



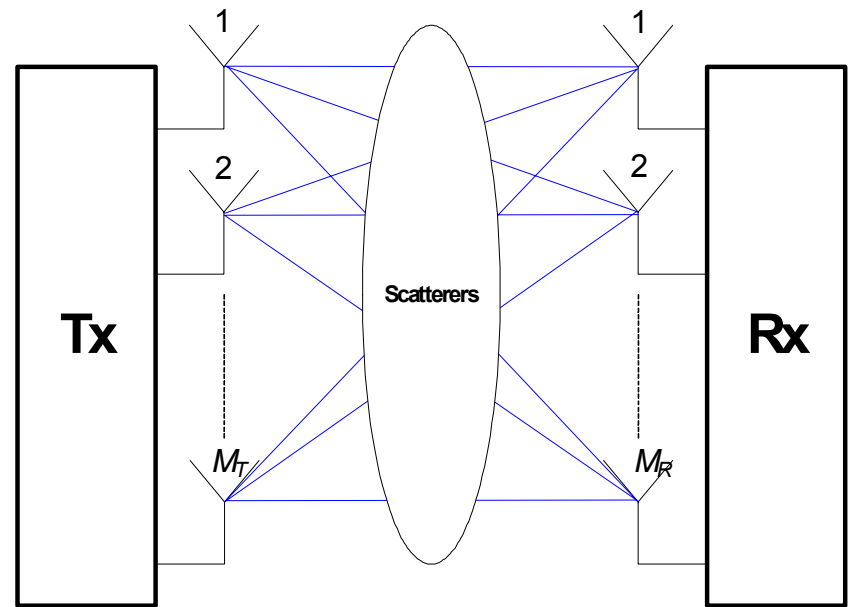
# Comparative Study of MIMO-OFDM Uplink Scheduling Criteria

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# Introduction: Multiple Input Multiple Output (MIMO) Channels

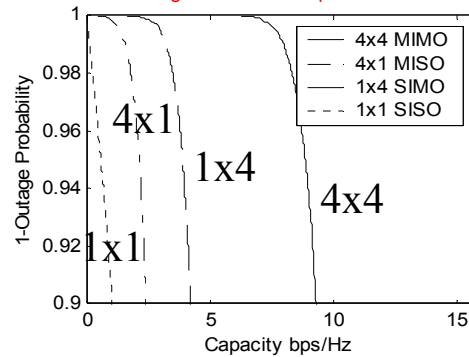
- A MIMO channel is a wireless link between  $M_T$  transmit and  $M_R$  receive antennas.
- MIMO channels boost the information capacity of wireless systems by order of magnitude [Telater95][Foschini98].



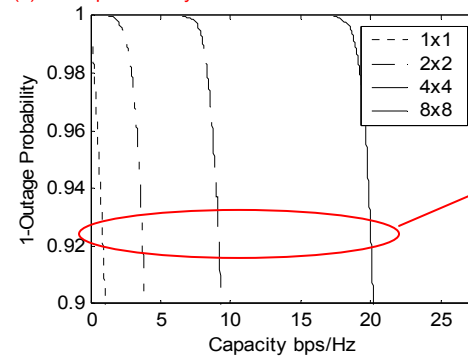
$$\mathbf{H}(t) = \begin{pmatrix} h_{11}(t) & \dots & h_{1M_T}(t) \\ \vdots & \ddots & \vdots \\ h_{M_R1}(t) & \dots & h_{M_RM_T}(t) \end{pmatrix}$$

# MIMO Capacity

(a) Complementary CDF at SNR=10dB; Fading Channels Comparisons

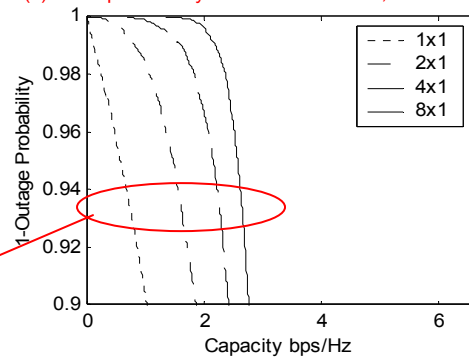


(b) Complementary CDF at SNR=10dB for MIMO Channels



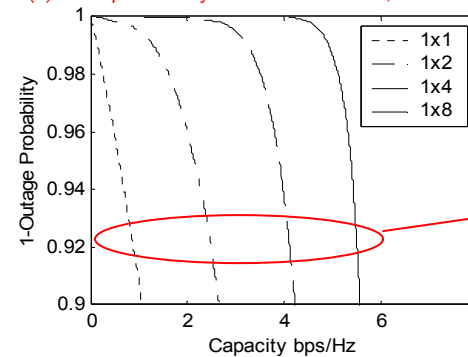
Doubling number of antennas, doubles the information capacity

