

Q#1: A 1.0-C charge moves with a velocity  $\vec{v} = (2.0\hat{i} + 3.0\hat{j})$  m/s and experiences a magnetic force  $\vec{F}_B = (15\hat{i} - 10\hat{j} + 8.0\hat{k})$  N in a magnetic field  $\vec{B} = B_y\hat{j} + 5.0\hat{k}$ . Then y-component of magnetic field  $B_y$  is:

$$\vec{F}_B = q(\vec{v} \times \vec{B}) = 1 \times (2\hat{i} + 3\hat{j}) \times (B_y\hat{j} + 5\hat{k}) = 2B_y\hat{k} - 10\hat{j} + 15\hat{i}$$

$$\vec{F}_B = 15\hat{i} - 10\hat{j} + 8.0\hat{k} = 2B_y\hat{k} - 10\hat{j} + 15\hat{i}$$

$$B_y = \frac{8}{2} = 4 \text{ T}$$

Q#2: A proton moves with constant velocity,  $\vec{v} = (8.0 \times 10^5 \text{ m/s})\hat{i}$ , through crossed electric and magnetic fields. If the magnetic field is  $\vec{B} = (2.5 \text{ mT})\hat{j}$ , what is the electric field? [ $\hat{i}$ ,  $\hat{j}$  and  $\hat{k}$  are the unit vectors in the positive x, y and z directions, respectively].

$$-\vec{E} = (\vec{v} \times \vec{B}) \Rightarrow \vec{E} = -(\vec{v} \times \vec{B}) = -8 \times 10^5 \hat{i} \times 2.5 \times 10^{-3} \hat{j}$$

$$\vec{E} = -8 \times 10^5 \times 2.5 \times 10^{-3} (2 \times \hat{j}) = -2 \times 10^3 \hat{k}$$

Q#3: A 100 turns coil, lies in xz-plane, has an area of 2.0 m<sup>2</sup> and carries a current  $I = 0.3$  A in the direction indicated in the following figure. The coil lies in a magnetic field directed along the x-axis and has a magnitude of 1.5 T. What is magnitude and direction of the torque on the coil?

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

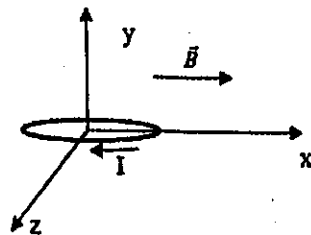
$$\vec{B} = 1.5 \hat{i}$$

$$\vec{\mu} = NI A (-\hat{j}) = -100 \times 0.3 \times 2 \hat{j}$$

$$= -60 \hat{j}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B} = -60 \hat{j} \times 1.5 \hat{i}$$

$$\vec{\tau} = -90 (\hat{j} \times \hat{i}) = 90 \hat{k}$$



Q#1: At one instant, an electron is moving in the  $xy$  plane. The components of its velocity are  $v_x = 5.0 \times 10^5$  m/s and  $v_y = 3.0 \times 10^5$  m/s. A magnetic field  $B = 0.80$  T is in the positive  $y$  direction. At that instant, what is the magnetic force on the electron?

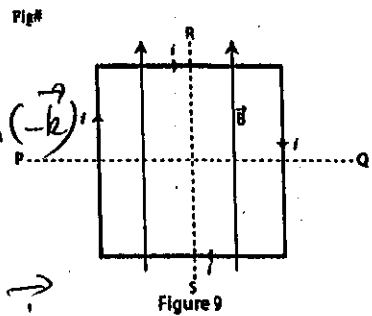
$$\begin{aligned} \vec{F}_B &= q(\vec{v} \times \vec{B}) = -1.6 \times 10^{-19} (5 \times 10^5 \vec{i} + 3 \times 10^5 \vec{j}) \times 0.8 \vec{j} \\ &= -1.6 \times 0.8 \times 10^{-14} \times 5 \times (\vec{i} \times \vec{j}) \\ \vec{F}_B &= -6.4 \times 10^{-14} \vec{k} \end{aligned}$$

Q#2: A proton is moving with velocity of  $\vec{v} = (1.5 \vec{i} + 1.5 \vec{j}) \times 10^6$  m/s. It enters a region of a uniform magnetic field pointing in the negative  $z$  direction. What is the direction of a uniform electric field in the  $xy$  plane that will make the proton move un-deflected?

