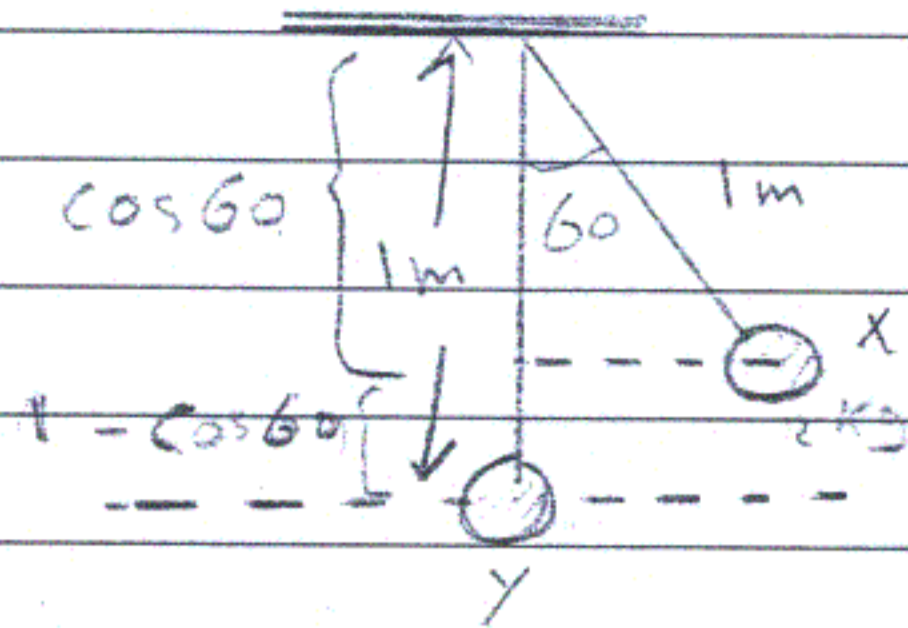


(CH #8)

Q.1

$$\Delta U_g + \Delta K = 0$$

$$\Rightarrow U_i(x) = K_f(y)$$



$$y_i = 1 - (1 \cos 60)$$

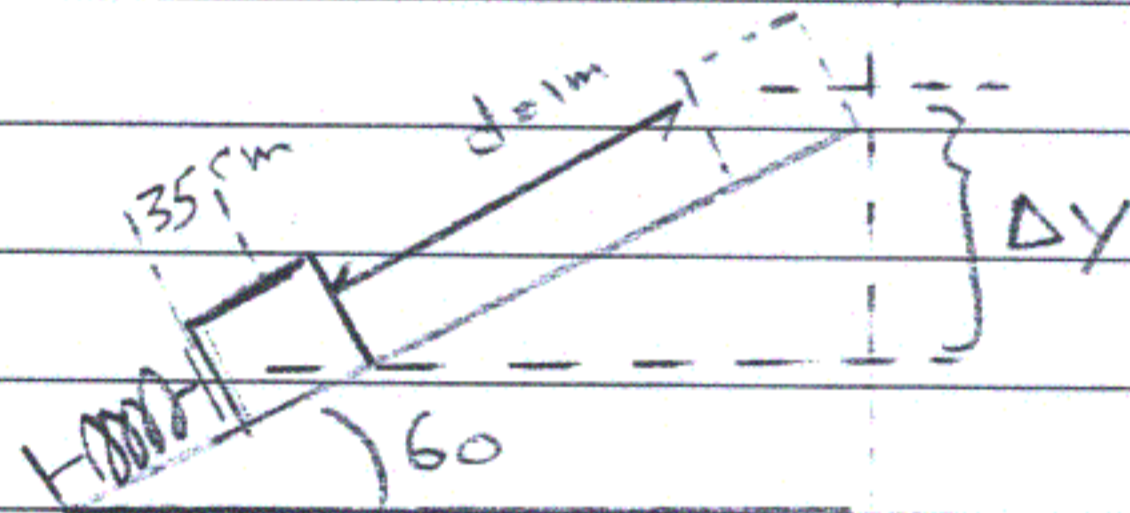
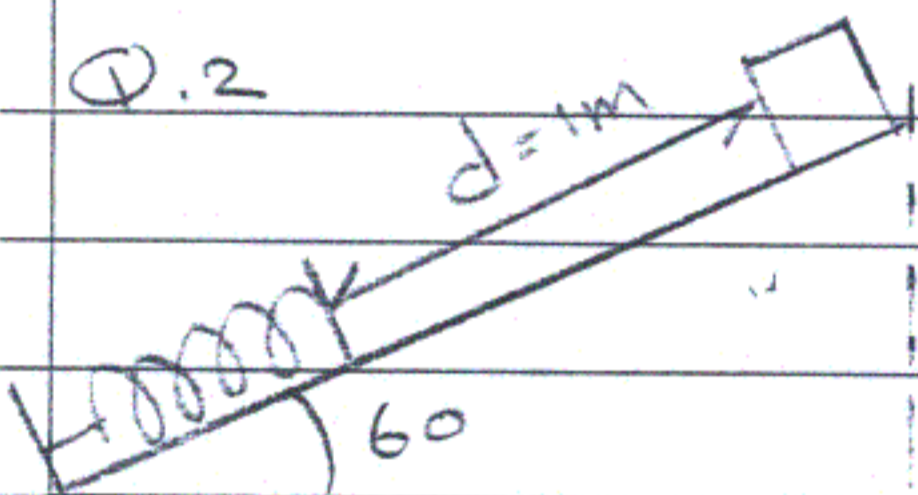
$$y_i = 0.5 \text{ m}$$

