

King Fahd University of Petroleum and Minerals
Prep-Year Math Program
Math (001)-Term (131)
Recitation (R1 and R2)
Answered by Sayed Omar

Question 1: Given the following numbers:

$$-1, 0, 1, 2, -91, 2.12122123\dots, \frac{22}{7}, -41, 2.2\bar{3}, \pi, \frac{\sqrt{2}}{3}, \frac{\sqrt{81}}{3}, 3.14, \frac{12.1}{1.1}$$

Complete the following:

Integers: _____

Rational Numbers: _____

Non-Integer Rational Numbers: _____

Non-Negative Integer Numbers: _____

Irrational Numbers: _____

Answer:

Integers: $-1, 0, 1, 2, -91, -41, \frac{\sqrt{81}}{3}, \frac{12.1}{1.1}$

Rational Numbers: $-1, 0, 1, 2, -91, \frac{22}{7}, -41, 2.2\bar{3}, \frac{\sqrt{81}}{3}, 3.14, \frac{12.1}{1.1}$

Non-Integer Rational Numbers: $\frac{22}{7}, 2.2\bar{3}, 3.14$

Non-Negative Integer Numbers: $0, 1, 2, \frac{\sqrt{81}}{3} = 3, \frac{12.1}{1.1} = 11$

Irrational Numbers: $2.12122123\dots, \pi, \frac{\sqrt{2}}{3}$

Question 2:

Let U be the universal set, where: $U = \{x \mid x \text{ is a whole number less than } 11\}$ and

$$A = \{x \mid x \text{ is an even natural number } \leq 8\}$$

$$B = \{2, 4, 5, 8, 10\}$$

$$C = \{1, 2, 4, 5, 7, 8\}$$

i. Find: $(A \cap B)' =$ $B' \cup C' =$

ii. Answer the following as TRUE or FALSE?

Answer:

(i): $(A \cap B)' = \{0, 1, 3, 5, 6, 7, 9, 10\}$ $B' \cup C' = \{0, 1, 3, 6, 7, 9, 10\}$

Answer: (ii):

- a) $A' = \{0,1,3,5,7,9,10\}$ **TRUE**
- b) $\emptyset \in U$ **FALSE**
- c) $\{0\} \subseteq A$ **FALSE**
- d) $\emptyset \subseteq U$ **TRUE**
- e) $A \cup B' = \{0,1,2,5,6\}$ **FALSE**
- f) $(A \cap B)' = B' \cup C'$ **FALSE**

Question 3:

If $x = 3 \cdot 4^2 + |-7| - 3^4 \div 9$, $y = 35 - 20 \div 5 \times 2 - 6 \times 3$ and $z = 6 - 4 \div 2 + 45$, then find the value of the expression: $x - 2[y \div (z - x)]$

Answer: $x - 2[y \div (z - x)] = 40$

Question 4: TRUE or FALSE

- 1) The operation of division of real numbers is associative. **FALSE**
- 2) $\frac{2x + w}{x + 3y} = \frac{2 + w}{1 + 3y}$ **FALSE**
- 3) If x is any real number, then $|-x - 1| = x + 1$. **FALSE**
- 4) If x is any real number, then $|-x - y| = |x + y|$. **TRUE**
- 5) $2(x + 2)\left(x - \frac{1}{2}\right) = (x + 2)(2x - 1)$ **TRUE**
- 6) Any integer number is either positive or negative. **FALSE**

Question 5:

a) If $x < 0$, then $|x| + |-x| + x =$

A) $3x$

B) $-2x$

C) x

D) $-x$

E) $-3x$

b) If $-3 < x < -2$, then $|-3x| + \sqrt{(x-3)^2} + 2|x+1| =$

A) $1 - 6x$

B) $4x + 1$

D) $5 - 2x$

E) 1

Question 6: Let $A = \{y \mid y = x - |x|, \text{ where } x \text{ is an integer } -4 < x \leq 0\}$ and $B = \{-6, -4, -2, -1, 0\}$, then $A \cap B =$

A) $\{-4, -2\}$

B) A

C) \emptyset (the empty set)

D) $A \cup B$

E) B