$$\begin{aligned} \vec{E} &= -(\vec{v} \times \vec{B}) = -[(1.5 \vec{i} + 1.5 \vec{j}) \times 10^6 \times B_3 (-\vec{k})] \\ &= B_3 [1.5 \times 10^6 [(\vec{i} \times \vec{k}) + (\vec{j} \times \vec{k})]] = 1.5 \times 10^6 B_3 [-\vec{j} + \vec{i}] \\ \vec{E} &= 1.5 \times 10^6 B_3 [\vec{i} - \vec{j}] \\ \theta &= \tan^{-1}(E_y/E_x) = \tan^{-1}\left(\frac{-1}{+1}\right) = 135^\circ \end{aligned}$$

Q#3: In Figure 9, a square loop of wire of side 0.50 m lies in the  $xy$  plane. The current in the loop is 0.25 A. There is a uniform magnetic field  $B$  in the positive  $y$  direction of magnitude 0.75 T. What is the torque on the loop?

$$\begin{aligned} \vec{B} &= 0.75 \vec{j} \\ \vec{\mu} &= i A (-\vec{k}) = 0.25 \times (0.5)^2 \times (-\vec{k}) \\ \vec{\mu} &= -0.0625 \vec{k} \end{aligned}$$



$$\begin{aligned} \tau &= \vec{\mu} \times \vec{B} = -0.0625 \vec{k} \times 0.75 \vec{j} \\ &= -0.0625 \times 0.75 \times (\vec{k} \times \vec{j}) \\ \vec{\tau} &= 0.0469 \vec{i} \end{aligned}$$

Q#1: An electron has a velocity:  $v = (5 \times 10^6 i - 3 \times 10^6 j) \text{ m/s}$  and moves through a uniform magnetic field:  $B = (0.5 i + 0.3 j) \text{ T}$ . Find the magnetic force (in Newtons) on the electron.

$$\begin{aligned} \vec{F}_B &= qv(\vec{v} \times \vec{B}) = -1.6 \times 10^{-19} (5 \times 10^6 i - 3 \times 10^6 j) \times (0.5 i + 0.3 j) \\ &= -1.6 \times 10^{-19} [5 \times 10^6 \times 0.3 (\vec{i} \times \vec{j}) - 3 \times 10^6 \times 0.5 (\vec{j} \times \vec{i})] \\ &= -4.8 \times 10^{-13} \vec{k} \end{aligned}$$

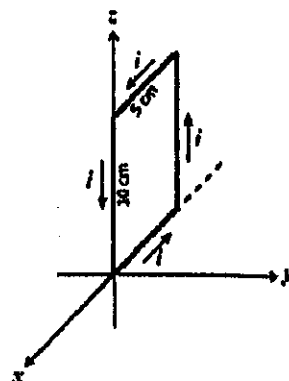
Q#2: An electron with a velocity  $v = 5.0 \times 10^7 i \text{ (m/s)}$  enters a region of space where perpendicular electric and magnetic fields are present. The electric field is  $E = -10^4 j \text{ (N/C)}$ . What magnetic field (in Tesla) will allow the electron to go through undeflected?

$$\begin{aligned} +\vec{E} &= q(\vec{v} \times \vec{B}) \\ +(-10^4 j) &= 5 \times 10^7 (\vec{i} \times \vec{B}) \\ -10^4 j &= 5 \times 10^7 (\vec{i} \times \vec{B}) \quad , \quad \vec{B} \text{ is in the direction of } \vec{k} \\ |\vec{B}| &= \frac{10^4}{5 \times 10^7} = 2 \times 10^{-4} \text{ T} \end{aligned}$$

Q#3: Figure 8 shows a 20-turn rectangular coil of dimensions 10 cm by 5.0 cm. It carries a current of 0.10 A, and is hinged along one long side. There is a uniform magnetic field  $B = 0.5 i \text{ T}$  in the region. In unit vector notation what is the torque acting on the coil about the hinge line?

$$\begin{aligned} \vec{B} &= 0.5 i \text{ T} \\ \mu &= NiA \vec{j} \\ &= 20 \times 0.1 \times 5 \times 10^{-2} \times j \\ &= 0.01 j \end{aligned}$$

$$\begin{aligned} \vec{\tau} &= \vec{\mu} \times \vec{B} \\ &= 0.01 j \times 0.5 i \\ &= 0.01 \times 0.5 (\vec{j} \times \vec{i}) \\ &= -0.005 \vec{k} = -5 \times 10^{-3} \vec{k} \end{aligned}$$



Quiz #10 Ch#28 T122 Phys102.28-30-v4

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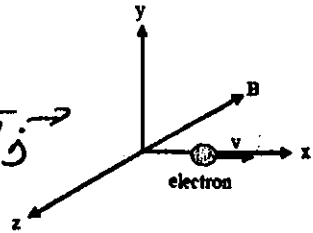
Section # .....

