

Name: \_\_\_\_\_

Solution

Serial # \_\_\_\_\_

1. Find the general solution of the following DE:

$$y^{(4)} + 3y'' - 4y = 0$$

The characteristic eq<sup>n</sup> is  $\lambda^4 + 3\lambda^2 - 4 = 0$

$$(\lambda - 1)(\lambda + 1)(\lambda^2 + 4) = 0$$

$$\lambda = 1, -1, 2i, -2i$$

the general solution is,

$$y = C_1 e^x + C_2 e^{-x} + C_3 \cos 2x + C_4 \sin 2x$$

$$\left. \begin{array}{l} 1 \left[ \begin{array}{ccccc} 1 & 0 & 3 & 0 & -4 \\ & 1 & 1 & 4 & 4 \\ \hline & 1 & 1 & 4 & 4 & 0 \end{array} \right. \end{array} \right\}$$

$$\Rightarrow (\lambda - 1)(\lambda^3 + \lambda^2 + 4\lambda + 4)$$

$$\left. \begin{array}{l} -1 \left[ \begin{array}{cccc} 1 & 1 & 4 & 4 \\ & -1 & 0 & -4 \\ \hline & 1 & 0 & 4 & 0 \end{array} \right. \end{array} \right\}$$

$$\Rightarrow (\lambda - 1)(\lambda + 1)(\lambda^2 + 4)$$