

Summary chapter 30

I. Objective:

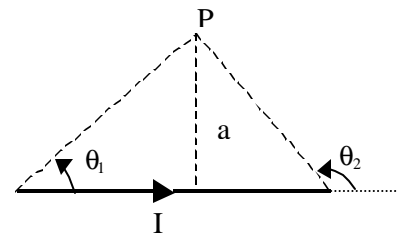
1. Calculate **the magnetic field** at a point P due to a current element by using **Biot-Savart law**.
2. Calculate **the magnetic force** between two parallel conductors carrying currents I_1 and I_2 .
3. Use **Ampere's law** to calculate the magnetic field due to a cylindrical wire of **radius R**.
4. Calculate the magnetic field due to a **solenoid**.
5. Calculate the **magnetic flux** through a surface A placed in a magnetic field.

II. Summary of major points:

1. * The magnetic field due to a straight carrying a current I is given by;

$$B_p = \frac{\mu_0 I}{4\pi a} (\cos \theta_1 - \cos \theta_2)$$

where a is distance between P and the wire and $\mu_0 = 4\pi \times 10^{-7}$ wb/A.m.



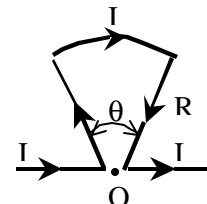
The direction of the magnetic field at point P is **out of the paper**.

- * The magnetic field due to an infinite long wire ($\theta_1 = 0, \theta_2 = \pi$) is:

$$B_p = \frac{\mu_0 I}{2\pi a}$$

- * The magnetic field at the center of an arc of radius **R** which subtends an angle θ is given by:

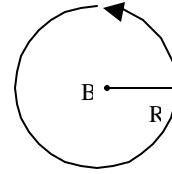
$$B_o = \frac{\mu_0 I}{4\pi R} \theta$$



The angle θ is in **radian**.

- * The magnetic field **at the center** of circular loop carrying a current I is given by:

$$B = \frac{\mu_0 I}{2R} \quad (\text{here } \theta = 2\pi)$$



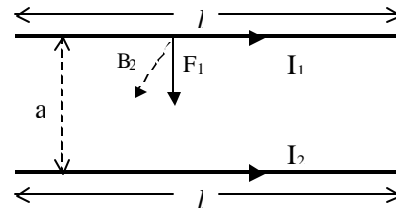
where R is the radius of the loop.

The direction of the magnetic at the center of the loop is **out of the paper**.

2. The **magnetic force** per unit length between parallel conductors is given by:

$$\frac{F_1}{\ell} = \frac{\mu_0 I_1 I_2}{2pa}$$

where a is distance between the two conductors.



- * If the currents, I_1 and I_2 have the **same** direction, the wires will **attract** each other.
- * If the current have **opposite** direction, the wires will **repel** each other.

3. Amper's law is defined as;

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

The magnetic field due to a long wire of radius R is;

$$B = \frac{\mu_0 I_0}{2\pi r} \quad r \geq R \quad (\text{inside the wire})$$

$$B = \left(\frac{\mu_0 I_0}{2\pi r} \right) r \quad r < R \quad (\text{outside the wire})$$

4. The magnetic flux through a surface A is given by:

$$\Phi_m = \int \vec{B} \cdot d\vec{A}$$

If the area is a **plane** then and B is **uniform** then:

$$\Phi_m = BA \cos \theta$$

where θ is angle between B and A .