$$mgy_i = \frac{1}{2} m v_f^2$$

$$v_f = \sqrt{2gy_i} = \sqrt{2 \times 9.8 \times 0.5}$$

$$v_f = 3.1 \text{ m/s}$$

Q.2

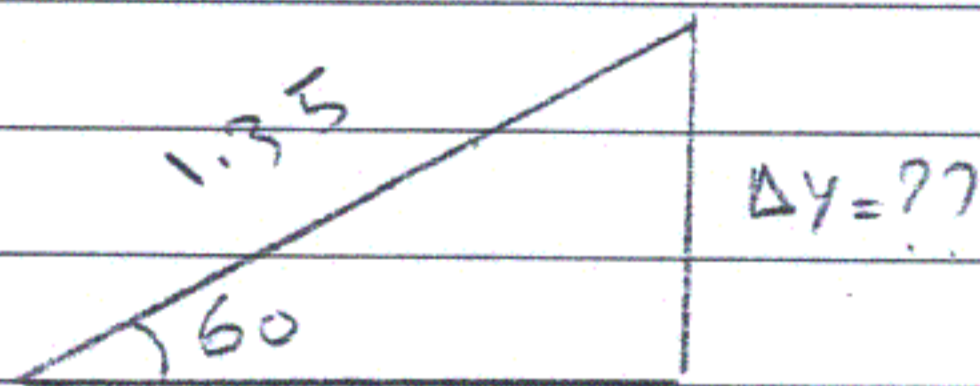


$$\Delta y = 1.35 \sin 60$$

$$\Delta y = 1.17 \text{ m}$$

for moving down

$$\Rightarrow (\Delta y = -1.17 \text{ m})$$



for spring $x_i = 0$ (relax)

$$x_f = 0.35 \text{ m}$$

$$K_i = 0, K_f = 0$$

\Rightarrow Ch.8

Cont CH8

~~Cont~~
Cont (2)

$$W = \Delta K + \Delta U_g + \Delta U_s - \Delta E_{th}$$

\Rightarrow

$$0 = \Delta U_g + \Delta U_s$$

$$0 = mg(\Delta y) + \frac{1}{2}k(x_f^2 - x_i^2)$$

$$0 = 3 \times 9.8(-1.17) + \frac{1}{2}(k)(0.35)^2$$

$$\Rightarrow k = 561.6 \text{ N/m}$$

Q.3

$$E_i = E_f$$

$$E_i = U_i + K_i$$

$$E_i = 0 + \frac{1}{2}m v_i^2$$

$$= \frac{1}{2} \times 0.5 \times 10^2$$

$$E_i = 25 \text{ J} = E_f$$

Q.4

for cycle under conservative force

$$W = 0 \Rightarrow W_{A \rightarrow B} + W_{B \rightarrow C} + W_{C \rightarrow A} = 0$$

$$W_{AB} + 54 - 96 = 0$$

$$= W_{A \rightarrow B} = 42 \text{ J}$$

Now:

$$W_{A \rightarrow B} + W_{B \rightarrow D} + W_{D \rightarrow A} = 0$$

$$W_{D \rightarrow A} = -42 - 136 = -178 \text{ J} = -W_{A \rightarrow D}$$

$$W_{A \rightarrow D} = +178 \text{ J}$$

Ch8

(2)

