

Name:

ID:

Sec: 10

MATH-102

Term-142

CQ-MAC

FORM A

(show all your work and circle one letter to get a full mark or you will get zero)

1) The interval of convergence of the series

$$\sum_{n=1}^{\infty} \frac{(x+1)^n}{n \cdot 2^n} \text{ is}$$

- (a)  $[-3,1)$
- (b)  $(-3,1]$
- (c)  $[-3,1]$
- (d)  $[-0.5,0.5]$
- (e)  $[-0.5,0.5)$
- (f) none of the above

2) If  $g(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$  then, the

coefficient of  $x^5$  in the Maclaurin series of  $\frac{g(x)}{1-x}$

is

- (a)  $-15/24$
- (b)  $11/24$
- (c)  $13/24$
- (d)  $-13/24$
- (e)  $-11/24$
- (f) none of the above

3) The power series representation for the function

$$f(x) = \frac{27x^2}{1+3x^2} \text{ is}$$

- (a)  $\sum_{n=0}^{\infty} (-1)^n 3^n x^{2n}$
- (b)  $\sum_{n=0}^{\infty} (-1)^n 3^{n+2} x^{2n+2}$
- (c)  $\sum_{n=0}^{\infty} (-1)^n 3^{n+3} x^{2n+2}$
- (d)  $\sum_{n=0}^{\infty} (-1)^n 3^{n+1} x^{2n+2}$
- (e)  $\sum_{n=0}^{\infty} \frac{(-1)^n 3^{n-2} x^{2n+2}}{2}$
- (f) none of the above

4) if the Maclaurin series of  $e^x \cos x$  is

$$A + Bx + Cx^2 + Dx^3 + \dots$$

then  $C+D =$

- (a)  $1/2$
- (b)  $2/3$
- (c)  $-1/3$
- (d)  $0$
- (e)  $1$
- (f) none of the above

5)  $\int \frac{1}{x^2} \cos(x^3) dx =$

- (a)  $\sum_{n=0}^{\infty} \frac{(-1)^n x^{6n-1}}{(2n)!(3n-1)}$   
 (b)  $\sum_{n=0}^{\infty} \frac{(-1)^n x^{6n-2}}{(2n)!(6n-2)}$   
 (c)  $\sum_{n=0}^{\infty} \frac{(-1)^n x^{6n-1}}{(2n+1)!(6n-1)}$   
 (d)  $\sum_{n=3}^{\infty} \frac{(-1)^n x^{6n-1}}{(2n)!(6n-1)}$   
 (e)  $\sum_{n=0}^{\infty} \frac{(-1)^n x^{6n-1}}{(2n)!(6n-1)}$   
 (f) none of the above

6) Let  $g(x) = x^3 \tan^{-1} x$  and let

$$g''(x) = \sum_{n=0}^{\infty} c_n x^n \quad \text{then } c_{10} =$$

- (a) 144/8  
 (b) 44/3  
 (c) 14/5  
 (d) 0  
 (e) 10  
 (f) none of the above

6) The radius of convergence of the series

$$\sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{2^{2n} (n!)^2} \quad \text{is}$$

- (a) 0  
 (b)  $\infty$   
 (c) 1  
 (d) 2  
 (e) 3  
 (f) none of the above

7) The radius of convergence of the series

$$\sum_{n=1}^{\infty} \frac{n!(x+1)^{2n}}{2} \quad \text{is}$$

- (a) 0  
 (b)  $\infty$   
 (c) 1  
 (d) 2  
 (e) 3  
 (f) none of the above

2) The interval of convergence of the series

$$\sum_{n=5}^{\infty} \frac{(-1)^n x^n}{4^n \cdot n^3} \quad \text{is}$$

- (a)  $[-5,5]$   
 (b)  $[-5,5)$   
 (c)  $(-5,5]$   
 (d)  $[-4,4]$   
 (e)  $(-4,4)$   
 (f) none of the above

4)  $1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6} + \dots =$

- (a)  $\pi/4$   
 (b) 1  
 (c)  $\ln(2)$   
 (d) e  
 (e) -1  
 (f) none of the above