

# Ayman Ghannam

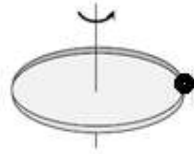
## Chapter 10

### Rotation



- Q.1 What is the angular speed in radians per second of the Earth in its orbit about the Sun. ( $\omega = 1.99 \times 10^{-7}$  rad/s)
- Q.2 Calculate the required time for a wheel, initially at rest, to turn through 10 full revolutions if it can accelerate at a rate of  $1\pi$  rad/s<sup>2</sup>.  $t = 6.3$  s
- Q.3 A wheel spins at a rate of 30 revs/sec comes to a complete stop in 10 seconds. Find:
- the angular acceleration of the wheel.  $-6\pi$  rad/s<sup>2</sup>
  - the number of revolutions the wheel undergoes before it comes to a stop.  $300\pi$  rad

- Q.4 The angular position of a point on the rim of a rotating wheel is given by  $\theta(t) = 4.0t - 3.0t^2 + t^3$ , where  $\theta$  is in radians if  $t$  is given in seconds.
- What are the angular velocities at  $t = 2.0$  s and  $t = 4.0$  s?  $4$  rad/s ---  $28$  rad/s
  - What is the average angular acceleration for the time interval that begins at  $t = 2.0$  s and ends at  $t = 4.0$  s?  $12$  rad/s<sup>2</sup>
  - What are the instantaneous angular accelerations at the beginning and end of this time interval?  $6$  rad/s<sup>2</sup> ---  $18$  rad/s<sup>2</sup>



- Q.5 The angular position of a point on the rim of a rotating wheel is given by  $\theta(t) = -1.00 - 0.600t + 0.250t^2$ , where  $\theta$  is in radians if  $t$  is given in seconds. What theta at time  $t_{\min}$

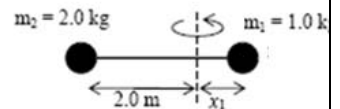
H.W. At what time,  $t_{\min}$ , does  $\theta(t)$  reach the minimum value? What is  $\theta(t)$  at  $t_{\min}$ ?  
**Answer:** Calculate  $\omega(t) = 0$  to find  $t_{\min} = 1.20$  s, and  $\theta(t_{\min}) = -1.36$  rad  $\approx -77.9^\circ$

- Q.6 An electric motor rotating a grinding wheel at 100 rev/min is switched off. Assuming constant negative angular acceleration of magnitude  $2.00$  rad/s<sup>2</sup>, (a) How long does it take the wheel to stop?  $5.24$  s  
 (b) Through how many radians does it turn during the time found in (a)?  $27.5$  rad
- Q.7 A disk, of radius  $6.0$  cm, is free to rotate at a constant rate of  $1200$  rpm about its axis. Find:
- the radial acceleration
  - the tangential acceleration.  $948$  m/s<sup>2</sup> ---  $0$
- Q.8 A disk—a horizontal rotating platform—of radius  $r$  is initially at rest, and then begins to accelerate constantly until it has reached an angular velocity  $\omega$  after 2 complete revolutions. What is the angular acceleration of the disk during this time?  $\omega^2/8\pi$
- Q.9. A racing car travels on a circular track of radius  $275$  m. Suppose the car moves with a constant linear speed of  $51.5$  m/s. a) Find its angular speed.  $0.19$  rad/s  
 b) Find the magnitude and direction of its acceleration.  $a_t = 0$  ---  $a_r = 9.645$  m/s<sup>2</sup>
- Q.10 A wheel  $1.65$  m in diameter lies in a vertical plane and rotates about its central axis with a constant angular acceleration of  $3.70$  rad/s<sup>2</sup>. The wheel starts at rest at  $t = 0$ , and the radius vector of a certain point P on the rim makes an angle of  $57.3^\circ$  with the horizontal at this time. At  $t = 2.00$  s, find the following:
- the angular speed of the wheel.  $7.4$  rad/s
  - the tangential speed of the point P.  $6.11$  m/s
  - the total acceleration of the point P.  $45.28$  rad/s<sup>2</sup> ---  $3.86^\circ$
  - the angular position of the point P.  $8.4$  rad
- Q.11 Calculate the rotational inertia of a wheel that has a kinetic energy of  $24400$  J when rotating at  $\omega = 602$  revs/min.  $12.3$  kg.m<sup>2</sup>

