	0101	5	5	5	5
7 to +7	0110	6	6	6	6
 2's complement 	0111	7	7	7	7
representation is not	1000	8	-0	-7	-8
symmetrical	1001	9	-1	-6	-7
Range for 2's	1010	10	-2	-5	-6
complement is from - 8 to +7 – with one	1011	11	-3	-4	-5
representation for	1100	12	-4	-3	-4
ZFRO	1101	13	-5	-2	-3
ZEIG	1110	14	· · · · · · · · · · · · · · · · · · ·	-2	
	1111	15	-7	-0	-1

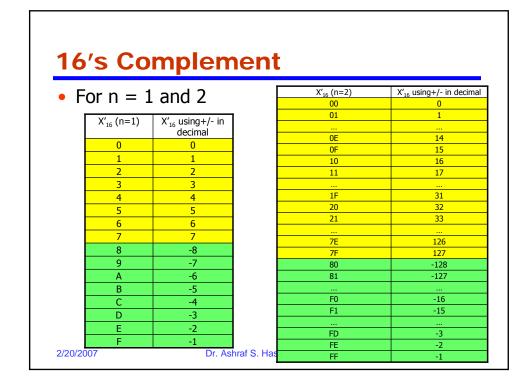
• Th			izes the prope d number rep	
		Signed- Magnitude	1's Complement	2's Complement
	Symmetric	Y	Y	Ν
	No of Zeros	2	2	1
	Largest	2 ⁽ⁿ⁻¹⁾ -1	2 ⁽ⁿ⁻¹⁾ -1	2 ⁽ⁿ⁻¹⁾ -1
	Smallest	-{2 ⁽ⁿ⁻¹⁾ -1}	-{2 ⁽ⁿ⁻¹⁾ -1}	-2 ⁽ⁿ⁻¹⁾
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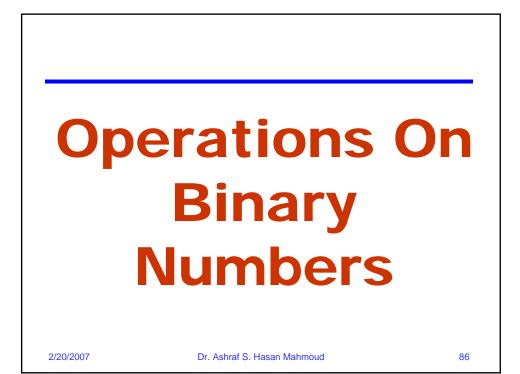


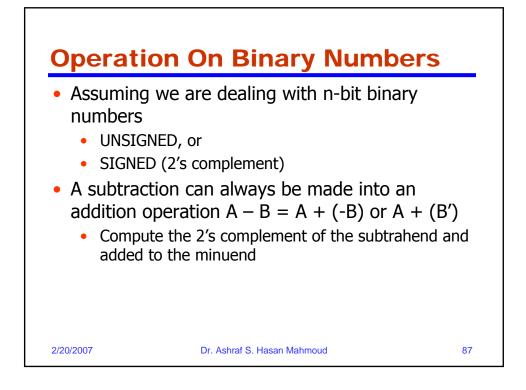
For $n =$	1 and 2	X′ ₁₀ (n=2)	X' ₁₀ using+/- in decimal
		00	0
X' ₁₀ (n=1)	X' ₁₀ using+/-	01	1
-	in decimal	02	2
0	0		
1	1	09	9
		10	10
2	2	11	11
3	3	12	12
4	4		
5	-5	49	49
		50	-50
6	-4	51	-49
7	-3	52	-48
8	-2		
9	-1	<u>98</u> 99	-2

