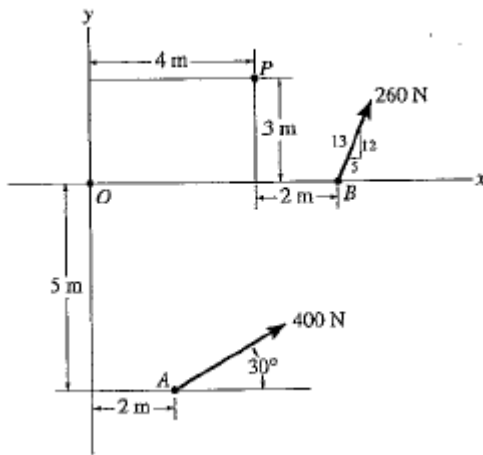


CIVIL ENGINEERING DEPARTEMENT - KFUPM.  
CE 202 Statics and Strength of Materials

First Semester: '101 Instructor: Dr. Salah Al-Dulaijan

HOME WORK ASSIGNMENT NO. 2 SOLUTION

1. Determine the magnitude and directional sense of the resultant moment of the forces about point P.



**Solution:**

Sign convention: All clockwise moments are +ve, and counterclockwise moments are -ve

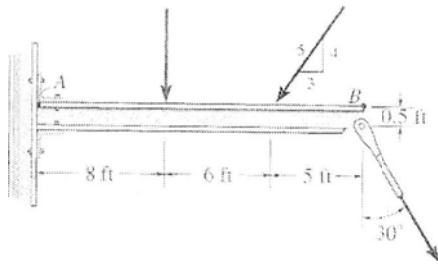
$$\begin{aligned} M_{P} \mathcal{F}_y &= -260(12/13)(2) + 400\sin 30^\circ(2) \\ &= 480 + 400 \\ &= -80 \text{ Nm} \end{aligned}$$

$$\begin{aligned} M_{P} \mathcal{F}_x &= -260(5/13)(3) - 400\cos 30^\circ(8) \\ &= -300 - 2771.28 \text{ Nm} \\ &= -3071.28 \text{ Nm} \end{aligned}$$

$$M_P = M_{P} \mathcal{F}_x + M_{P} \mathcal{F}_y = -80 \text{ Nm} - 3071.28 \text{ Nm} = -3151.28 \text{ Nm}$$

Therefore the magnitude of the resultant moment of the forces about point P is 3151.28 Nm, and directional sense is counterclockwise

2. Determine the moment about point B of each of the three forces acting on the beam.

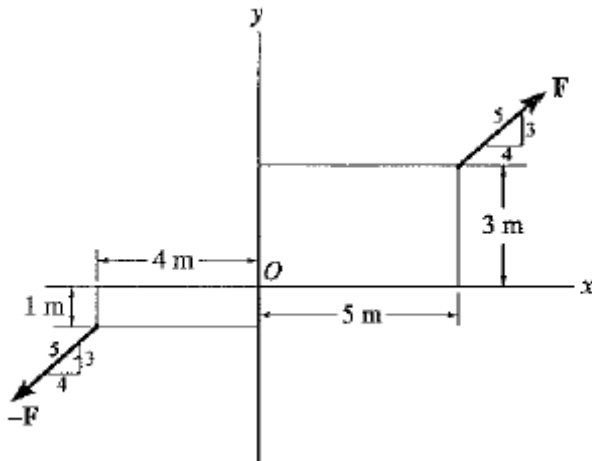


**Solution:**

Sign convention: All clockwise moments are +ve, and counterclockwise moments are -ve

$$\begin{aligned}
 f_1: M_{Bf_1} &= -375 \times 11 = -4125 \text{ lb.ft} \\
 f_2: M_{Bf_2} &= -500 \times \left(\frac{4}{5}\right) \times 5 = -2000 \text{ lb.ft} \\
 f_3: M_{Bf_3} &= -160 \times \sin(30^\circ) \times 0.5 = -40 \text{ lb.ft}
 \end{aligned}$$