- Q.12 As shown in the figure, three masses, of  $1.5$  kg each, are fastened at fixed position to a very light rod pivoted at one end. Find the moment of inertia for the rotation axes shown.  $21$  kg.m<sup>2</sup>

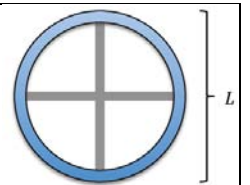


- Q.13 A rigid body consists of two particles attached to a rod of negligible mass. The rotational inertia of the system about the axis shown in Figure is  $10$  kg m<sup>2</sup>. What is  $x_1$ ?  $1.14$  m

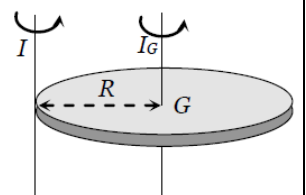


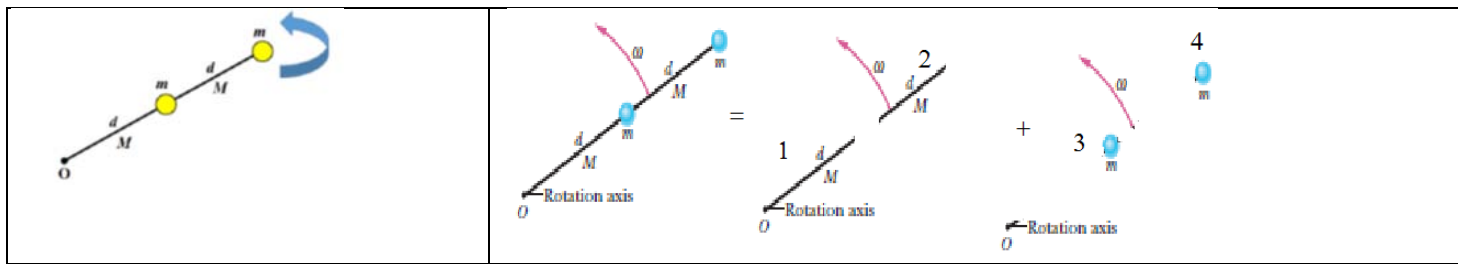
- Q.14 A hoop rolls without sliding on a horizontal floor. The ratio of its translational kinetic energy to its rotational kinetic energy (about its central axis) is.  $1$

- Q.15 A pair of long, thin, rods, each of length  $L$  and mass  $M$ , are connected to a hoop of mass  $M$  and radius  $L/2$  to form a 4-spoked wheel as shown in the figure. Express all answers in terms of the given variables and fundamental constants. Calculate the moment of inertia for the entire spoked-wheel assembly for an axis of rotation through the center of the assembly and perpendicular to the plane of the wheel.  $15/12 ML^2$
- Answer:** The moment of inertia for the spoked wheel is simply the sum of the individual moments of inertia of its three components: the two long thin rods and the hoop around the outside:



