

Math 102
First Major Exam
Summer - 2000 **TIME : 75 Minutes**

1. If $f(x) = \frac{x^3}{x^2 - 1}$, then find x so $f^{-1}(x) = 2$.
2. Find $\frac{dy}{dx}$, if $y = e^{\cos^{-1}x} \ln xe^x$.
3. $\lim_{x \rightarrow 0} \frac{2^x e^x}{x^2}$
4. Sketch the region bounded by the curves $x = y^2$, and $y = x - 2$. And find its area.
5. Solve for x , where $e^{2x} - e^x - 6 = 0$.
6. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\tan x}{\sec x}$
7. Find the volume of the solid generated if the region bounded by the graphs of $y = \frac{1}{2}x$, $y = x - 1$, and $x = 3$ is revolving about the x axis.
8. $\frac{d}{dx} \int_{\tan x}^{\sqrt{x}} \frac{t^2}{t^2 - 2} dt$
9. Use logarithmic differentiation to find y' if $y = x^2 - 3 \sin x$.
10. Find the volume of the solid generated if the region bounded by the graphs of $y = \ln x$, $x = e$, and $y = 0$ is revolving about the y axis.

KFUPM — Math Dept

MATH 102-2

Summer 2001

Quiz 4 B

- (4pts)1. $\int \frac{1}{x^2 \sin \frac{1}{x}} dx$
 (3pts)2. $\int e^{3x} \cos 4x dx$
 (3pts)3. $\int \cot^3 x dx$

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Summer 1999(983)
MATH 102 Final Exam
Time: 2 $\frac{1}{4}$ hours

Name: _____
 ID #: _____ Section #: _____
 Serial #: _____

Notes:

The exam is composed of two parts:
 Part I multiple choice (13 questions).
 Part II solving (4 questions).

Do all the problems.

renewcommand	Quest.#	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
	Grade	4	4	4	4	4	4	4	4	4	4	4	4	4	4	6	4	4
	Marks																	

Total: _____/70

For questions 1 to 13, circle one of the choices:

renewcommand

1.	(a)	(b)	(c)	(d)	(e)
2.	(a)	(b)	(c)	(d)	(e)
3.	(a)	(b)	(c)	(d)	(e)
4.	(a)	(b)	(c)	(d)	(e)
5.	(a)	(b)	(c)	(d)	(e)
6.	(a)	(b)	(c)	(d)	(e)
7.	(a)	(b)	(c)	(d)	(e)
8.	(a)	(b)	(c)	(d)	(e)
9.	(a)	(b)	(c)	(d)	(e)
10.	(a)	(b)	(c)	(d)	(e)
11.	(a)	(b)	(c)	(d)	(e)
12.	(a)	(b)	(c)	(d)	(e)
13.	(a)	(b)	(c)	(d)	(e)

setcounter **Part I** Multiple-choice type questions (1–13)

Q1. Comment
$$\int_e^{e^2} \frac{1}{x \ln x^2} dx$$

setcounter

$\ln 2$ #

$\frac{\ln 2}{2}$ #

$e^2 e$ #

$\frac{e^2 - 1}{4e^4}$ #

$2e^2 e$ #

Q2. Comment
$$\int_1^8 \frac{1}{\sqrt{1 + \sqrt{x} - 1}} dx$$

setcounter

$\frac{16}{3}$ #

$\frac{232}{15}$ #

$\ln 2$ #

$\frac{22}{5}$ #

2 #

Q3. Comment
$$\int \frac{dx}{\sqrt{e^{2x} - 4}}$$

setcounter

$\frac{1}{2} \arcsin \frac{e^x}{2} + c$ #

$\arcsin \frac{e^x}{2} + c$ #

$\frac{1}{2} \operatorname{mbox} \frac{e^x}{2} + c$ #

$$\frac{1}{2} \int e^x dx = \frac{1}{2} e^x + c \quad \#$$

$$\int \frac{e^x}{2} dx = \frac{1}{2} e^x + c \quad \#$$

Q4. Comment If $f(x) = e^x \sin x$, then $2f(x) - 3f(x)$ is:
 setcounter

$$e \quad \#$$

$$2e \quad \#$$

$$2e \quad \#$$

$$0 \quad \#$$

$$e \quad \#$$

Q5. The area of the region inside the graph of $r = 2 - 2\cos \theta$ is given by:
 setcounter

