

Ideal Gas Law	:	$PV = nRT = NkT$
Isothermal processes	:	$T = \text{constant} \quad \text{P} \quad (DT = 0)$
Isobaric processes	:	$P = \text{constant} \quad \text{P} \quad (DP = 0)$
Isovolumetric processes	:	$V = \text{constant} \quad \text{P} \quad (DV = 0)$
Adiabatic process	:	$Q = \text{zero} \quad \text{P} \quad (Q = 0) \quad \text{P} \quad PV^\gamma = \text{constant}$ $TV^{\gamma-1} = \text{constant}$
Internal Energy	:	$U = nC_v T, \quad DU = nC_v DT$
Work	:	$dW = PdV, \quad W = \int PdV$
Heat	:	$Q = nC_v DT$ (for constant volume), $R = C_p - C_v$ $Q = nC_p DT$ (for constant pressure), $\gamma = C_p / C_v$
1st Law of T.D.	:	$Q = W + DU$
Entropy	:	$dS = dQ/T, \quad DS = \int dQ/T$

Isothermal Processes:

$$T = \text{constant} \quad \text{P} \quad PV = nRT = \text{constant} \quad \text{P} \quad P_i V_i = P_f V_f$$

$$DT = 0 \quad \text{P} \quad PDV - VDP = 0$$

$$DU = 0$$

$$W = nRT \ln(V_f/V_i) = P_i V_i \ln(V_f/V_i) = P_f V_f \ln(V_f/V_i)$$

$$Q = W = nRT \ln(V_f/V_i) = P_i V_i \ln(V_f/V_i) = P_f V_f \ln(V_f/V_i)$$

$$DS = \int dQ/T = Q/T = W/T = nR \ln(V_f/V_i)$$

Isobaric Process:

$$P = \text{constant} \quad \text{P} \quad V/T = nRT/P = \text{constant} \quad \text{P} \quad V_i/T_i = V_f/T_f$$

$$DP = 0 \quad \text{P} \quad PDV = nRDT \quad \text{P} \quad P = nRDT/DV$$

$$DU = nC_v DT = C_v PDV/R = C_v W/R = (\gamma - 1)^{-1} W$$

$$W = PDV = nRDT = n(C_p - C_v) DT = (\gamma - 1) nC_v DT$$

$$Q = W + DU = nC_v DT + (\gamma - 1) nC_v DT = \gamma nC_v DT = nC_p DT = \gamma PDV / (\gamma - 1)$$

$$DS = \int dQ/T = \int \gamma nC_v dT/T = \gamma nC_v \ln(T_f/T_i) = nC_p \ln(T_f/T_i) = nC_p \ln(V_f/V_i)$$

Isovolumetric Process:

$$V = \text{constant} \quad \text{P} \quad P/T = nRT/V = \text{constant} \quad \text{P} \quad P_i/T_i = P_f/T_f$$

$$DV = 0 \quad \text{P} \quad VDP = nRDT \quad \text{P} \quad V = nRDT/DP$$

$$DU = nC_v DT = C_v VDP/R$$

$$W = 0$$

$$Q = DU = nC_v DT = C_v VDP/R$$

$$DS = \int dQ/T = \int nC_v dT/T = nC_v \ln(T_f/T_i) = nC_v \ln(P_f/P_i)$$

Adiabatic Process:

$$PV^\gamma = \text{constant} \quad \text{P} \quad P_i V_i^\gamma = P_f V_f^\gamma \quad \text{P} \quad VdP - \gamma PdV = 0$$

$$TV^{\gamma-1} = \text{constant} \quad \text{P} \quad T_i V_i^{\gamma-1} = T_f V_f^{\gamma-1} \quad \text{P} \quad VdT - (\gamma - 1)TdV = 0$$

$$DU = nC_v DT = - \int PdV = \int (P_i V_i^\gamma) dV / V^\gamma = (P_i V_i^\gamma) (1 - \gamma) (V_f/V_i)^{1-\gamma}$$

$$W = -DU = -nC_v DT = (P_i V_i - P_f V_f) / (\gamma - 1) = -nRDT / (\gamma - 1)$$

$$Q = 0$$

$$DS = \int dQ/T = 0 \quad (\text{entropy stays constant in reversible adiabatic processes, } Q = 0)$$