

Show all necessary steps for full marks.

Q1. (5 points) (2.6 Exercise 27): **Graph** the piecewise-defined function.

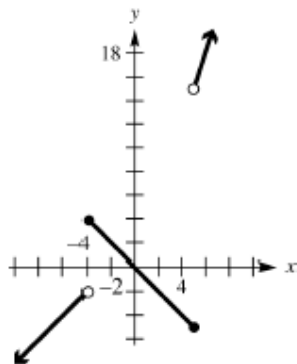
(a): Find the range.

(b): Determine the intervals where the function is decreasing.

(c): Determine the interval where the function is increasing.

$$f(x) = \begin{cases} 2+x & \text{if } x < -4 \\ -x & \text{if } -4 \leq x \leq 5 \\ 3x & \text{if } x > 5 \end{cases}$$

Solution:



(a): Range = $(-\infty, 4] \cup (15, \infty)$

(b): The function is decreasing on $[-4, 5]$

(c): The function is increasing on $(-\infty, -4)$ and $(5, \infty)$

Q2. (5 points) (Recitation 2.6) If $f(x) = \left\lfloor 1 - \frac{x}{2} \right\rfloor$, sketch the graph of $f(x)$ and find

a) x - and y - intercepts

b) $f(-2.4) + f(2.006)$

Solution: $n = \left\lfloor 1 - \frac{x}{2} \right\rfloor$

$$n \leq 1 - \frac{x}{2} < n + 1$$

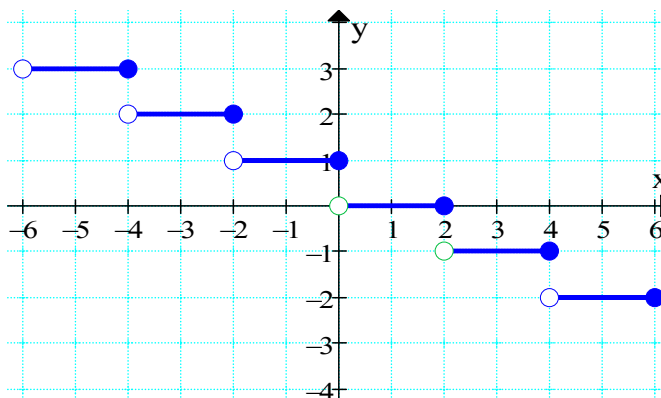
$$2n \leq 2 - x < 2n + 2$$

$$2n - 2 \leq -x < 2n$$

$$-2n + 2 \geq x > -2n$$

$$-2n < x \leq -2n + 2$$

n	$-2n < x \leq -2n + 2$	$f(x) = \left\lfloor 1 - \frac{x}{2} \right\rfloor$
-2	$4 < x \leq 6$	-2
-1	$2 < x \leq 4$	-1
0	$0 < x \leq 2$	0
1	$-2 < x \leq 0$	1



(a): x - int: $\{x \mid 0 < x \leq 2\}$

y - int: $y = 1$

(b): $f(-2.4) + f(2.006) = ?$

$$f(-2.4) = \left\lfloor 1 - \frac{-2.4}{2} \right\rfloor = \left\lfloor \frac{2+2.4}{2} \right\rfloor = \left\lfloor \frac{4.4}{2} \right\rfloor = \lfloor 2.2 \rfloor = 2$$

$$f(2.006) = \left\lfloor 1 - \frac{2.006}{2} \right\rfloor = \left\lfloor \frac{2-2.006}{2} \right\rfloor = \left\lfloor \frac{-0.006}{2} \right\rfloor = \lfloor -0.003 \rfloor = -1$$

$$f(-2.4) + f(2.006) = 2 - 1 = 1$$

Q3. (5 points) (Recitation 2.7 Q#3) Determine which of the following functions are even, odd, or neither.

a) $f(x) = \frac{2x}{3x - x^5}$

b) $f(x) = x^4 - 5x + 8$

c) $f(x) = x^2 + |x| + 4$

Solution: (a) $f(-x) = \frac{2(-x)}{3(-x) - (-x)^5} = \frac{-2x}{-3x + x^5} = \frac{-1}{-1} \cdot \frac{-2x}{-3x + x^5} = \frac{2x}{3x - x^5} = f(x)$

$\Rightarrow f$ is an even function.

b) $f(-x) = (-x)^4 - 5(-x) + 8 = x^4 + 5x + 8 \neq f(x)$ and $\neq -f(x) \Rightarrow f$ is neither even nor odd.

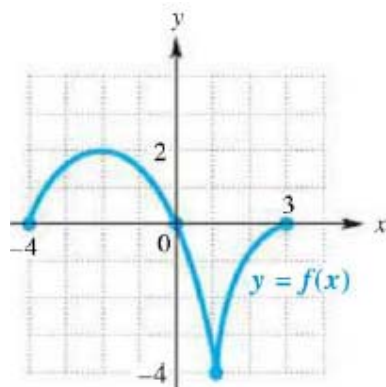
c) $f(-x) = (-x)^2 + |-x| + 4 = x^2 + |x| + 4 = f(x) \Rightarrow f$ is an even function.

Q4. (5 points) (2.7Example 9): A graph of a function defined by $y = f(x)$ is shown in adjacent figure. Use this graph to sketch each of the following graphs.

(a): $g(x) = f(x) + 3$

(b): $h(x) = f(x + 3)$

(c): $k(x) = f(x - 2) + 3$



Solution:

