

1. The **electric current I** is defined as:

$$I = \frac{dq}{dt}$$

The current is the rate of flow of electric charge. It has units of Coulomb/second or **Ampere (A)**.

It is also given by:

$$I = n e v_d A$$

where n is number of charge carriers, e is the magnitude of the charge of the electron, v_d is drift speed, that is, the speed of the electrons in the conductor, and A is cross-sectional area of the conductor.

A uniform **current density J** is defined as:

$$J = \frac{I}{A} = n e v_d = \frac{1}{\mathbf{r}} E = \mathbf{s} E$$

Where \mathbf{r} is the resistivity and \mathbf{s} is conductivity and E is electric field. The current density has units of **A/m²**.

2. **The resistance R** of a conductor is defined as

$$R = \frac{V}{I}$$

where V is the potential difference across the conductor and I is the current through the conductor.

This relation is called *Ohm's law*. The unit of the resistance R is volt per ampere or *Ohms* (Ω).

The resistance depends on the geometry of the conductor, that is the length L and the cross section area A .

$$R = r \frac{L}{A} = \frac{L}{sA}$$

where r is resistivity and s is conductivity.

3. The resistivity of a conductor varies with temperature as:

$$r = r_0 [1 + \alpha(T - T_0)]$$

where r is resistivity at temperature T , r_0 is resistivity at temperature T_0 and α is temperature coefficient of resistivity (constant).

We can see from the above equation that

$$\alpha = \frac{r - r_0}{r_0 \Delta T}$$

It is easy to see that the unit of α is $^{\circ}\text{C}^{-1}$ or $/\text{K}$.

Similarly, the resistance varies with temperature T as

$$R = R_0 [1 + \alpha(T - T_0)]$$

where R_0 is the resistance of the conductor at T_0 and R is the resistance at temperature T .

Note: We neglect the changes in the length and cross section area with temperature.

4. The **dissipated power P** in a resistor is given by;

$$P = VI = RI^2 = \frac{V^2}{R} \text{ (watt)}$$

This dissipated or lost power is transformed into heat.

Note: A light bulb with a power of 60 W has a resistance *smaller* than a light bulb with a power of 40 W!