

(show all your work and circle one letter to get a full mark or you will get zero)

- 3) The sum of the absolute maximum and the absolute minimum values of the function

$$f(x) = 2x^3 + 3x^2 - 12x$$

is

- (a) 45
- (b) -33
- (c) 38**
- (d) -7
- (e) 35
- (f) none of the above

$$f'(x) = 6x^2 + 6x - 12 = 0$$

$$\Rightarrow x^2 + x - 2 = 0 \Rightarrow (x+2)(x-1) = 0$$

$\Rightarrow x = 1, x = -2$ are criticals

$$\text{Now, } f(x) = x[2x^2 + 3x - 12] = x[x(2x+3)-12]$$

2)

- The sum of all critical points of the function

$$(a) 49/12$$

$$(b) 19/4$$

$$(c) 10/12$$

$$(d) 5$$

$$(e) 3$$

$$(f) \text{none of the above}$$

$$f(x) = \frac{x^2 + 6}{\sqrt{4x-7}}$$

$$f' = 0 \Rightarrow (3x-2)(x+3) = 0$$

$$\backslash \quad x = 2/3 \text{ and } x = -3$$

$$f \text{ DNE} \Rightarrow x = 7/4$$

$$\text{Domain is } 4x-7 > 0 \Rightarrow x > 7/4$$

$$\text{so we have only one critical } x = \frac{2}{3}$$

$$f'(x) = \frac{2x\sqrt{4x-7} - \frac{2(x^2+6)}{\sqrt{4x-7}}}{(4x-7)} \times \frac{1}{\sqrt{4x-7}}$$

$$= \frac{2x(4x-7) - 2(x^2+6)}{(4x-7)\sqrt{4x-7}}$$

$$= \frac{6x^2 + 14x - 12}{(4x-7)\sqrt{4x-7}}$$

- 1) The sum of the absolute maximum and the absolute minimum values of the function

$$f(x) = \begin{cases} x^2 - 4x & \text{if } 0 \leq x < 5 \\ -x + 10 & \text{if } 5 \leq x \leq 6 \end{cases}$$

is

$$(a) 1$$

$$(b) 4$$

$$(c) 0$$

$$(d) 9$$

$$(e) 5$$

$$(f) \text{none of the above}$$

$$f'(x) = \begin{cases} 2x-4 & \text{if } 0 < x < 5 \\ -1 & \text{if } 5 < x < 6 \end{cases}$$

$$f'_-(5) = 6, f'_+(5) = -1 \Rightarrow f \text{ is not diff at } x=5$$

$$\Rightarrow x = 5 \text{ is critical point}$$

$$f'(x) = 0 \Rightarrow 2x-4 = 0 \Rightarrow x = 2 \in [0, 5]$$

$$\Rightarrow x = 2 \text{ is a critical point}$$

$$\begin{array}{cccc} x=0 & x=2 & x=5 & x=6 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ f(0)=0 & f(2)=-4 & f(5)=5 & f(6)=4 \end{array}$$

$$\text{largest } = 5, \text{ smallest } = -4 \Rightarrow \text{global max value } = 5 \quad \left\{ \begin{array}{l} \text{sum} = 1 \\ \text{global min value } = -4 \end{array} \right.$$

it is easy to evaluate using $f(x) = x[x(2x+3)-12]$
 not to use $f(x) = 2x^3 + 3x^2 - 12x$

$$\begin{array}{cccc} x=-3 & x=-2 & x=1 & x=3 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ f(-3)=9 & f(-2)=20 & f(1)=-7 & f(3)=45 \end{array}$$

$$\text{global max} + \text{global min} = 45 - 7 = 38$$