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sec: 5, 16

① The area of the surface obtained by rotating the curve $y = x^5$, $1 \leq x \leq 32$ about the x-axis is given by

(a) $\int_1^{32} 2\pi x^5 \sqrt{1+25x^8} dx$

(b) $\int_1^{32} 2\pi x^5 \sqrt{1+5x^4} dx$

(c) $\int_1^2 2\pi y \sqrt{1+25x^8} dy$

(d) $\int_1^2 2\pi \sqrt[5]{y} \sqrt{1+\frac{1}{25}y^{-8/5}} dy$

(e) $\int_1^{32} 2\pi x \sqrt{1+25x^8} dx$

② If $F(x) = \int_x^0 \sqrt{1+t^3} dt$ then $F'(1) =$

(a) $\sqrt{2}$

(b) $\sqrt{3}$

(c) $1-\sqrt{2}$

(d) $-\sqrt{2}$

(e) 0

③ The interval of convergence of the power series

$$\sum_{n=1}^{\infty} \frac{(2x+1)^n}{n} \quad |5$$

(a) $(-\frac{3}{2}, \frac{1}{2}]$

(b) $[-1, 0)$

(c) $[-\frac{3}{2}, \frac{1}{2})$

(d) $(-1, 0]$

(e) $[-\frac{3}{2}, \frac{1}{2}]$

④ The improper integral

$$\int_1^{\infty} \frac{x dx}{e^{px}}$$

is convergent

(a) diverges for all p

(b) $p < 0$

(c) $p > -3$

(d) $p < -3$

(e) $p > 0$

(5) The series $\sum_{n=1}^{\infty} \frac{\sin^2 n}{\pi n + n\sqrt{n}}$

- (a) diverges by integral test
- (b) is a convergent geometric
- (c) converges by the comparison test
- (d) is a convergent p-series
- (e) diverges by the test for divergence

(6) The Taylor series of $f(x) = \frac{1}{x+2}$ about $x = -1$

- (a) $\sum_{n=0}^{\infty} (-1)^n (x+1)^n$
- (b) $\sum_{n=0}^{\infty} (-1)^n (x+2)^n$
- (c) $\sum_{n=0}^{\infty} (-1)^n \cdot n! (x+1)^n$
- (d) $\sum_{n=0}^{\infty} \frac{(-1)^n}{n!} (x+1)^n$
- (e) $\sum_{n=0}^{\infty} \frac{(-1)^n}{n!} (x+2)^n$

(7) The volume generated by rotating the region bounded by the given curves

$$y = \frac{1}{x}, y = 0, x = 1, x = 4$$

about the y-axis

- (a) 7π
- (b) 6π
- (c) 5π
- (d) 4π
- (e) 3π

(8) $\int_{-2}^2 |1-x^2| dx =$

- (a) 1
- (b) 2
- (c) 3
- (d) 4
- (e) 5

(9) If R_n is the Riemann sum for $f(x) = 2 - \frac{1}{3}x$, $1 \leq x \leq 4$ with n rectangles and taking sample points to be the right endpoint then $R_n =$

- (a) $5 - \frac{1}{n} + \frac{3n+1}{n^2}$
- (b) $\frac{5}{3} - \frac{n+1}{n}$
- (c) $5 - \frac{n+1}{2n}$
- (d) $2 - \frac{n+1}{3n}$
- (e) $5 - \frac{3n+3}{2n}$