- Describe the benefits of a virtual memory system
- Explain the concepts of demand paging, page replacement algorithms, and allocation of page frames


## Outline

- Background
- Demand Paging
- Copy-on-Write
- Page Replacement
- Allocation of Frames
- Thrashing
- Demand Segmentation
- Operating System Examples

Note: Most of the slides are compiled from the textbook and its complementary resources

## Background

- All memory management strategies have the same goal to keep many processes in memory simultaneously to allow multiprogramming and hence increase the CPU utilization
- Memory management is required because instructions must be in physical memory to be executed
- Put the entire process in physical memory (problem: limited memory)
- Dynamic loading can ease this restriction (requires extra work by the programmer)
- Virtual memory is a technique that allows the execution of processes that are not completely in memory
- Creates illusion of a "virtual" memory that can be larger than real memory but still nearly as fast

Background (cont.)

- Virtual memory separation of user logical memory from physical memory.
- Only part of the program needs to be in memory for execution.
- Logical address space can therefore be much larger than physical address space.
- Potentially as big as a disk, but normally constrained by the address size [ $2^{32}=4 \mathrm{~GB}$ ]

- Advantages:
- Processes can be larger can physical memory in the system
- Programmers need not worry about the memory storage limitations
- Allows address spaces to be shared by several processes.
- Allows for more efficient process creation. Allows processes to share files
- Disadvantages
- Not easy to implement
- May substantially decrease the performance if it is used carelessly
$\qquad$

Shared Library Using Virtual Memory


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- Virtual memory can be implemented via:
- Demand paging
- Demand segmentation
- Bring a page into memory only when it is needed during program execution
- Less physical memory needed
- Reduce the swap time and thus has faster response
- Accommodate more users
- A swapper manipulates the entire process, whereas a pager (a lazy swapper) manipulates just individual pages associated with a process
- Page is needed $\Rightarrow$ reference to it
- invalid reference $\Rightarrow$ abort
- not-in-memory $\Rightarrow$ bring to memory

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Transfer of a Paged Memory to Contiguous Disk Space

Each page table entry has a validinvalid bit is associated
( $1 \Rightarrow$ inmemory, $0 \Rightarrow$ not-inmemory)

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Steps in Handling a Page Fault


## Example

- Memory access time = 100 nanoseconds
- Average page-fault service $=25$ microseconds
- Then:

$$
\begin{aligned}
\text { EAT } & =(1-p) \times 100+p \times 25,000,000 \\
& =100+24,999,900 p
\end{aligned}
$$

Activity: What should be the value for $p$ if we want the performance degradation to be less than $10 \%$ ?

- Copy-on-Write (COW) allows both parent and child processes to initially share the same pages in memory

If either process modifies a shared page, only then is the page copied

- COW allows more efficient process creation as only modified pages are copied
- Free pages are allocated from a pool of zeroed-out pages


## Page Replacement

- Prevent over-allocation of memory by modifying pagefault service routine to include page replacement
- Use modify ( dirty) bit to reduce overhead of page transfers - only modified pages are written to disk
- Page replacement completes separation between logical memory and physical memory - large virtual memory can be provided on a smaller physical memory


## Page Replacement Algorithms

1. Find the location of the desired page on disk
2. Find a free frame:
3. If there is a free frame, use it
4. If there is no free frame, use a page replacement algorithm to select a victim frame; write the victim frame to the disk, change the page and frame tables accordingly
5. Read the desired page into the (newly) free frame; Update the page and frame tables
6. Restart the user process

- Many page replacement algorithms exist
- Want lowest page-fault rate
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
- Reference strings are either generated randomly or using by tracing a given system
- As the number of frames available to the process increases, the number of
page faults decreases

Page Replacement Algorithms (cont.)

- Replacement algorithms
- FIFO Page Replacement (the simplest)
- Optimal Page Replacement (OPT or MIN)
- Least Recently Used (LRU) Page Replacement
- LRU Approximation Page Replacement
- Counting algorithms (not commonly used)
- Least frequently used (LFU) algorithm
- Most frequently used (MFU) algorithm


## FIFO Algorithm

- Replaces the oldest page in the memory
- Easy to understand and program
- Performance is not always good
- Suffer from Belady's anomaly
- Given reference string
- $7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1$
- Number of frames is 3
- Allocation and replacement


Num of page faults $=15$

## Another Example (cont.)

- FIFO Replacement suffers from Belady's Anomaly
- more frames does not guarantee less page faults!!!



## Another Example

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- 3 frames ( 3 pages can be in memory at a time per process)

| 1 | 1 | 4 | 5 |  |
| :--- | :--- | :--- | :--- | :--- |
| 2 | 2 | 1 | 3 | 9 page faults |
| 3 | 3 | 2 | 4 |  |

- 4 frames

| 1 | 1 | 5 | 4 |  |
| :--- | :--- | :--- | :--- | :--- |
| 2 | 2 | 1 | 5 | 10 page faults |
| 3 | 3 | 2 |  |  |
| 4 | 4 | 3 |  |  |
|  |  |  |  |  |

Optimal Algorithm

- Replace the page that will not be used for the longest period of time
- Has the lowest page fault rate
- Never suffer from Belady's anomaly
- Difficult to implement
- it requires future knowledge of the reference string
- Used for measuring how well other algorithms perform (benchmark)


## Optimal Algorithm (cont.)

- Given reference string
- $7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1$
- Number of frames is 3
- Allocation and replacement


