

ING FAHD UNIVERSITY OF PETROLEUM AND MINERALS
DEPARTMENT OF MATHEMATICS & STATISTICS
MATH 201-04
Quiz # 3

1. Identify (**2pts**) and sketch (**2pts**) the surface $z = \sqrt{1 + x^2 + y^2}$.

Solution:

$$\begin{aligned}z^2 &= 1 + x^2 + y^2 \\z^2 - x^2 - y^2 &= 1.\end{aligned}$$

Therefore, the surface is the upper half of a Hyperboid of two sheets.

2. (a) Change (**2pts**) $(\sqrt{3}, \frac{\pi}{3}, -1)$ From cylindrical to spherical coordinates.
(b) Change the equation $x = 3$ into Cylindrical coordinates(**2pts**).

Solution:

$$\begin{aligned}\rho &= \sqrt{r^2 + z^2} = 2, \\ \theta &= \frac{\pi}{3}, \\ \cos \varphi &= \frac{z}{\rho} = -\frac{1}{2}, \\ \varphi &= \frac{2\pi}{3}.\end{aligned}$$

Therefore $(\sqrt{3}, \frac{\pi}{3}, -1) \rightarrow (2, \frac{\pi}{3}, \frac{2\pi}{3})$.

(b)

$$\begin{aligned}x &= r \cos \theta \\ r \cos \theta &= 3 \\ r &= 3 \sec \theta.\end{aligned}$$

3. (**2pts**) Identify and sketch the surface $r^2 = r$.

Solution:

$$\begin{aligned}r^2 - r &= 0 \implies \\ r &= 1 \text{ or } r = 0.\end{aligned}$$

$r = 1$ is a circular cylinder of radius 1 with axis along the z -axis. $r = 0$ is the z -axis itself. Therefore, the surface is the union of the cylinder and the z -axis.