Examples: Kepler's third law PHYS 215 (Introduction to Astronomy)

PHYS 215 Selected Problems from Chapter One

1. How long it takes a space craft moving at speed of 100,000 km/hr to reach Barnard's star system which is at a distance of about 5.5 ly from us?

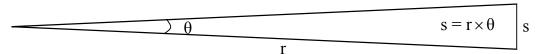
distance = d =
$$5.5 \text{ ly} \times 9.46 \times 10^{12} \text{ km/ly} = 5.20 \times 10^{13} \text{ km}$$

time = t = d / v = 5.20×10^{13} / $100000 = 5.2 \times 10^{8} \text{ hrs.} = 2.2 \times 10^{7} \text{ days}$
= $5.9 \times 10^{4} \text{ yrs.}$

2. How far away [in parsec (pc) and light years (ly)] is a star from us if a round trip journey takes about 200 years for a space craft that is moving at one tenth the speed of light?

time for round trip =
$$2 \times t = 200$$
 yrs. = 73050 days = 1753200 hrs. = 6.312×10^9 s time for one way = $t = 6.312 \times 10^9$ s / $2 = 3.156 \times 10^9$ speed = $v =$ one tenth of the speed of light = $0.1 \times 300000 = 30000$ km/s distance = $d = (v \times t) = 30000 \times 3.156 \times 10^9 = 9.467 \times 10^{13}$ km = 3.064 pc = 9.988 ly

3. What is the angular size of Jupiter at the closest approach to the Earth (apposition) and the farthest distance from the Earth (conjunction)?



diameter of Jupiter = s = 142984 kmdistance of Jupiter from the Sun = $r_J = 5.20 \text{ au}$ Closest approach to the Earth

$$r_1 = r_J - r_e = 5.20 - 1.00$$

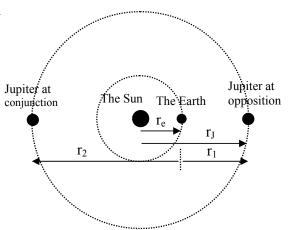
= 4.20 au = 6.3×10⁸ km
farthest distance from the Earth
 $r_2 = r_J + r_e = 5.20 + 1.00$
= 6.20 au = 9.3×10⁸ km

$$\theta_1 = s / r_1 = 142984 / 6.3 \times 10^8 = 2.27 \times 10^{-4} \text{ rad}$$

= 0.013 degrees = 0.78 arc minutes
= 46.8 arc seconds

$$\theta_2 = s / r_2 = 142984 / 9.3 \times 10^8 = 1.54 \times 10^{-4} \text{ rad}$$

= 0.0088 degrees = 0.53 arc minutes
= 31.7 arc-seconds



4. What should be the distance of a sphere (diameter = 30 cm) from us if its angular diameter is equal to 50 seconds of arc?

50 sec. of arc = 0.83333 min. of arc = 0.01389 degrees
=
$$0.0002424$$
 rad.
r = s / θ = 30 / 0.00024 = 123759 cm = 1238 m = 1.24 km.

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