

Name: _____

ID # _____

Key

- 1- A 0.4-kg mass attached to a spring of force constant 40 N/m vibrates with a simple harmonic motion of amplitude 10 cm. Calculate the shortest time that is taken by the mass to move from $x = 0$ to $x = 10$ cm. [0.157 s]

$$m = 0.4 \text{ kg}$$

$$k = 40 \text{ N/m}$$

$$x_m = 10 \text{ cm}$$

time from $x=0$ to $x=x_m$
equals $\frac{T}{4}$.

$$T = 2\pi \sqrt{\frac{m}{k}} = 2\pi \sqrt{\frac{0.4}{40}} = 0.628$$

$$\text{time} = \frac{T}{4} = 0.157 \text{ s}$$

- 2- A mass of 1.0 kg connected to a light spring of force constant 30 N/m oscillates on a horizontal frictionless surface with magnitude 3 cm. Find the kinetic energy of the system when the displacement equals 2 cm. [7.5×10^{-3} J]

$$m = 1 \text{ kg}$$

$$k = 30 \text{ N/m}$$

$$x_m = 3 \text{ cm}$$

when $x = 2$ find $K = ?$

$$K = E - U = \frac{1}{2} k x_m^2 - \frac{1}{2} k x^2$$

$$= \frac{1}{2} (30) (0.03^2 - 0.02^2)$$

$$= 15 (5 \times 10^{-4}) = 7.5 \times 10^{-3} \text{ J}$$

- 3- A particle at the end of a spring executes simple harmonic motion with an amplitude of 4.0 cm. At what displacement (x) will its speed be equal to one half its maximum speed? [3.46 cm]

$$v^2 = \omega^2 (x_m^2 - x^2)$$

$$\left(\frac{v_m}{2}\right)^2 = \frac{k}{m} (x_m^2 - x^2)$$

where $\omega = \sqrt{\frac{k}{m}}$

where $v_m = x_m \omega = x_m \sqrt{\frac{k}{m}}$

$$\Rightarrow \frac{x_m^2 k}{4m} = \frac{k}{m} (x_m^2 - x^2)$$

$$\frac{x_m^2}{4} = x_m^2 - x^2$$

$$x^2 = \frac{3x_m^2}{4} \Rightarrow x = \frac{\sqrt{3}x_m}{2} = \frac{\sqrt{3} \cdot 4}{2}$$

$$= 3.46 \text{ cm}$$

another method

طريقة أخرى

$$v = -v_m \sin \omega t$$

$$\frac{v_m}{2} = -v_m \sin \omega t \Rightarrow \omega t = \sin^{-1}\left(\frac{1}{2}\right) = \dots$$

$$x = x_m \cos \omega t$$

$$= 4 \cos\left(\frac{\pi}{6}\right)$$

$$= 3.46 \text{ cm}$$