Num of page faults = 9

Least Recently Used (LRU) Algorithm

- FIFO uses the past (looks backward)
- OPT uses the future (looks forward)
- LRU uses the recent past as an approximation of the near future
- Replace the page that has NOT been used for the longest period of time
- Counter implementation
- Every page entry has a counter; every time the page is referenced through this entry, copy the clock into the counter
- When a page needs to be changed, look at the counters to determine which are to change
- 4 frames example
$1,2,3,4,1,2,5,1,2,3,4,5$

| 1 | 4 |
| :--- | :--- |
| 2 |  |
| 3 |  |
| 4 |  |
|  |  |$\quad$|  |
| :--- |$\quad$|  |
| :--- |

- Example

- Another example:
- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

$$
\begin{array}{|l|l|l|}
\hline 1 & 5 & \\
\cline { 1 - 1 } 2 & & \\
\cline { 1 - 1 } & 5 & \\
\hline & 5 & 4 \\
\cline { 1 - 1 } & 3 & \\
\hline
\end{array}
$$

## LRU Algorithm (Cont.)

- Stack implementation: keep a stack of page numbers in a double link form. If a page is referenced, then move it to the top. At worst, we require 6 pointers to be changed
- No search for replacement and does not suffer from Belady's anomaly
- Requires hardware support



## LRU Approximation Algorithms

- Some systems provide no hardware support for LRU
- Many system provide some help in the form of a reference bit
- With each page associate a bit, initially $=0$
- When page is referenced bit set to 1
- Replace the one which is 0 (if one exists). We do not know the order, however.
- Record reference bits at regular interval can provide ordering information
- Second-chance algorithm
- Need reference bit
- Clock replacement
- If page to be replaced (in clock order) has reference bit $=1$ then:
- set reference bit 0
- leave page in memory
- replace next page (in clock order), subject to same rules
- A pointer indicates which page needs to be replaced next
- When a frame is needed, the pointer is advanced until it finds a page with reference bit $=0$
- As the pointer advances, it clears the reference bits



## Counting Algorithms

- Keep a counter of the number of references that have been made to each page:
- Least Frequently Used (LFU) Algorithm:
- Replaces page with the smallest count
- An actively used page should have a large reference number
- Most Frequently Used (MFU) Algorithm
- Replaces page with the highest count
- Based on the argument that the page with the smallest count was probably just brought in and has yet to be used
- Not commonly used: expensive implementation + not approximating OPT


## Allocation of Frames

- Each process needs minimum number of pages
- Example: IBM 370-6 pages to handle move instruction:
- instruction is 6 bytes, might span 2 pages
- 2 pages to handle from
- 2 pages to handle to
- Major allocation schemes
- Fixed allocation (equal, proportional)
- Priority allocation


## Fixed Allocation

## Priority Allocation

- Equal allocation: e.g., if 100 frames and 5 processes, give each 20 pages
- Proportional allocation: Allocate according to size of process
$s_{i}=$ size of process $p_{i}$
$m=64, \quad s_{i}=10, s_{2}=127$
$S=\sum s_{i}$
$m=$ total number of frames
$a_{i}=$ allocation for $p_{i}=\frac{s_{i}}{S} \times m$
$a_{1}=\frac{10}{137} \times 64 \approx 5$
$a_{2}=\frac{127}{137} \times 64 \approx 59$
- Both depend on the degree of multiprogramming
- Use a proportional allocation scheme using priorities rather than size
- A high priority process is given more frames to speed its execution
- If process $P_{i}$ generates a page fault
- Select for replacement one of its frames
- Select for replacement a frame from a process with lower priority number


## Local vs. Global Allocation

- Local replacement:
- Each process selects from only its own set of allocated frames
- The number of frames allocated to each process does not change
- Can hinder a process by not making available to it a less used page
- Global replacement:
- Process selects a replacement frame from the set of all frames
- One process can take a frame from another
- A process can increase its frames on the expense of other unfortunate processes
- Thus a process can not control its fault rate; it depends not only on its paging behavior but also on other processes
- Generally results in greater system throughput and hence it is more common

Thrashing (cont.)

- Thrashing is a high paging activity that may occur when the number of frames allocated to a process is below the minimum number of frames required to support its execution
- A process is thrashing if it is busy spending more time paging than executing
- Can we limit the effects of thrashing?
- Use local replacement algorithm
- Provide a process as many frames as possible?? How??
- Working-set strategy which is based the assumption of locality
- A locality is a set of pages that are actively used together


## Working-Set Model

- The working set strategy prevents thrashing while keeping the degree of multiprogramming as high as possible
- $\Delta \equiv$ working-set window $\equiv$ a fixed number of page references Example: 10,000 instruction
- WSS ( working set size of Process $P_{i}$ ) $=$ total number of pages referenced in the most recent $\Delta$ (varies in time)


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## The Page-Fault Frequency (PFF) Strategy

- Define an upper bound $U$ and lower bound $L$ for page fault rates
- Allocate more frames to a process if fault rate is higher than $U$
- Allocate less frames if fault rate is $<\mathrm{L}$
- The resident set size should be close to the working set size $W$
- We suspend the process if the PFF > U and no more free frames are available



## Memory-Mapped Files



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## Another Consideration

- A program structure example:
- Array $A[1024,1024]$ of integer. Each row is stored in one page
- Program 1


## for $j:=1$ to 1024 do

for $i:=1$ to 1024 do
A $[i, j]:=0 ;$

- $1024 \times 1024$ page faults

A[1,1], A[1,2],..,A[1,1024]

- Program 2 A[2,1], A[2,2],..,A[2,1024]
for $i:=1$ to 1024 do
for $j:=1$ to 1024 do
$\mathrm{A}[i, \mathrm{f}]:=0 ;$
- 1024 page faults

A[1024,1],A[1024,2],...,A[1024,1024]

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