

# 36.

$$K = 50 \text{ GeV} = 50 \times 10^9 \times 1.6 \times 10^{-19} = 8 \times 10^{-9} \text{ J}$$

$$\begin{aligned} \text{a) } E &= K + m_0 c^2 = 50 \times 10^3 \text{ MeV} + 939 \text{ MeV} \\ &= 50939 \text{ MeV} \end{aligned}$$

$$E^2 = p^2 c^2 + m_0^2 c^4$$

$$p = \frac{1}{c} \sqrt{E^2 - (m_0 c^2)^2} = \frac{1}{c} \sqrt{(50939)^2 - (939)^2}$$

$$\boxed{p = 50930 \left( \frac{\text{MeV}}{c} \right)} \quad \text{note the unit!}$$

$$\text{b) } K = (\gamma - 1) m_0 c^2$$

$$50 \times 10^3 = (\gamma - 1) 939 \Rightarrow \gamma - 1 = 53.2$$

$$\gamma = 54.2 = \frac{1}{\sqrt{1 - \frac{u^2}{c^2}}}$$

$$\Rightarrow \frac{u^2}{c^2} = \frac{\gamma^2 - 1}{\gamma^2} \Rightarrow u = c \sqrt{\frac{\gamma^2 - 1}{\gamma^2}} = \boxed{0.9998c}$$

# 38.

$$\text{a) } E = 400 m_0 c^2 = 400 (939 \text{ MeV}) = \gamma m_0 c^2$$

$$\Rightarrow \gamma = 400 = \frac{1}{\sqrt{1 - \frac{u^2}{c^2}}} \Rightarrow u = c \sqrt{\frac{\gamma^2 - 1}{\gamma^2}} = \boxed{0.999997c}$$

$$K = (\gamma - 1) m_0 c^2 = 399 (939 \text{ MeV}) = \boxed{37.5 \text{ GeV}}$$