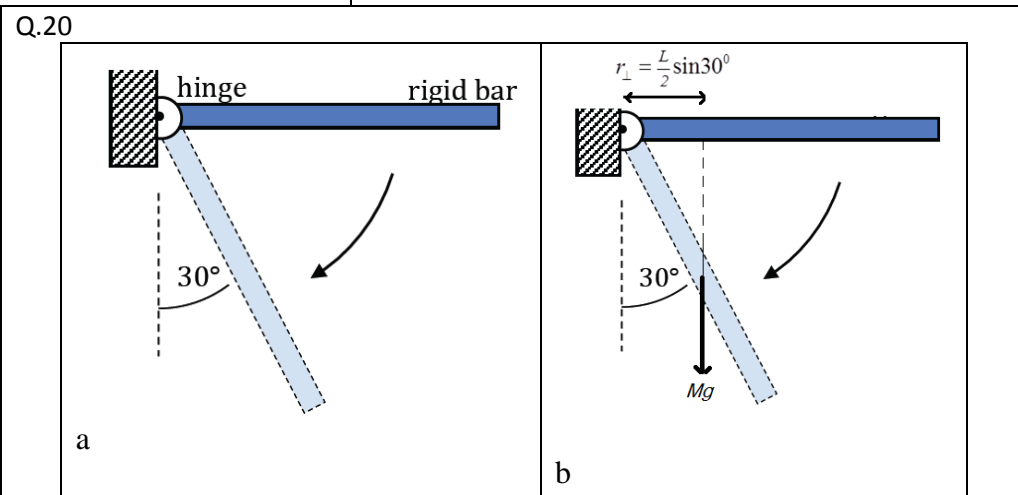
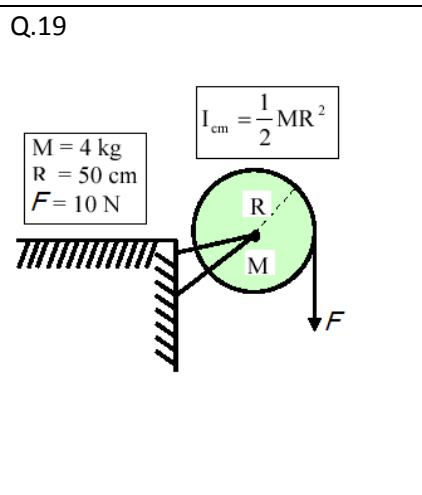
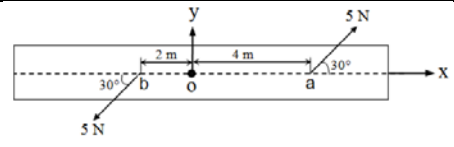
- Q.16 Moment of inertia of a disc about an axis through its center of mass and perpendicular to its plane is  $I_G = \frac{1}{2} MR^2$ . Calculate the moment of inertia about an axis through its tangent perpendicular to the plane.  $3/2 MR^2$





**Q.17:** In the Figure, two particles, each with mass  $m = 0.85 \text{ kg}$ , are fastened to each other, and to a rotation axis at  $O$ , by two thin rods, each with length  $d = 5.6 \text{ cm}$  and mass  $M = 1.2 \text{ kg}$ . The combination rotates around the rotation axis with the angular speed  $\omega = 0.30 \text{ rad/s}$ . Measured about  $O$ , what are the combination's  
 (a) rotational inertia and  $.0023 \text{ kg}\cdot\text{m}^2$   
 (b) kinetic energy  $1.1 \text{ E-3 J}$

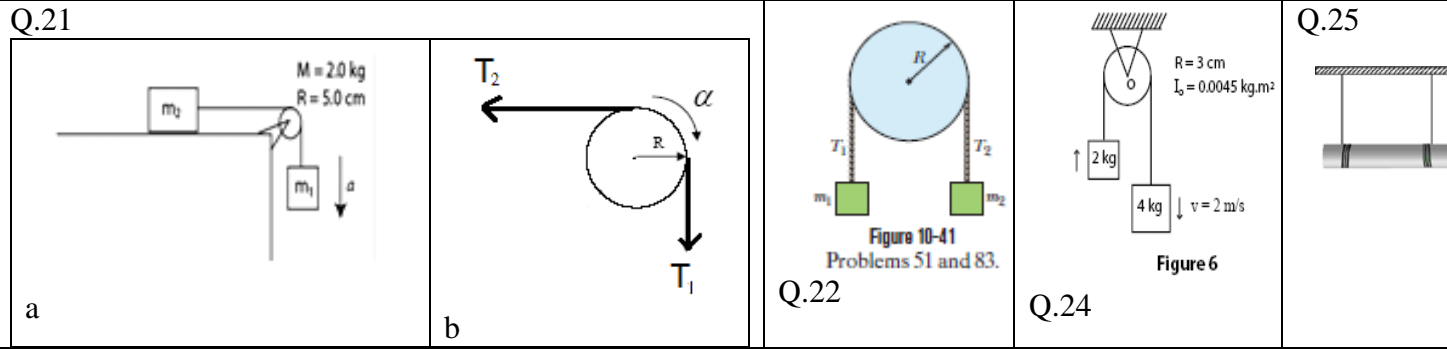
**Q.18** Calculate the net torque (magnitude, in N.m, and direction) on a uniform beam shown in the Figure about a point  $O$  passing through its center.  $15 \text{ N}\cdot\text{m}$  K direction