3. Determine the magnitude and sense of the couple moment. Each force has a magnitude of  $F = 8 \text{ kN}$ .



**Solution:**

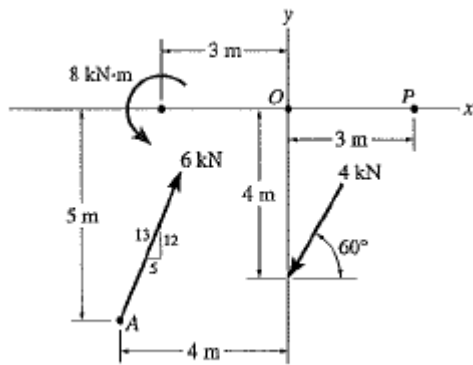
Sign convention: All clockwise moments are +ve, and counterclockwise moments are -ve

$$\begin{aligned}
 f_1: M_{O_f1x} &= 8 \times \left(\frac{4}{5}\right) \times 3 = 19.2 \text{ kNm} \\
 M_{O_f1y} &= -8 \times \left(\frac{3}{5}\right) \times 5 = -24.0 \text{ kNm} \\
 f_2: M_{O_f2x} &= 8 \times \left(\frac{4}{5}\right) \times 1 = 6.4 \text{ kNm} \\
 M_{O_f2y} &= -8 \times \left(\frac{3}{5}\right) \times 4 = -19.2 \text{ kNm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Total Moment, } M_O &= M_{O_f1x} + M_{O_f1y} + M_{O_f2x} + M_{O_f2y} \\
 &= 19.2 - 24.0 + 6.4 - 19.2 \\
 &= -17.6 \text{ kNm}
 \end{aligned}$$

Therefore the couple moment has a magnitude of 17.6 Nm, and produces a counterclockwise moment about point O

4. Replace the force and couple system by an equivalent force and couple moment at point O.



**Solution:**

Sign convention: All clockwise moments are +ve, and counterclockwise moments are -ve

$$M_1: M_{O M_1} = -8 \text{ kNm}$$

$$F_1: M_{O F_{1x}} = -6 \times \left(\frac{5}{13}\right) \times 5 = -150/13 \text{ kNm}$$

$$M_{O F_{1y}} = +6 \times \left(\frac{12}{13}\right) \times 4 = +288/13 \text{ kNm}$$

$$F_2: M_{O F_{2x}} = +4 \times \cos(60^\circ) \times 4 = 8 \text{ kNm}$$

$$M_{O F_{2y}} = +4 \times \sin(60^\circ) \times 0 = 0 \text{ kNm}$$

$$\text{Total moment about O, } M_O = M_{O M_1} + M_{O F_{1x}} + M_{O F_{1y}} + M_{O F_{2x}} + M_{O F_{2y}}$$

$$= 8 + 150/13 - 288/13 + 8$$

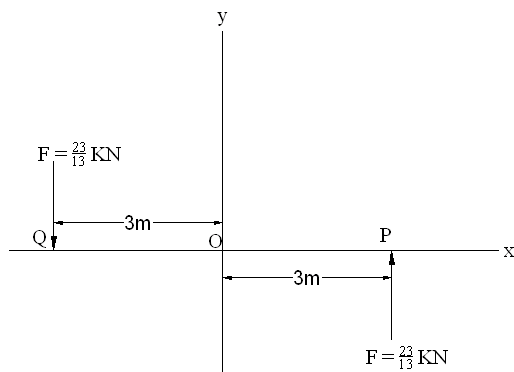
$$= -138/13 \text{ kNm, } = 10.6154 \text{ kNm.}$$

Therefore we need to provide couple forces F, d metres apart that will create a counterclockwise moment about O. Lets choose points P & Q along the line PQ, then

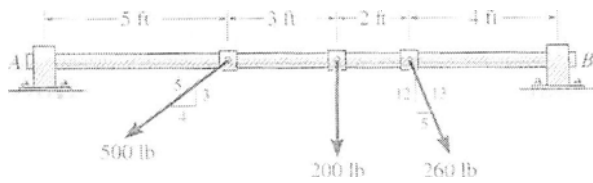
$$d = PQ = 6\text{m}$$

$$F = M_O / d = 138 / (13 \times 6) = 23/13 \text{ kN} = 1.7692 \text{ kN}$$

The couple will need to be such that will produce a counterclockwise moment as illustrated below



5. Replace the three forces acting on the shaft by a single resultant force. Specify where the force acts, measured from point B.