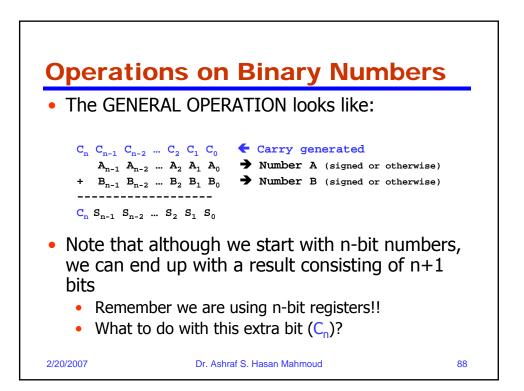
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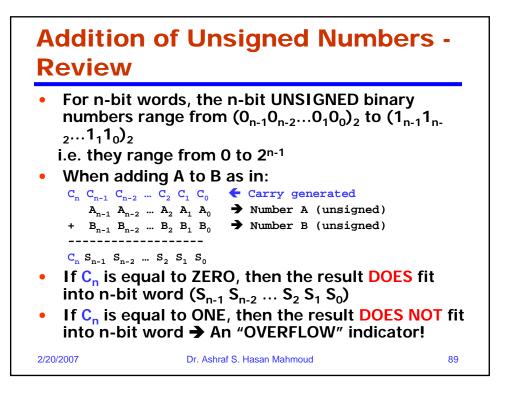
B's Cor	nplem	ent		
For $n = 1$ and 2		X′ ₈ (n=2)	X' ₈ using+/- in decimal	
			00	0
$V'_{(n-1)}$	V/ using /	1 L	01	1
X' ₈ (n=1)	X' ₈ using+/-		02	2
	in decimal			<u>.</u>
0	0	-	07	7
1	1		<u> </u>	8
2	2		11	10
3	3		36	30
4	-4		37	31
			40	-32
5	-3		41	-31
6	-2			
7	-1		70	-8
	-1	I [71	-7
		_		
/20/2007	_	Ashraf S. H	<u> </u>	-2 -1

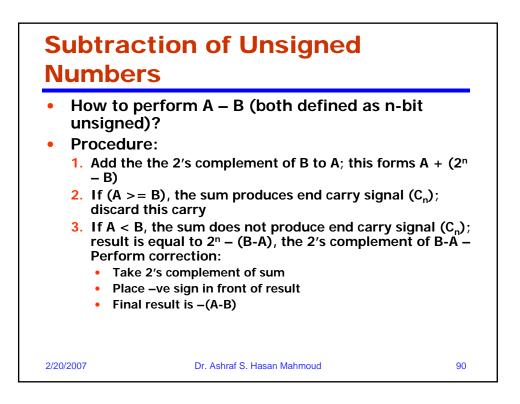


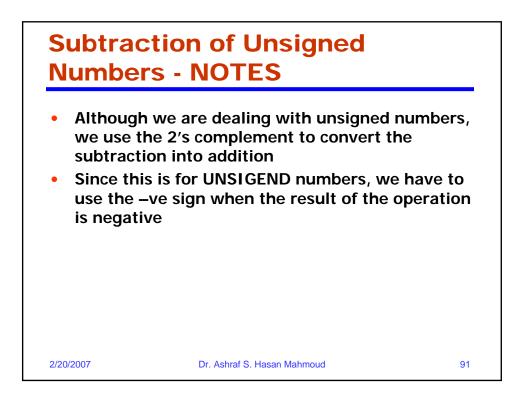


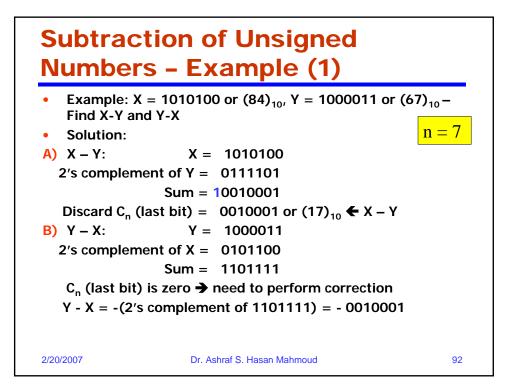












Subtraction of Unsigned Numbers – Example (2) – Base 10

• Example: X = (72532)₁₀, Y = (3250)₁₀ – Find X-Y and Y-X • Solution: A) X – Y: X = 7253210's complement of Y = 96750 Sum = 169282 Discard C_n (last bit) = $(69282)_{10} \leftarrow X - Y$ **B)** Y – X: Y = 3250 10's complement of X = 27468Sum = 30718 C_n (last bit) is zero \rightarrow need to perform correction Y - X = -(10's complement of 30718) = - 69282 The same procedure can be used for any base R system. 2/20/2007 Dr. Ashraf S. Hasan Mahmoud 93

