

Name:

ID:

Sec: 10

MATH-102

Term-142

Lcq-3

(Circle one letter and show all your work)

1) The average value of the function

$$f(x) = \frac{\tan x}{x^2 + 1} + \sqrt{4 - x^2} \text{ over the interval } [-2, 2] \text{ is}$$

- (a) 0
- (b) $\pi/4$
- (c) $\pi/3$
- (d) $\pi/2$**
- (e) π
- (f) None of the above

$$2) \int_0^1 \frac{e^{\tan^{-1} x}}{1 + x^2} dx =$$

- (a) $1 - e^{\pi/2}$
- (b) $e^\pi - \pi$
- (c) $e^{\pi/2} - 1$
- (d) $e^{-\pi/4} - 2$
- (e) $e^{\pi/4} - 1$**
- (f) None of the above

$$3) \int_0^1 (1+x)\sqrt{4-4x} dx =$$

- (a) 28/15**
- (b) 15/28
- (c) 14/15
- (d) 28/13
- (e) 15/13
- (f) None of the above

4) If g is a continuous function such that

$$\int_0^{2x} e^{t/2} g(t) dt = \frac{1}{2} x e^x, \text{ then } g(4) =$$

- (a) 4/3
- (b) 2/3
- (c) 3/2
- (d) 4/5
- (e) 3/4**
- (f) None of the above

5) The area of the region enclosed by the curves $y^2 = -x$ and the line $x + y + 2 = 0$ is equal to

- (a) 7/2
- (b) 0
- (c) 1
- (d) 9/2**
- (e) 5/2
- (f) None of the above

(Circle one letter and show all your work)

6) The area of the region enclosed by the curve $y = 4 - x^2$ and the lines $y = 2x - 4$ and $y = 4$ is equal to

- (a) $\int_0^4 ((4x - x^2) - (2x - 4)) dx$
- (b) $\int_2^4 ((y/2 + 2) - \sqrt{4 - y}) dx$
- (c) $\int_0^4 ((y/2 + 2) + \sqrt{4 - y}) dx$
- (d)** $\int_0^4 ((y/2 + 2) - \sqrt{4 - y}) dx$
- (e) $\int_0^2 ((2x - 4) - (4 - x^2)) dx$
- (f) None of the above

7) Let P be a partition of the interval $[0, 2]$, then the

limit $\lim_{\|P\| \rightarrow 0} \sum_{k=1}^n [c_k + c_k^2] \Delta x_k =$

- (a) $12/3$
- (b) **$14/3$**
- (c) $16/3$
- (d) $18/3$
- (e) $20/3$
- (f) None of the above

8) If $F(x) = \int_{1/2}^{2x} f(t) dt$ and $f(t) = \int_{1/2}^{t^2} \frac{\sqrt{1+u^2}}{u} dt$ then $F''(1) =$

- (a) $5\sqrt{17}$
- (b)** $4\sqrt{17}$
- (c) $3\sqrt{17}$
- (d) $2\sqrt{17}$
- (e) $\sqrt{17}$
- (f) None of the above

9) $\int_0^{\pi/4} (\sec x + \cos x)^2 dx =$

- (a)** $(5\pi+10)/8$
- (b) $(4\pi+10)/8$
- (c) $(3\pi+10)/8$
- (d) $(2\pi+10)/8$
- (e) $(\pi+10)/8$
- (f) None of the above

10) $\int \frac{\ln(\tan^{-1} x)}{(x^2 + 1) \tan^{-1} x} dx =$

- (a) $[\ln(\tan^{-1} x)]^2 + C$
- (b) $\frac{1}{2} [\ln(\tan^{-1} x)] + C$
- (c)** $\frac{1}{2} [\ln(\tan^{-1} x)]^2 + C$
- (d) $\frac{1}{2} [\tan^{-1} x]^2 + C$
- (e) $\ln(\tan^{-1} x) + C$
- (f) None of the above