**Solution:**

Sign convention: All clockwise moments are +ve, and counterclockwise moments are -ve

**Total vertical force,  $\sum F_y = -500 \times (3/5) - 200 - 260 \times (12/13) = -740 \text{ lb}$**

**Total horizontal force,  $\sum F_x = -500 \times (4/5) + 260 \times (5/13) = -300 \text{ lb}$**

**$F_R = \sqrt{(\sum F_x)^2 + (\sum F_y)^2} = \sqrt{300^2 + 740^2} = 798.5 \text{ lb}$**

**$\theta = \tan^{-1}(740/300) = 67.9^\circ \text{ to the -ve x-axis,}$**

Take Moment about any point on the system, say B

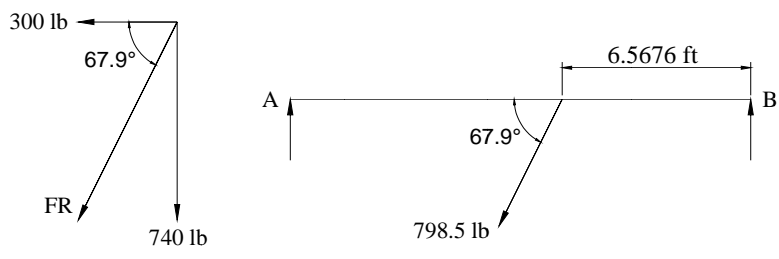
Moment about B is produced only by  $F_y$ , thus

**$\sum M_B = -500 \times (3/5) \times 9 - 200 \times 6 - 260 \times (12/13) \times 4 = -4860 \text{ lb.ft}$**

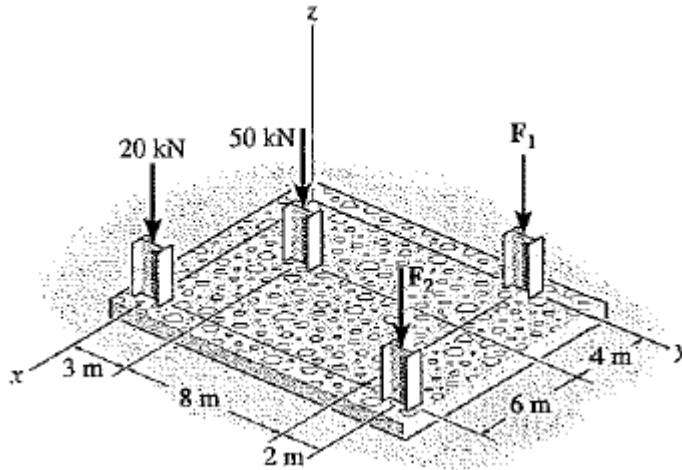
The total moment of all the vertical components of the forces is the same by the moment of the vertical component of the resultant of the forces. Thus

**$\sum F_y \times d = -4860 \text{ lb.ft}$**

**$-740d = -4860 \text{ lb.ft} \implies d = 243/37 \text{ ft} = 6.5676 \text{ ft from end B of the shaft.}$**



6. The building slab is subjected to four parallel column loadings. Determine the equivalent resultant force and specify its location (x,y) on the slab. Take  $F_1 = 20 \text{ kN}$ ,  $F_2 = 50 \text{ kN}$ .



**Total force/force resultant,  $f_z = -20 - 50 - 20 - 50 = -140 \text{ kN}$ , meaning  $140 \text{ kN}$  downward**

**Moment about x - axis,  $M_x = 20(0) + 50(3) + 20(11) + 50(13) = 1020 \text{ kNm}$**

**Moment about y - axis,  $M_y = 20(10) + 50(4) + 20(0) + 50(10) = 900 \text{ kNm}$**

**Load centre along x, represented by  $\mathcal{X}$  is given by**

$$M_y = f_z \times \mathcal{X} \Rightarrow \mathcal{X} = M_y / f_z$$

$$\mathcal{X} = M_y / f_z = 900 / 140 = 45/7 = 6.4286 \text{ m}$$

**Similarly,**

$$\mathcal{Y} = M_x / f_z = 1020 / 140 = 51/7 = 7.2857 \text{ m}$$

Therefore, the equivalent resultant force =  $140 \text{ kN}$  (downward) and its location (x,y) relative to the origin is  $(6.4286 \text{ m}, 7.2857 \text{ m})$