Q#1: In the figure, an electron of speed  $2.0 \times 10^5$  m/s moves along positive x axis in a uniform magnetic field of 0.2 T pointing into the page -z direction. The magnetic force on the electron is:

$$\vec{F}_B = q(\vec{v} \times \vec{B}), \quad v = 2 \times 10^5 \vec{i}; \quad B = -0.2 \text{ nT } \vec{k}$$

$$F_B = -1.6 \times 10^{-19} \left( (2 \times 10^5 \vec{i}) \times (-0.2 \vec{k}) \right)$$

$$= 0.64 \times 10^{-14} \times (\vec{i} \times \vec{k}) = -6.4 \times 10^{-15} \vec{j}$$



Q#2: The following figure shows a proton moving at a constant speed of 300 m/s along the negative x-axis through uniform electric and magnetic fields. The electric field is directed along the positive y-direction and has a magnitude of 900 N/C. What is the magnitude and direction of the magnetic field?

$$-\vec{E} = (\vec{v} \times \vec{B}) ; \quad v = 300(-\vec{i}) \text{ m/s}$$

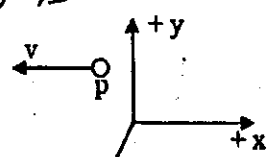
$$E = 900 \vec{j} \text{ N/C}$$

$$E = -(\vec{v} \times \vec{B})$$

$$900 \vec{j} = - (300(-\vec{i}) \times \vec{B})$$

$$3 \cdot 900 \vec{j} = 300 (\vec{i} \times \vec{B}) \quad (\text{B must be in } (-\vec{k}))$$

$$3 = B \Rightarrow \boxed{B = 3 \text{ T}}$$



Q#3 A single circular loop of radius 1.00 m carries a current of 10.0 mA. It is placed in a uniform magnetic field of magnitude 0.500 T that is directed parallel to the plane of the loop, as shown in FIGURE 8. What is the magnitude of the torque exerted on the loop by the magnetic field?

$$\vec{\mu} = NiA(-\vec{k})$$

$$= 1 \times 10 \times \pi R^2 \times (-\vec{k})$$

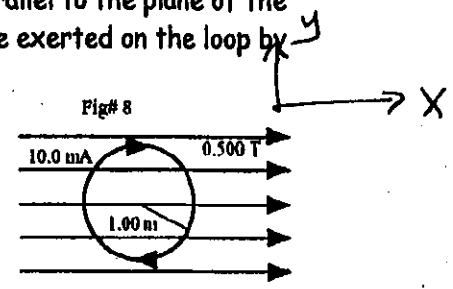
$$\vec{\mu} = 10\pi (-\vec{k}) \times 10^{-3}$$

$$\vec{B} = 0.5 \vec{i}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B} = 10\pi (-\vec{k}) \times 0.5 \vec{i} \times 10^{-3}$$

$$= 5\pi (-\vec{k} \times \vec{i}) \times 10^{-3} = 5\pi \times 10^{-3} (-\vec{j})$$

$$|\tau| = 5\pi \times 10^{-3} = 1.57 \times 10^{-2} \text{ N}\cdot\text{m}$$



Quiz #10 Ch#28 T122 Phys102.28-30-v5

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Q#1: What is the magnitude of the magnetic force on a charged particle ( $Q = +5.0 \mu\text{C}$ ) moving with a speed of 80 km/s in the positive  $x$  direction in a region containing a uniform magnetic field  $\vec{B}$  with components  $B_x = 5.0 \text{ T}$ ,  $B_y = 4.0 \text{ T}$ , and  $B_z = 3.0 \text{ T}$ ?

$$\vec{B} = 5\vec{i} + 4\vec{j} + 3\vec{k} ; v = 80 \text{ km/s} = 8 \times 10^4 \text{ m/s}$$

$$\vec{F}_B = q(\vec{v} \times \vec{B}) = 5 \times 10^{-6} \times (8 \times 10^4 \vec{i}) \times (5\vec{i} + 4\vec{j} + 3\vec{k})$$

$$= 40 \times 10^{-2} \times [4(\vec{i} \times \vec{j}) + 3(\vec{i} \times \vec{k})] = 0.4(4\vec{k} - 3\vec{j})$$

$$\vec{F}_B = 1.6\vec{k} - 1.2\vec{j} ; |\vec{F}_B| = \sqrt{(1.6)^2 + (1.2)^2} = 2 \text{ N}$$

Q#2: A proton travels through both a uniform magnetic field and a uniform electric field. The magnetic field is given by  $B = 2.5 \text{ i (mT)}$ . At one instant, the velocity of the proton is  $v = 2.0 \times 10^3 \text{ j (m/s)}$  and the net force acting on it is zero. Find the electric field in units of V/m. Ignore the gravitational force on the proton.

$$-\vec{E} = (\vec{v} \times \vec{B}) \Rightarrow \vec{E} = -(\vec{v} \times \vec{B})$$

$$\vec{E} = -((2 \times 10^3 \vec{j}) \times (2.5 \times 10^{-3} \vec{i}))$$

$$\vec{E} = -5(\vec{j} \times \vec{i}) = 5\vec{k}$$

Q#3: The coil in FIGURE 7 has its plane parallel to the  $xz$  plane, and carries current  $I = 1.0 \text{ A}$  in the direction indicated. The coil has 8.0 turns and a cross sectional area of  $4.0 \times 10^{-3} \text{ m}^2$ , and lies in an external uniform magnetic field that is given by  $B = -2\vec{i} \text{ (mT)}$ . Find the torque (in units of  $\mu\text{N}\cdot\text{m}$ ) on the coil due to the magnetic field.

$$\vec{\mu} = NIA(-\vec{j}) = 8 \times 1 \times 4 \times 10^{-3} \times (-\vec{j})$$

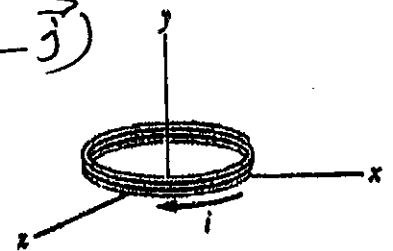
$$\vec{\mu} = -32\vec{j}$$

$$\vec{B} = -2\vec{i} \times 10^{-3} \text{ T}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

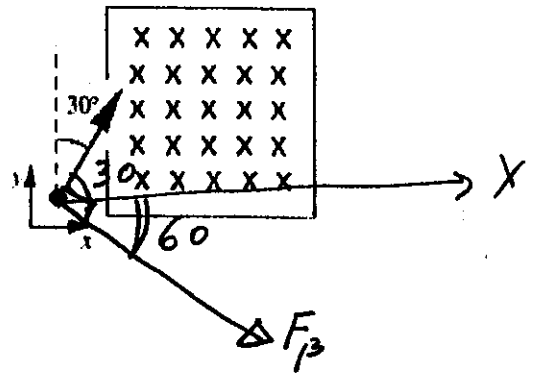
$$= (-32\vec{j}) \times (-2 \times 10^{-3} \vec{i})$$

$$= 64 \times 10^{-3} (\vec{j} \times \vec{i}) = -64\vec{k}$$



Q#1: An electron enters a region that contains a magnetic field directed into the page as shown in figure 7. The velocity of the electron makes an angle of 30 degrees with the +y axis. What is the direction of the magnetic force on the electron when it enters the field?

$\vec{F}_B$  60° below X-axis



Q#2: A uniform magnetic field of magnitude 2.0 T, directed along the positive y axis, crosses an electric field  $\vec{E}$ . What is magnitude and direction of the electric field needed to guide an electron with a speed of 30 m/s along a straight line in the positive x axis direction?

$$-\vec{E} = (\vec{v} \times \vec{B}) ; \vec{B} = 2\vec{j} \text{ T} ; v = 30\vec{i} \text{ m/s}$$

$$\vec{E} = -(\vec{v} \times \vec{B}) = -(30\vec{i} \times 2\vec{j}) = -60(\vec{i} \times \vec{j})$$

$$\vec{E} = -60\vec{k} = 60(-\vec{k}) = 60 \text{ V/m } (-\vec{k})$$

Q#3: A 20-turn coil, with an area of 1.5 m<sup>2</sup>, lies in the xz plane and carries a current  $I = 0.20 \text{ A}$  in the direction indicated in Figure 11. The coil is placed in a uniform magnetic field that lies in the xy plane and makes an angle of 30° with the +x-axis, and has a magnitude of 0.50 T. What is the torque on the coil?

$$\vec{B} = 0.5 \cos 30 \vec{i} + 0.5 \sin 30 \vec{j}$$

$$\vec{\mu} = NI A (-\vec{j})$$

$$= 20 \times 0.2 \times 1.5 (-\vec{j})$$

$$\vec{\mu} = -6\vec{j}$$

$$\tau = \vec{\mu} \times \vec{B} = -6\vec{j} \times (0.5 \cos 30 \vec{i} + 0.5 \sin 30 \vec{j})$$

$$= -6 \times 0.5 \times \cos 30 (\vec{j} \times \vec{i})$$

$$\tau = -2.6 \times (\vec{j} \times \vec{i}) = -2.6 \times (-\vec{k}) = 2.6\vec{k}$$

