# N-Gram: Part 1 ICS 482 Natural Language Processing 

Lecture 7: N-Gram: Part 1

Husni Al-Muhtaseb

# بسم اله الرحمن الرحيم <br> ICS 482 Natural Language Processing 

Lecture 7: N-Gram: Part 1<br>Husni Al-Muhtaseb

## NLP Credits and Acknowledgment

These slides were adapted from presentations of the Authors of the book

## SPEECH and LANGUAGE PROCESSING:

An Introduction to Natural Language Processing, Computational
Linguistics, and Speech Recognition
and some modifications from presentations found in the WEB by several scholars including the following

# NLP Credits and Acknowledgment 

If your name is missing please contact me muhtaseb

At
Kfupm.
Edu.

## NLP Credits and

|  | echestampeint | Khurshid Ahmad | Martha Palmer |
| :---: | :---: | :---: | :---: |
| Martin | Björn Gambäck | Staffan Larsson | julia hirschberg |
| Jig Martin | Christian Korthals | Robert Wilensky | Elaine Rich |
| Dan Jurafsky | Thomas G. Dietterich |  | Christof Monz |
| Siway Fong | Devika Subramanian | Feiyu Xu | Bonnie J. Dorr |
|  | Duminda Wijesekera | Jakub Piskorski | Nizar Habash |
|  | Lee McCluskey | Rohini Srihari | Massimo Poesio |
| M y-Angela Papalaskari | David J. Kriegman | Mark Sanderson | David Goss-Grubbs Thomas K Harris |
|  | Kathleen McKeown | Andrew Elks | John Hutchins |
|  | Michael J. Ciaraldi | Marc Davis | Alexandros |
| ata Subramaniam | David Fin | Ray Larson | Potamianos <br> Mike Rosner |
| tin | er-So | Jimmy Lin | Latifa Al-Sulaiti |
| uce R. Maxim | Franz J. Kurfess | Marti Hearst | Giorgio Satta |
| . | Tim Finin | Andrew McCallum | Cristopher Manning |
| th Srinivas | Nadjet Bouayad | Nick Kushmerick | Hinrich Schütze |
| eon Ntafos | Kathy McCoy | Mark Craven | Alexander Gelbukh |
| Paolo Pirjanian | Hans Uszkoreit | Chia-Hui Chang | Gina-Anne Levow |
| Rigrardo Vilalta | Azadeh Maghsoodi | Diana Maynard | Qitao Gao |
| Tom Lenaerts |  | James Allan | $\underset{\text { Zeynep Altan }}{\text { Qing Ma }}$ |

## Previous Lectures

- Pre-start questionnaire
- Introduction and Phases of an NLP system
- NLP Applications - Chatting with Alice
- Regular Expressions, Finite State Automata, and Regular languages
- Deterministic \& Non-deterministic FSAs
- Morphology: Inflectional \& Derivational
- Parsing and Finite State Transducers
- Stemming \& Porter Stemmer


## Today's Lecture

- 20 Minute Quiz
- Words in Context
- Statistical NLP - Language Modeling
- N Grams


## NLP - Machine Translation



## Where we are?

Discussed individual words in isolation

- Start looking at words in context
- An artificial task: predicting next words in a sequence


## Try to complete the following

- The quiz was ------
- In this course, I want to get a good -----

Can I make a telephone -----

- My friend has a fast -----
- This is too -------
- الوقت كالسيف إن لم تقطعه -------

لا إله إلا أنت سبحانك إني كنت من -------

## Human Word Prediction

- Some of us have the ability to predict future words in an utterance

How?

