

# CH#31

## H.W. Solution

#3  $U_E = \frac{q^2}{2C}$ ,  $C = \frac{q^2}{2U_E}$ ,  $q^2 = 1.6 \times 10^{-6} C$

$$U_E = 1.40 \times 10^{-6} J$$

#7

$q$   $\xrightarrow{\text{corrosion products}}$   $x$

$i$   $\longrightarrow$   $v$

$\frac{1}{C}$   $\longrightarrow$   $K$

$L$   $\longrightarrow$   $m$

a.  ~~$\frac{1}{2} m v^2$~~

$L = 1.25 H$

$m = 1.25 kg$

b.  $K = \frac{1}{C} = \frac{2 U_E}{\frac{q^2}{2}}$

c.  $U = \frac{1}{2} K A^2$

$$A = \sqrt{\frac{2U}{K}}$$

d.  $U = \frac{1}{2} m v^2$

$$v = \sqrt{\frac{2U}{m}}$$

#19

$$a. \quad q = Q \sin(\omega t)$$

$$i = Q \omega \cos(\omega t)$$

$$i_{\max} = Q \omega = 2.0 \text{ A}$$

$$Q = \frac{i_{\max}}{\omega}$$

$$\text{where } \omega = \frac{1}{\sqrt{LC}}$$

$$b. \quad U = \frac{1}{2} \frac{q^2}{2C}$$

$$\frac{dU}{dt} = \frac{1}{2C} (2q) \frac{dq}{dt} = 0$$

Because  $\frac{dU}{dt} = 0$  at the maxima.

$$\therefore q \cdot \frac{dq}{dt} = 0$$

$$(Q \sin(\omega t))(Q \omega) \cos(\omega t) = 0$$

$$\therefore \sin(2\omega t) = 0$$

#19 Cont

$$\Rightarrow 2\omega t = \pi$$

$$t = \frac{\pi}{2\omega}$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$C \quad U = \frac{q^2}{2C} = \frac{Q^2}{2C} \sin^2(\omega t)$$

$$t = \frac{\pi}{2\omega}$$

# 26

$$q = Q e^{-\frac{Rt}{2L}} \cos(\omega t)$$

$$U_E = \frac{q^2}{2C} = \frac{Q^2}{2C} e^{-\frac{Rt}{L}}$$

$$U_{max} = \frac{Q^2}{2C}$$

$$\therefore U_E = U_{max} e^{-\frac{Rt}{L}}$$

$$\frac{U_E}{U_{max}} = \frac{1}{2} = e^{-\frac{Rt}{L}}$$

$$\therefore \frac{Rt}{L} = \ln(2)$$

$$t = \frac{L \ln(2)}{R}$$

# 29.  $i_L = I_L \sin(\omega t - \frac{\pi}{2})$

$$I_L = \frac{V_L}{X_L} = \frac{\epsilon_m}{\omega L}$$

$\omega = \omega_d = 2\pi f = 2000\pi$

$\therefore I_L = \frac{30}{2000\pi \times 50 \times 10^{-3}}$

$I_L = \frac{30}{100\pi} = 95.5 \text{ mA}$

#29

$$b. \omega_d = 2\pi f = 2\pi \times 8000.$$

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#36, From the graph  
the resonance frequency

$$\omega = \omega_d = 25 \times 10^3 \text{ rads.}$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$LC = \frac{1}{\omega^2} = \frac{1}{(25 \times 10^3)^2}$$

$$a. C = \frac{1}{2 \times 10^{-4} \times 625 \times 10^6}$$

$$= \frac{1}{1250 \times 10^2}$$

$$= 8 \mu\text{F}$$

$$b. I_{\text{max}} = \frac{E_m}{R}$$

$$\therefore R = \frac{E_{\text{max}}}{I_{\text{max}}} = \frac{8}{4} = 2 \Omega$$

Note  $I_{\text{max}} = 4 \text{ A}$ , from graph.

$$\# 41, \tan \phi = \frac{X_L - X_C}{R}$$

$$R = \frac{X_L - X_C}{\tan \phi}$$

$$X_L = \omega L = 2\pi \times 930 \times 88 \times 10^{-3}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi \times 930 \times 0.44 \times 10^{-6}}$$

$$\phi = 75^\circ$$

Solve for R

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# 53.

$$a) Z = \sqrt{R^2 + X_L^2}$$

$$= \sqrt{100 + (1.3)^2}$$

$$= \sqrt{105.69}$$

$$\approx 10.28 \Omega$$

$$b) P_{AV} = E_{rms} \cdot I_{rms} \cdot \cos \phi$$

$$E_{rms} = 120 \text{ V}, I_{rms} = \frac{E_{rms}}{Z} = \frac{120}{10.28}, \cos \phi = \frac{R}{Z}$$

#61

$$N_P = 500,$$

$$N_S = 10.$$

$$V_S = V_P \cdot \frac{N_S}{N_P}$$

$$a. \quad V_S = 120 \times \frac{10}{500}$$

$$~~= 2.4 V~~$$

$$= 2.4 V$$

b.

$$I_P = \frac{V_P}{R_{eq}} = \frac{120}{\left(\frac{N_P}{N_S}\right)^2 R}$$

$$= \frac{120}{2500 \times 15}$$

$$= 3.2 \text{ mA}$$

$$b. \quad I_S = \frac{V_S}{R} = \frac{2.4}{15}$$
$$= 0.16 \text{ A}$$