

King Fahd University of Petroleum and Minerals  
Department of Mathematics and Statistics

**Calculus II**  
**EXAM I**  
**Semester II, Term 082**  
**Tuesday, March 31, 2009**  
**Net Time Allowed: 120 minutes**

**MASTER VERSION**

1. Using four rectangles and right end points, the estimated area under the graph of  $f(x) = 1 + \frac{x^2}{4}$  from  $x = -2$  to  $x = 6$  is

(a) 36

(b) 40

(c) 18

(d) 24

(e) 34

2.  $\int \frac{\cos^2 t}{1 + \sin t} dt =$

(a)  $t + \cos t + c$

(b)  $1 + \cos t + c$

(c)  $\frac{1}{2}t^2 - \cos t + c$

(d)  $t - \sin t + c$

(e)  $t - \frac{1}{2}\sin^2 t + c$

3.  $\int (2 - \sqrt{x})^2 dx =$

(a)  $4x - \frac{8}{3}\sqrt{x^3} + \frac{1}{2}x^2 + c$

(b)  $\frac{(2 - \sqrt{x})^3}{3} + c$

(c)  $4x + \frac{1}{2}x^2 + c$

(d)  $4x - x^{2/3} + \frac{1}{2}x^2 + c$

(e)  $4x - 6x^{3/2} + x^2 + c$

4.  $\int_4^{10} \frac{x}{x^2 - 4} dx =$

(a)  $\frac{3}{2} \ln 2$

(b)  $3 \ln 2$

(c)  $\frac{3}{4} \ln 2$

(d)  $\frac{1}{2} \ln 2$

(e)  $3 \ln 4$

5. If  $F(x) = \int_{\frac{1}{2}}^x f(t) dt$  and  $f(t) = \int_{\frac{1}{2}}^{t^2} \frac{\sqrt{1+u^2}}{u} du$ , then  $F''(1) =$

(a)  $2\sqrt{2}$

(b)  $\sqrt{2}$

(c)  $\frac{\sqrt{2}}{2}$

(d)  $3\sqrt{2}$

(e)  $\frac{\sqrt{2}}{6}$

6. If  $y = \int_{\sqrt{x}}^{x^3} \sqrt{t} \sin t dt$ , then  $\frac{dy}{dx} =$

(a)  $3\sqrt{x^7} \sin(x^3) - \frac{1}{2\sqrt[4]{x}} \sin \sqrt{x}$

(b)  $\sqrt{x^3} \sin x^3 - \sqrt[4]{x} \sin \sqrt{x}$

(c)  $\sqrt{x} \sin x^3 - \frac{1}{\sqrt[4]{x}} \sin \sqrt{x}$

(d)  $\sqrt{x^3} \sin \sqrt{x} - x^2 \sin x^3$

(e)  $x^3 \sin \sqrt{x} - \sqrt{x} \sin x^3$

7. Using the definition of the Area and definite integral, the value of the limit  $\lim_{n \rightarrow \infty} \sum_{i=1}^n e^{4+\frac{3i}{n}} \cdot \frac{2}{n}$  is [Hint: Express the limit as a definite integral].

(a)  $\frac{2}{3}[e^7 - e^4]$

(b)  $e^4$

(c)  $\frac{2}{3}e^{7/4}$

(d) does not exist

(e)  $e^{-3} + e^{-4}$

8. If  $f(x) = \begin{cases} x & 0 \leq x \leq 1 \\ \sqrt{1 - (x-1)^2} & 1 \leq x \leq 2 \end{cases}$ , and definite ingeral is interpreted as an area, then the value of the integral  $\int_0^2 f(x)dx$  is