- Domain knowledge
- Syntactic knowledge
- Lexical knowledge


## Claim

- A useful part of the knowledge is needed to allow Word Prediction (guessing the next word)
- Word Prediction can be captured using simple statistical techniques
- In particular, we'll rely on the notion of the probability of a sequence (e.g., sentence) and the likelihood of words co-occurring


## Why to predict?

- Why would you want to assign a probability to a sentence or...
- Why would you want to predict the next word...
- Lots of applications


## Lots of applications

- Example applications that employ language models:
- Speech recognition
- Handwriting recognition
- Spelling correction
- Machine translation systems
- Optical character recognizers


## Real Word Spelling Errors

- Mental confusions (cognitive)
- Their/they're/there
- To/too/two
- Weather/whether
- Typos that result in real words
- Lave for Have


## Real Word Spelling Errors

- They are leaving in about fifteen minuets to go to her horse. horse: house, minuets: minutes
- The study was conducted mainly be John Black be: by
- The design an construction of the system will take more than a year. an: and
- Hopefully, all with continue smoothly in my absence. With: will
- I need to notified the bank of.... notified: notify
- He is trying to fine out. fine: find


## Real Word Spelling Errors

- Collect a set of common pairs of confusions
- Whenever a member of this set is encountered compute the probability of the sentence in which it appears
- Substitute the other possibilities and compute the probability of the resulting sentence
- Choose the higher one


## Mathematical Foundations

Reminder

3/19/2008

## Motivations

- Statistical NLP aims to do statistical inference for the field of NL

Statistical inference consists of taking some data (generated in accordance with some unknown probability distribution) and then making some inference about this distribution.

## Motivations (Cont)

- An example of statistical inference is the task of language modeling (ex how to predict the next word given the previous words)
- In order to do this, we need a model of the language.
- Probability theory helps us finding such model


## Probability Theory

- How likely it is that an A Event (something) will happen
- Sample space $\Omega$ is listing of all possible outcome of an experiment
- Event A is a subset of $\Omega$
- Probability function (or distribution)

$$
P: \Omega \rightarrow[0,1]
$$

## Prior Probability

Prior (unconditional) probability: the probability before we consider any additional knowledge

$$
P(A)
$$

## Conditional probability

- Sometimes we have partial knowledge about the outcome of an experiment
- Conditional Probability
- Suppose we know that event B is true
- The probability that event A is true given the knowledge about B is expressed by

$$
P(A \mid B)
$$

## Conditionals Defined

Conditionals

$$
P(A \mid B)=\frac{P\left(A^{\wedge} B\right)}{P(B)}
$$

Rearranging

$$
P\left(A^{\wedge} B\right)=P(A \mid B) P(B)
$$

And also

$$
\begin{aligned}
P\left(A^{\wedge} B\right) & =P(B \mid A) P(A) \\
P\left(A^{\wedge} B\right)=P\left(B^{\wedge} A\right) & =P(B \mid A) P(A)
\end{aligned}
$$

## Conditional probability (cont)

$$
\begin{aligned}
P(A, B) & =P(A \mid B) P(B) \\
& =P(B \mid A) P(A)
\end{aligned}
$$

- Joint probability of A and B.


## Bayes' Theorem

- Bayes' Theorem lets us swap the order of dependence between events
We saw that $\quad P(A \mid B)=\frac{P(A, B)}{P(B)}$
Bayes' Theorem:

$$
P(A \mid B)=\frac{P(B \mid A) P(A)}{P(B)}
$$

## Bayes

. We know...

- So rearranging things

$$
\begin{aligned}
& P(A \wedge B)=P(A \mid B) P(B) \\
& \text { and }
\end{aligned}
$$

$$
\begin{gathered}
P(A \wedge B)=P(B \mid A) P(A) \\
P(A \mid B) P(B)=P(B \mid A) P(A)
\end{gathered}
$$

$$
P(A \mid B)=\frac{P(B \mid A) P(A)}{P(B)}
$$

## Bayes

## "Memorize" this

$$
P(A \mid B)=\frac{P(B \mid A) P(A)}{P(B)}
$$

## Example

- S:stiff neck, M: meningitis
- $\mathrm{P}(\mathrm{S} \mid \mathrm{M})=0.5, \mathrm{P}(\mathrm{M})=1 / 50,000 \mathrm{P}(\mathrm{S})=1 / 20$
- Someone has stiff neck, should he worry?