Cont ch8 :-

Q.5

There is No displacement along the axis

$$\Rightarrow (T) \Rightarrow d=0$$

$$\Rightarrow W_T = 0$$

Q.6 Using Hook's Law to find "X"

$$f_a = kx \Rightarrow mg = kx$$

$$2.5 \times 9.8 = 240 x$$

$$\Rightarrow x = 0.1 \text{ m}$$

$$\Rightarrow \Delta U_x = \frac{1}{2} k (x_f^2 - x_i^2) \quad x_i = 0.1, x_f = 0$$

$$\Rightarrow \Delta U_x = 0 - \frac{1}{2} \times 240 \times (0.1)^2$$

$$(\Delta U_x = -1.2 \text{ J})$$

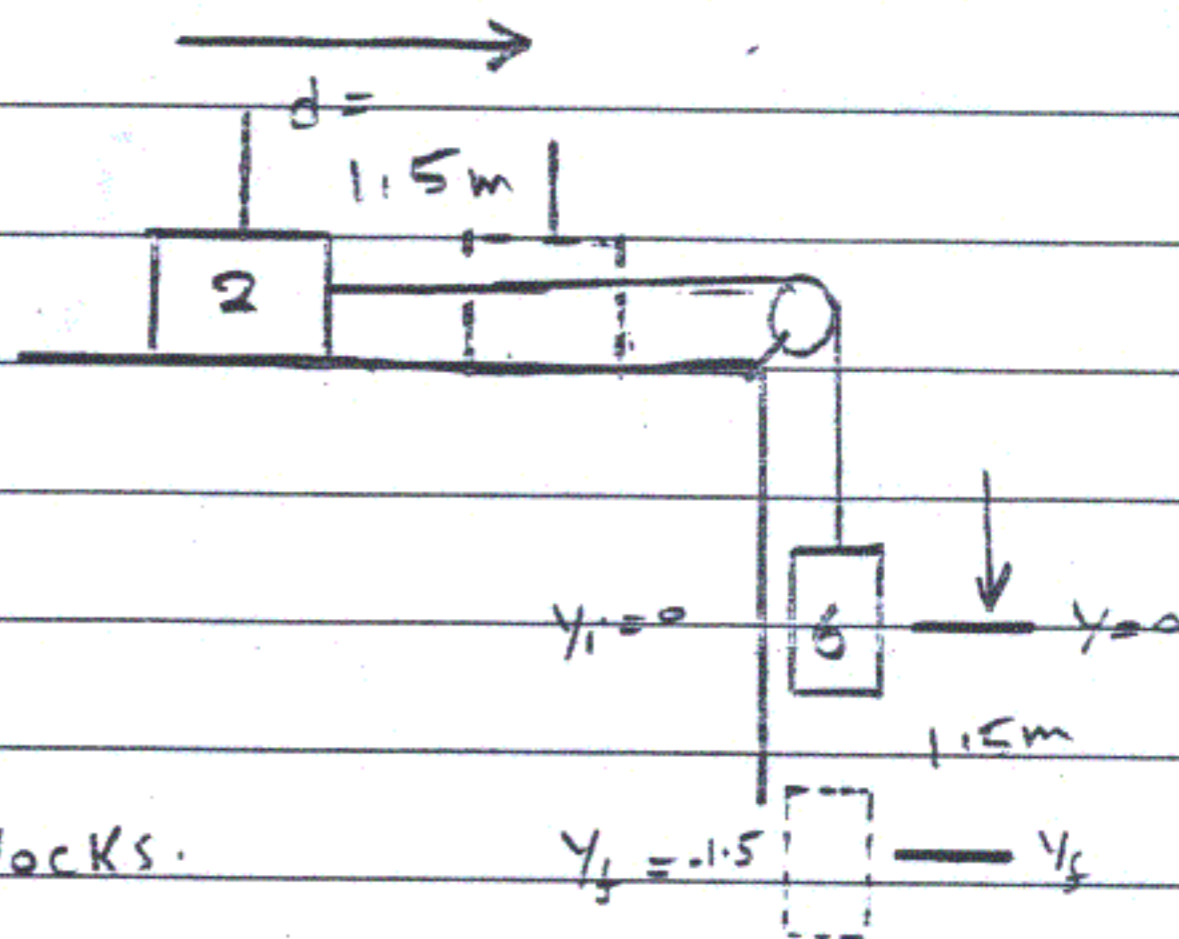
Q.7 $J = N \cdot m = (kg \cdot m/s^2) m = kg \cdot \frac{m^2}{s^2}$
 $= \text{Watt} \cdot s$