(a)  $(2 + \pi)/4$

(b)  $(1 + \pi)/4$

(c)  $(3 + \pi)/4$

(d)  $(4 + \pi)/4$

(e)  $(5 + \pi)/4$

9.  $\int_{-1}^2 (x - 2|x|) dx =$

(a)  $-\frac{7}{2}$

(b)  $-\frac{9}{2}$

(c)  $-\frac{5}{2}$

(d)  $-\frac{3}{2}$

(e)  $\frac{5}{2}$

10.  $\int e^{(2x^5 + \ln x^4)} dx =$

(a)  $\frac{1}{10}e^{2x^5} + c$

(b)  $e^{(\ln x^4 + 2x^5)} + c$

(c)  $\frac{x^5}{5} + \frac{1}{3}x^6 + c$

(d)  $e^{(x^4 + 2x^5)} + c$

(e)  $\frac{10}{3}e^{(x^4 + 2x^5)} + c$

11.  $\int (\sec^2 x) \tan(\tan x) dx =$

(a)  $\ln |\sec(\tan x)| + c$

(b)  $\ln |\tan(\tan x)| + c$

(c)  $-\sec(\tan x) + c$

(d)  $\ln |\sin(\tan x)| + c$

(e)  $\ln(\sec^2 x) + c$

12. If  $\int_0^1 f(x) dx = \pi$ , then  $\int_0^{\pi/4} f(\sin 2x) \cos 2x dx$  is

(a)  $\frac{\pi}{2}$

(b)  $\frac{\pi}{4}$

(c)  $\pi$

(d)  $2\pi$

(e)  $4\pi$

13.  $\int_1^2 \frac{x^2 - 2x - 3}{x^4 - 3x^3} dx =$

(a)  $\frac{7}{8}$

(b)  $-\frac{1}{8}$

(c)  $\frac{9}{8}$

(d)  $-\frac{3}{8}$

(e)  $\frac{5}{8}$

14. The volume of the solid obtained by rotating the region bounded by the curves  $y = x^2$  and  $y^2 = x$  about the  $x$ -axis is equal to

(a)  $3\pi/10$

(b)  $37\pi/10$

(c)  $\pi/10$

(d)  $\pi/6$

(e)  $5\pi/6$



15. The base of a solid is the region  $s$  bounded by the curves  $y = \sqrt{x}$ ,  $y = 0$ ,  $x = 1$  and  $x = 2$ . If the cross-sections of the solid perpendicular to the  $x$ -axis are squares with one side lying along the base, then the volume of the solid is

(a)  $\frac{3}{2}$

(b) 2

(c) 1

(d)  $\frac{1}{2}$

(e)  $\frac{2}{3}(2\sqrt{2} - 1)$

16. The area enclosed by the line  $x + 2y = 1$  and the parabola  $y^2 = 4 - x$  is given by the definite integral

(a)  $\int_{-1}^3 (3 + 2y - y^2) dy$

(b)  $\int_{-1}^3 \left[ \frac{1}{2}(1 - x) - \sqrt{4 - x} \right] dx$

(c)  $\int_{-1}^3 (y^2 - 2y - 3) dy$

(d)  $\int_{-3}^4 \left[ \frac{1}{2}(1 - x) - \sqrt{4 - x} \right] dx$

(e)  $\int_{-3}^1 (3 - 2y + y^2) dy$

17. The volume of the solid obtained by rotating the region bounded by the curves  $y = \frac{1}{x}$ ,  $y = 0$ ,  $x = 1$  and  $x = 3$  about the line  $y = 1$  is

(a)  $2\pi \left( \ln 3 - \frac{1}{3} \right)$

(b)  $\pi \left( \ln 3 + \frac{1}{3} \right)$

(c)  $2\pi \left( \ln 3 - \frac{2}{3} \right)$

(d)  $\frac{2\pi}{3}$

(e)  $\pi \left( 2 \ln 3 - \frac{1}{3} \right)$

18. The area of the region in the right half of the plane bounded by the curves  $y = 2x - 1$ ,  $y = x^2$ , and  $y = -x$  is equal to

(a)  $\int_0^{1/3} (x^2 + x) dx + \int_{1/3}^1 (x^2 - 2x + 1) dx$

(b)  $\int_0^1 (x^2 - x + 1) dx$

(c)  $\int_0^{1/3} (x^2 - x) dx + \int_{1/3}^1 (x^2 + 2x - 1) dx$

(d)  $\int_0^1 (x^2 + x - 1) dx$

(e)  $\int_0^{1/3} (x - x^2) dx + \int_{1/3}^1 (x^2 - 2x - 1) dx$

19. If we use the definition of  $\ln x$  as a definite integral, then an approximation of  $\ln 2$  using two rectangles and the sample points to be midpoints is equal to
- (a)  $\frac{24}{35}$
  - (b)  $\frac{13}{15}$
  - (c)  $\frac{12}{35}$
  - (d)  $\frac{11}{15}$
  - (e)  $\frac{29}{35}$
20. The limit  $\lim_{n \rightarrow +\infty} \sum_{i=1}^n \frac{1}{i+n}$  can be interpreted as the
- (a) area under the graph of the function  $y = \frac{1}{x}$  on  $[2, 4]$
  - (b) area under the graph of the function  $y = \frac{1}{x}$  on  $[0, 3]$
  - (c) area under the graph of the function  $y = \ln x$  on  $[2, 4]$
  - (d) area under the graph of the function  $y = \ln x$  on  $[1, 3]$
  - (e) area under the graph of the function  $y = x$  on  $[2, 4]$