$$
\begin{aligned}
& P(M \mid S)=\frac{P(S \mid M) P(M)}{P(S)} \\
& \quad=\frac{0.5 \times 1 / 50,000}{1 / 20}=0.0002
\end{aligned}
$$

## More Probability

-The probability of a sequence can be viewed as the probability of a conjunctive event -For example, the probability of "the clever student" is:
$P($ the $\wedge$ clever $\wedge$ student $)$

## Chain Rule

conditional probability: $\quad P(A \mid B)=\frac{P(A \wedge B)}{P(B)}$

$$
P(A \wedge B)=P(B \mid A) P(A)
$$

$$
\begin{aligned}
& P(A \wedge B)=P(A \mid B) P(B) \\
& \text { and } \\
& P(A \wedge B)=P(B \mid A) P(A)
\end{aligned}
$$

"the student":

$$
P(\text { The } \wedge \text { student })=P(\text { student } \mid \text { the }) P(\text { the })
$$

"the student studies": $P($ The $\wedge$ student $\wedge$ studies $)=$ $P($ The $) P($ student $\mid$ The $) P($ studies $\mid$ The $\wedge$ student $)$

## Chain Rule

the probability of a word sequence is the probability of a conjunctive event.

$$
\begin{aligned}
P\left(w_{1}^{n}\right)= & P\left(w_{1}\right) P\left(w_{2} \mid w_{1}\right) P\left(w_{3} \mid w_{1}^{2}\right) \ldots P\left(w_{n} \mid w_{1}^{n-1}\right) \\
& =\prod_{k=1}^{n} P\left(w_{k} \mid w_{1}^{k-1}\right)
\end{aligned}
$$

Unfortunately, that's really not helpful in general. Why?

## Markov Assumption

$$
P\left(w_{n} \mid w_{1}^{n-1}\right) \approx P\left(w_{n} \mid w_{n-N+1}^{n-1}\right)
$$

- $P\left(W_{n}\right)$ can be approximated using only $\mathrm{N}-1$ previous words of context
- This lets us collect statistics in practice
- Markov models are the class of probabilistic models that assume that we can predict the probability of some future unit without looking too far into the past
- Order of a Markov model: length of prior context


## Corpora

- Corpora are (generally online) collections of text and speech
- e.g.
- Brown Corpus (1M words)
- Wall Street Journal and AP News corpora
- ATIS, Broadcast News (speech)
- TDT (text and speech)
- Switchboard, Call Home (speech)
- TRAINS, FM Radio (speech)


## Counting Words in Corpora

- Probabilities are based on counting things, so ....
- What should we count?
- Words, word classes, word senses, speech acts ...?
- What is a word?
- e.g., are cat and cats the same word?
- September and Sept?
- zero and 0 ?
- Is seventy-two one word or two? AT\&T?
- Where do we find the things to count?


## Terminology

- Sentence: unit of written language
- Utterance: unit of spoken language
- Wordform: the inflected form that appears in the corpus
- Lemma: lexical forms having the same stem, part of speech, and word sense
- Types: number of distinct words in a corpus (vocabulary size)
- Tokens: total number of words


## Training and Testing

- Probabilities come from a training corpus, which is used to design the model.
- narrow corpus: probabilities don't generalize
- general corpus: probabilities don't reflect task or domain
- A separate test corpus is used to evaluate the model, typically using standard metrics
- held out test set
- cross validation


## Simple N-Grams

An N-gram model uses the previous $\mathrm{N}-1$ words to predict the next one:

- $P\left(w_{n} \mid w_{n-1}\right)$
- Dealing with $P(<$ word $>\mid<$ some prefix $>)$
unigrams: $P($ student $)$
- bigrams: $P($ student $\mid$ clever $)$
trigrams: $P($ student $\mid$ the clever) quadrigrams: $P($ student $\mid$ the clever honest $)$


