

SOLUTIONS

King Fahd University of Petroleum & Minerals
Department of Mathematical Science
STAT-211-Term042-I

Quiz #7
ID:

Section:
Serial:

Name:

Question One (5-Points)

Write **True** if the statement is true or **False** if not:

1. A 95 percent confidence interval estimate will have a margin of error that is approximately + 95 percent of the size of the population mean. **False**
2. Increasing the sample size will result in a point estimate that is closer to the true population value. **False**
3. In estimating a population proportion, the factors that are needed to determine the required sample size are the confidence level, the margin of error and some idea of what the population proportion is. **True**
4. The margin of error is the difference between the point estimate and the parameter. **False**
5. In estimating a population mean, increasing the confidence level will result in a higher margin of error for a given sample size. **True**

Question Two (5-Points)

The annual income for independent sales representatives in the United States is thought to be highly right-skewed, if a sample of 36 independent sales representatives is selected and yields a mean equal to \$144,300 and a standard deviation of \$32.45. Given this information,

1. Find 98 % confidence interval for the true mean.
2. Suppose it is known that the population standard deviation is \$32.45. Determine how many **more** items must be sampled to obtain the a confidence interval estimate for the population mean if the confidence level is 90 % with a margin of error of ± 2.5 .

$$1 - \alpha = 0.98 \Rightarrow Z_{\frac{\alpha}{2}} = Z_{.01} = 2.33$$

$$1. \text{ A 98\% C.I. for } \mu \text{ is : } \bar{X} \pm Z_{\frac{\alpha}{2}} \cdot \frac{S}{\sqrt{n}} = 144,300 \pm (2.33) \cdot \frac{32.45}{\sqrt{36}}$$

$$144,300 \pm 12.6014$$

$$144,287.4 \dots \dots \dots 144,312.6$$

$$1 - \alpha = 0.90 \Rightarrow Z_{\frac{\alpha}{2}} = Z_{.05} = 1.645$$

$$2. n = \left(\frac{Z_{\alpha/2} \cdot \sigma}{e} \right)^2 = \left(\frac{(1.645) \cdot (32.45)}{2.5} \right)^2 = 455.91 \approx 456$$

The number of additional items = 456 - 36 = 420