**Q.19** A uniform disk of radius  $50 \text{ cm}$  and mass  $4 \text{ kg}$  is mounted on a frictionless axle, as shown in Figure. A light cord is wrapped around the rim of the disk and a steady downward pull of  $10 \text{ N}$  is exerted on the cord. Find the tangential acceleration of a point on the rim of the disk.  $5 \text{ m/s}^2$  clockwise

**Q.20** A rigid bar with a mass  $M$  and length  $L$  is free to rotate about a frictionless hinge at a wall, see figure a. The bar has a moment of inertia  $I = \frac{1}{3} ML^2$  about the hinge, and is released from rest when it is in a horizontal position as shown. What is the instantaneous angular acceleration when the bar has swung down so that it makes an angle of  $30^\circ$  to the vertical?  $\alpha = \frac{3g}{4L}$  Clockwise

**Q.21** A mass,  $m_1 = 5.0 \text{ kg}$ , hangs from a string and descends with a linear acceleration " $a$ ". The other end is attached to a mass  $m_2 = 4.0 \text{ kg}$  which slides on a frictionless horizontal table. The string goes over a pulley (a uniform disk) of mass  $M = 2.0 \text{ kg}$  and radius  $R = 5.0 \text{ cm}$  (see Figure a). Find the value of  $a$ .  $.49 \text{ m/s}^2$



**Q.22** In Fig. 10-41, block 1 has mass  $m_1 = 0.460 \text{ kg}$ , block 2 has mass  $m_2 = 0.500 \text{ kg}$ , and the pulley, which is mounted on a horizontal axle with negligible friction, has radius  $R = 5.00 \text{ cm}$ . When released from rest, block 2 falls  $75.0 \text{ cm}$  in  $5.00 \text{ s}$  without the cord slipping on the pulley. (a) What is the magnitude of the acceleration of the blocks?  $6 \cdot 10^{-2} \text{ m/s}^2$ . What are (b) tension  $T_2$ .  $4.87 \text{ N}$  and (c) tension  $T_1$ ?  $4.54 \text{ N}$  (d) What is the magnitude of the pulley's angular acceleration.  $1.2 \text{ rad/s}^2$ ? (e) What is its rotational inertia?  $1.38 \cdot 10^{-2} \text{ kg}\cdot\text{m}^2$

**Q.23** A grinding wheel of moment of inertia  $I = 0.01 \text{ kg}\cdot\text{m}^2$  is brought to rest, in 10 revolutions, from an initial angular velocity of  $\omega = 3000 \text{ rpm} = 314.2 \text{ rad/s}$ . What is the power dissipated?  $2.47 \cdot 10^3 \text{ W}$

**Q.24** Figure shows a pulley ( $R = 3.0 \text{ cm}$  and  $I_o = 0.0045 \text{ kg}\cdot\text{m}^2$ ) suspended from the ceiling. A rope passes over it with a  $2.0 \text{ kg}$  block attached to one end and a  $4.0 \text{ kg}$  block attached to the other. When the speed of the heavier block is  $2.0 \text{ m/s}$ , calculate the total kinetic energy of the pulley and blocks.  $22 \text{ J}$

**Q.25** A uniform cylinder of mass  $m = 2$  kg and radius  $r = 0.15$  m is suspended by two strings wrapped around it, as shown in Figure. The cylinder remains horizontal while descending. Calculate the acceleration of the center of mass of the cylinder.  $6.53\text{m/s}^2$