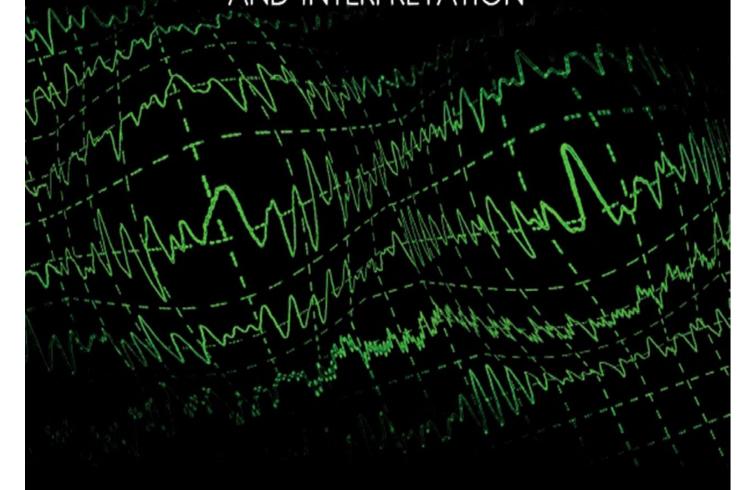




# REFLECTION SEISMOLOGY:

THEORY, DATA PROCESSING AND INTERPRETATION



**WENCAI YANG** 

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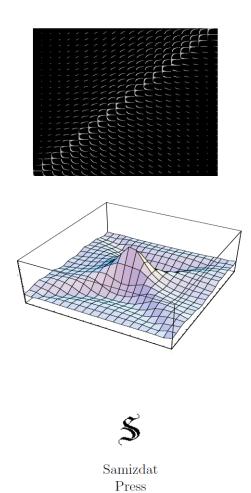
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