so The only nonaccepted unit of Potential Energy is $kg \cdot m/s^2$.

Cont ch8

Cont CH8

Q.8



$$W = \Delta K + \Delta U_g + \Delta E_{th}$$

But this time for two blocks.

$$0 = (\Delta K_2 + \Delta U_{g2} + \Delta E_{th2}) + (\Delta K_6 + \Delta U_{g6} + \Delta E_{th6})$$

$$0 = K_f(2) + 0 + f_k d + K_f(6) + mg(y_f - y_i) + 0$$

$$0 = \frac{1}{2} \times 2 \times v_f^2 + \mu_k N d + \frac{1}{2} \times 6 \times v_f^2 + 6 \times 9.8 \times (-1.5)$$

$$0 = v_f^2 + 0.4 \times 2 \times 9.8 \times 1.5 + 3 v_f^2 + (-88.2)$$

$$4 v_f^2 = 76.44$$

$$v_f = 4.137 \text{ m/s}$$

Q.9 $\Delta K = 0$, const speed

$\Delta U_g = 0$, horizontal surface

$$W_a = F d \cos 0 = 12 d$$

$\Delta U_x = 0$ (no spring)

$$\Rightarrow W_a = \Delta K + \Delta U_g + \Delta U_x + \Delta E_{th}$$

$$12 d = \Delta E_{th}$$

$$\Rightarrow \text{Power} = \frac{\Delta E_{th}}{t} = \frac{12 d}{t} = 12 (v) = 12 \times 1.5$$

$$\text{Power} = 18 \text{ watt}$$

→ ch.8

Cont (CH 8)

Q: 10

Use the K.E formulas:

$$K = \frac{1}{2} m v^2$$

you will find that: mass ρM and speed $3v$ will give max K.E.

Q.11 $v_i = 0 \Rightarrow K_i = 0$

$$v_f = 4 \text{ m/s} \Rightarrow K_f = \frac{1}{2} m (4)^2 = \frac{1}{2} \times 2 \times 4^2 = 16 \text{ J}$$

$$\Delta K = 16 - 0 = 16 \text{ J}$$

$$y_i = 1 \text{ m}$$

$$y_f = 0$$

$$\Delta y = -1 \text{ m}$$

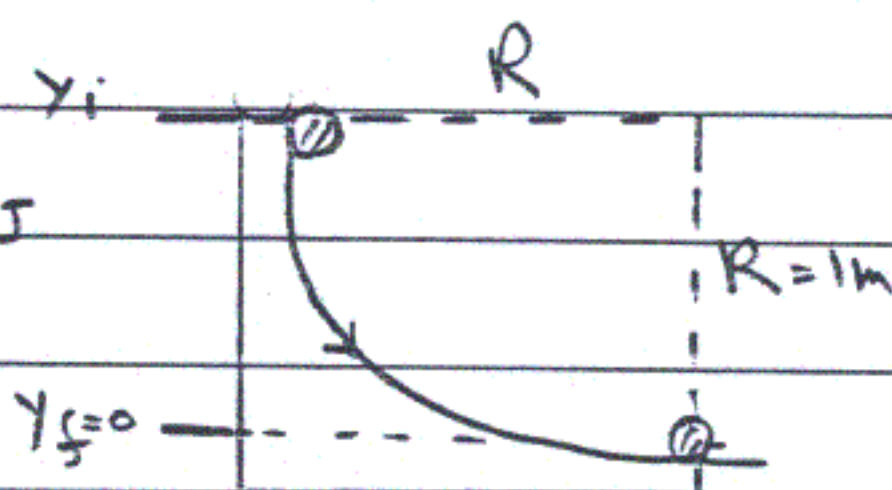
$$\Rightarrow \Delta U_g = mg \Delta y = 2 \times 9.8 (-1) = -19.6 \text{ J}$$