$$\int_0^{2\pi} (2 - 2\cos \theta)^2 d\theta \quad \#$$

$$\int_0^{2\pi} 2(2 - 2\cos \theta)^2 d\theta \quad \#$$

$$\int_0^{2\pi} \frac{1}{2}(2 - 2\cos \theta)^2 d\theta \quad \#$$

$$\int_0^{2\pi} 2 - 2\cos \theta d\theta \quad \#$$

$$\int_0^{2\pi} \frac{1}{2} (2 - 2\cos \theta)^2 d\theta \quad \#$$

Q6. Comment If the region bounded by the graphs of $y = \sqrt{x}$, and $y = \frac{1}{2}x$ is revolved about the line $x = 1$, then the volume of the solid generated by using the shell method is given by:
 setcounter

$$\int_0^4 2\pi(x-1) \left(\sqrt{x} - \frac{1}{2}x \right) dx \quad \#$$

$$\int_0^2 2\pi(x-1) \left(\sqrt{x} - \frac{1}{2}x \right) dx \quad \#$$

$$\int_0^4 \pi(x-1) \left(\sqrt{x} - \frac{1}{2}x \right) dx \quad \#$$

$$\int_0^4 2\pi(x-1) \left(\sqrt{x} - \frac{1}{2}x \right) dx \quad \#$$

$$\int_0^2 \pi(x-1) \left(\sqrt{x} - \frac{1}{2}x \right) dx \quad \#$$

Q7. Comment $\int_0^{\pi/6} \tan^4 2x dx$
 setcounter

$$\frac{\sqrt{3}}{2} - \frac{1}{2} \quad \#$$

$$\frac{\sqrt{3}}{2} - \frac{1}{6} \quad \#$$

$3\sqrt{3}$	$\frac{1}{6}$	#
	$\frac{1}{6}$	#
$2\sqrt{3}$	$\frac{1}{6}$	#

Q8. Comment One of the following is False: setcounter

- mbox #
- mbox #
- mbox #
- mbox #
- mbox #

Q9. Comment The number of points of intersection between the polar curves $r = \cos 4\theta$ and $r = \frac{1}{2}$ are:

setcounter

- 2 #
- 4 #
- 8 #
- 12 #
- 16 #

Q10. $\lim_{x \rightarrow 0} (1 - 2 \sin x)^{1/3x}$

setcounter

- mbox #
- $e^{2/3}$ #
- e #
- $e^{3/2}$ #
- 1 #

Q11. Comment The sequence $\{\sqrt{4n^2 - 3n} - 2n\}$ is:

setcounter

- mbox #
- mbox #
- mbox #
- mbox #
- mbox #

Q12. Comment The point at which the parametric curve $x = \tan^{-1} t, y = 5 \cosh 3t, t \in \mathbb{R}$ has a horizontal tangent is:

setcounter

$$5,0 \quad \#$$

$$0,15 \quad \#$$

$$3,5 \quad \#$$

$$\left(\frac{1}{2}, 5\right) \quad \#$$

$$0,5 \quad \#$$

- Q13. Comment If the region bounded by the graphs of $y = x^2 - 1$, and the x -axis is revolved about the x -axis, then the volume is given by:

setcounter

$$\int_{-1}^1 x^4 dx \quad \#$$

$$\int_{-1}^1 (x^4 - 1) dx \quad \#$$

$$\int_{-1}^1 (1 - x^2)^2 dx \quad \#$$

$$2 \int_0^1 (1 - x^2)^2 dx \quad \#$$

$$2 \int_{-1}^1 (1 - x^2)^2 dx \quad \#$$

Part II. Solving questions:

- Q14. Comment $\int \frac{\sinh^3 x}{\cosh^2 x} dx$

- Q15. Comment Sketch the region R in the 1st quadrant between the graphs of $y = 2^x$, y -axis, x -axis and $x = 2$. Find the area of R .

- Q16. Comment Determine whether the series $\sum_{n=1}^{\infty} \frac{e^{2n}}{2n-1!}$ is convergent or divergent.

- Q17. Comment $\int x\sqrt{4x^2 - 9} dx$