

King Fahd University of Petroleum and Minerals

Prep-Year Math Program

Math 002 - Term 151

Recitation (7.6 and 7.7)

**Question 1:** Solve the following equations

a)  $\sin \frac{x}{2} + \cos x = 1$ , for  $0 \leq x \leq \pi$ .

b)  $\sin 2x + \sin x - 2 \cos x - 1 = 0$ , where  $0 \leq x < 2\pi$

c)  $\tan \frac{x}{2} = 1 - \cos x$ , where  $0 \leq x < 2\pi$ .

**Answer:** (a):  $SS = \left\{0, \frac{\pi}{3}\right\}$       (b):  $SS = \left\{\frac{\pi}{2}, \frac{2\pi}{3}, \frac{4\pi}{3}\right\}$       (c):  $SS = \left\{0, \frac{\pi}{2}\right\}$

**Question 2:** Solve the equations:  $\arcsin 2x + \arccos x = \frac{\pi}{2}$

**Answer:**  $SS = \{0\}$

**Question 3**

The sum of all solutions of the equation  $-2 \cos 2x \sin 3x + 2 \cos 3x \sin 2x = \sqrt{3}$  in the interval  $[-\pi, \pi]$  is:

A)  $-\frac{4\pi}{3}$

B)  $-\frac{2\pi}{3}$

C)  $\frac{\pi}{3}$

D)  $-\pi$

E)  $\frac{2\pi}{3}$

**Question 4:** If  $\cos^{-1} x - \tan^{-1} \sqrt{3} = \sin^{-1} \frac{1}{3}$ , then  $x =$

A)  $\frac{2\sqrt{2} + \sqrt{3}}{6}$

B)  $\frac{2\sqrt{2} + 1}{6}$

C)  $\frac{4 + \sqrt{2}}{6}$

D)  $\frac{2\sqrt{2} - 1}{6}$

E)  $\frac{2\sqrt{2} - \sqrt{3}}{6}$