$$\Delta E_{th} = ? \quad \Delta U_x = 0, \quad W_a = 0$$

$$\Rightarrow \textcircled{W_a} = \Delta K + \Delta U_g + \textcircled{\Delta U_x} + \Delta E_{th}$$

$$0 = 16 + (-19.6) + \Delta E_{th}$$

$$\Rightarrow (\Delta E_{th} = 3.6 \text{ J})$$



Q.12

From the Figure

$$y_i = 50 \text{ m}$$

$$y_f = 20 \text{ m}$$

$$v_i = 30 \text{ m/s}$$

$$v_f = ?$$

This is an Isolated System

with no Friction \Rightarrow

$$\Delta E = 0 \Rightarrow \Delta K + \Delta U_g = 0 \Rightarrow \frac{1}{2} m (v_f^2 - v_i^2) + mg \Delta y = 0$$

$$(\div m) \Rightarrow \frac{1}{2} (v_f^2 - 30^2) + 9.8 (20 - 50) = 0$$

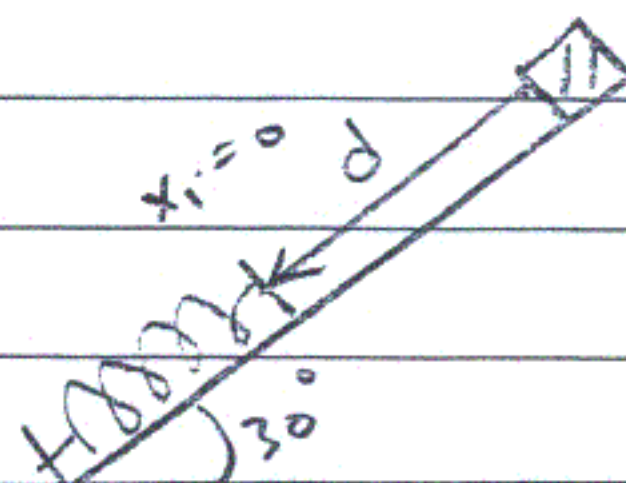
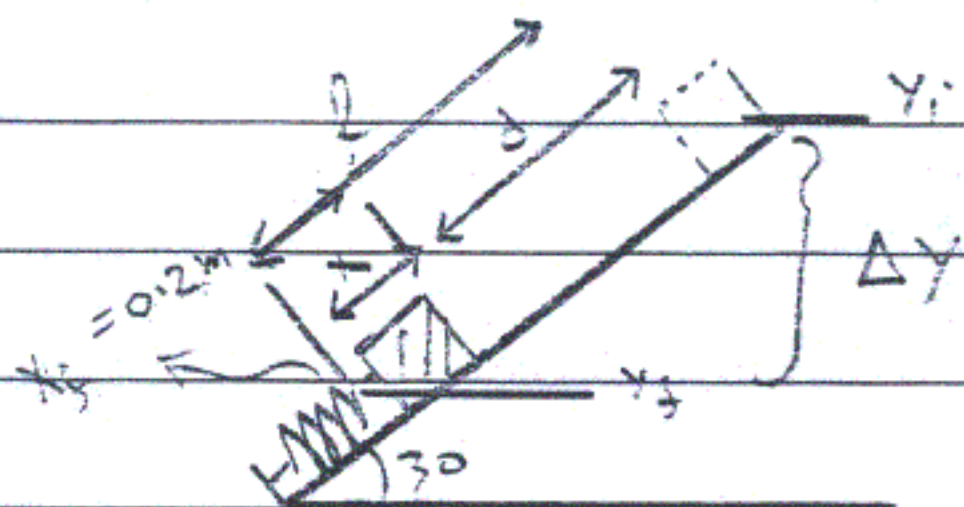
$$= \boxed{v_f = 38.6 \text{ m/s}}$$

ch 8

(5)

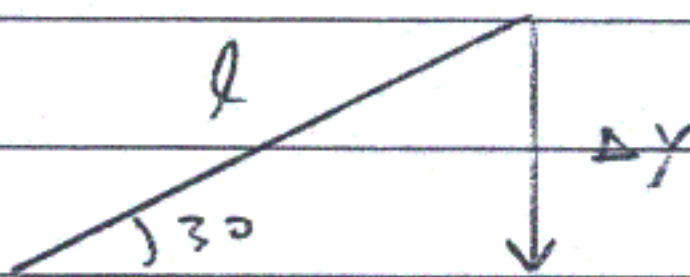
Cont ch8

Q.13



When $(l = d + x)$

$(l = 0.2 + d)$



$$\Delta y = -l \sin 30 \text{ (Down)}$$

$$\Rightarrow \Delta U_g = mg \Delta y = 3 \times 9.8 \times (-l \sin 30) = (-14.7l \text{ J})$$

$$\Delta K = 0 \text{ (from rest to rest)}$$

$$\Delta E_{th} = 0 \text{ (No Friction)}$$

$$\Delta U_x = \frac{1}{2} k (x_f^2 - x_i^2) = \frac{1}{2} \times 400 \times ((0.2)^2 - 0)$$

$$\Delta U_x = 8 \text{ J}$$

$$W_a = 0 \text{ (No applied Force)}$$

$$\Rightarrow \textcircled{W_a} = \textcircled{\Delta K} + \Delta U_g + \Delta U_x + \textcircled{\Delta E_{th}}$$

$$\Rightarrow 0 = -14.7l + 8$$

$$\Rightarrow l = 0.544 = 0.2 + d$$

$$\Rightarrow (d = 0.344 \text{ m})$$

Q.14 To Find $Y_{max} = \frac{V_0^2 (\sin \theta)^2}{2g}$, we need $V_0 = ?$

V_0 is the final velocity after leaving the spring

Now: Spring-mass system:

$$V_i = 0, V_f = ??$$

$$x_i = 0.2 \text{ m (when it was compressed)}$$

$$x_f = 0 \text{ (its back to relax length)}$$

$$\Delta y = 0.2 \sin 45 = 0.14 \text{ m (up)}$$

$$\Delta E_{th} = 0 \text{ (No friction)}$$

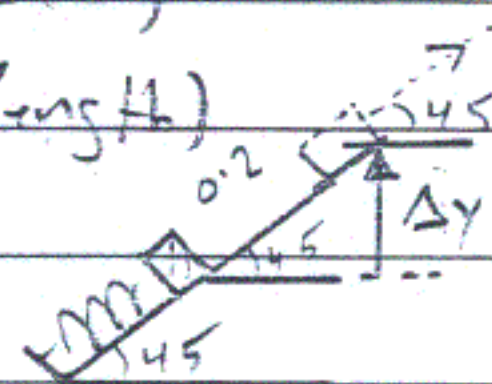
$$W_a = 0 \text{ (No applied Force)}$$

$$\Rightarrow \textcircled{W_a} = \Delta K + \Delta U_g + \Delta U_x + \textcircled{\Delta E_{th}}$$

$$0 = \frac{1}{2} \times 0.1 \times (V_f^2 - 0) + 0.1 \times 9.8 \times 0.14 + \frac{1}{2} \times 100 (0 - (0.2)^2) + 0$$

$$V_f = 6.1 \text{ m/s} = V_0 \text{ in the projectile:}$$

$$\Rightarrow Y_{max} = \frac{(6.1)^2 (\sin 45)^2}{2 \times 9.8} = 0.95 \text{ m}$$



ch8

6

Cont CH 8

Q. 15

$$\left. \begin{array}{l} V_i = 0 \\ V_f = 0 \end{array} \right\}$$

$$\Delta K = 0$$

$$\Delta Y = -1 \text{ m (Down)}$$

$$\Rightarrow \Delta U_g = m g \Delta Y = -1 \times 9.8 \times 1 = -9.8 \text{ J}$$

$$\Delta E_{th} = 0 \quad (\text{No friction})$$

$$W_a = 0 \quad \text{No applied Force}$$

For spring:

$$x_i = 0 \quad (\text{relax})$$

$$x_f = ? \quad (\text{max compressed distance})$$

$$\overset{0}{W_a} = \overset{0}{\Delta K} + \Delta U_g + \Delta U_s + \overset{0}{\Delta E_{th}}$$

$$= 0 = -9.8 + \frac{1}{2} (400) (x_f^2 - 0)$$

$$x_f = 0.221 \text{ m}$$

end

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