(c) Complementary CDF at SNR=10dB; MISO Channels



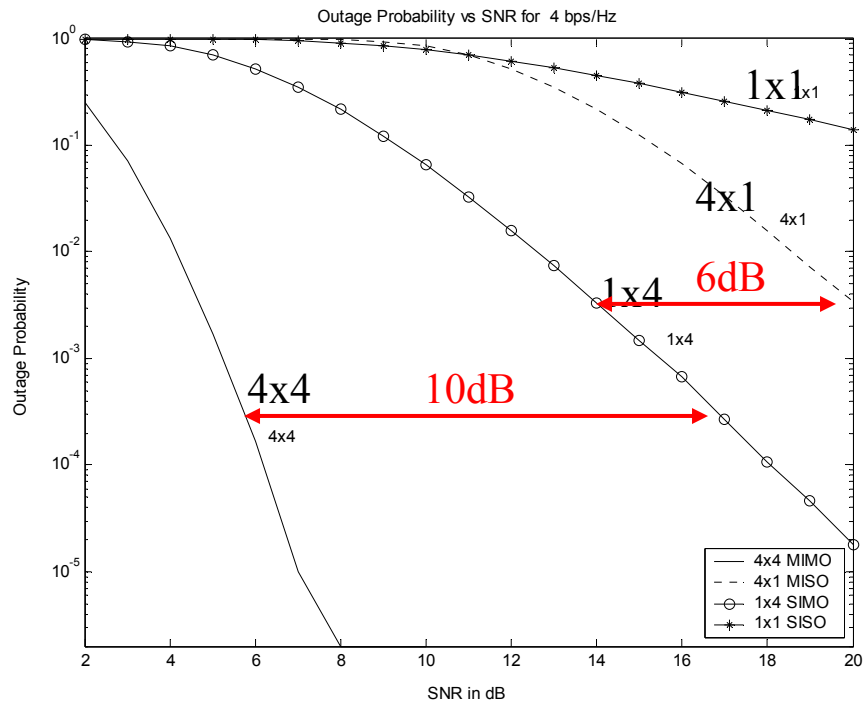
Diminishing returns

(d) Complementary CDF at SNR=10dB; SIMO Channels

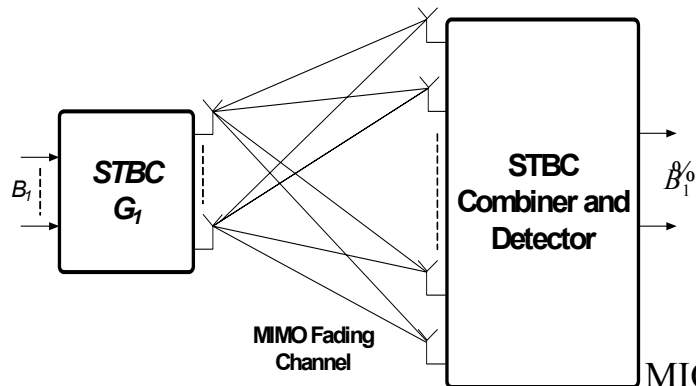
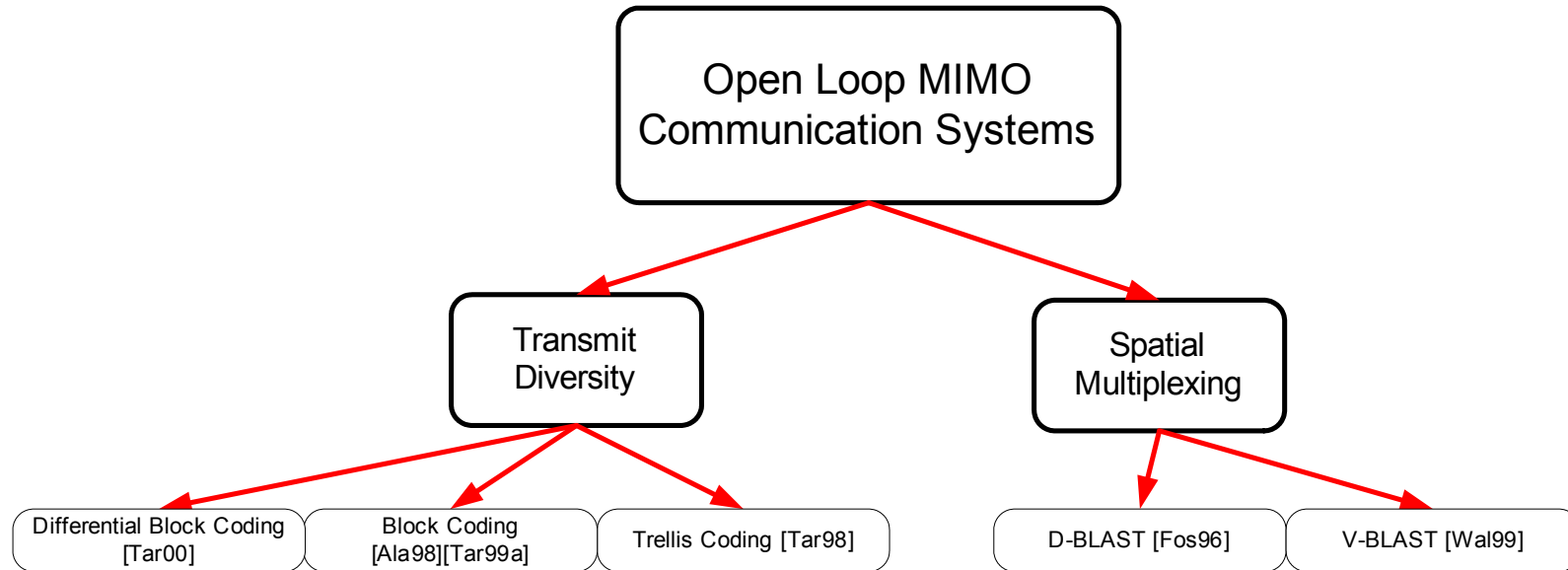


Good gains but not comparable to MIMO

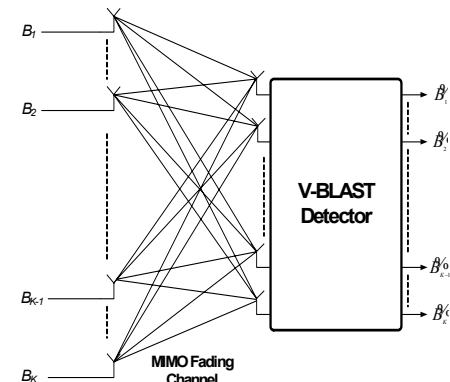
# MIMO Outage Probability



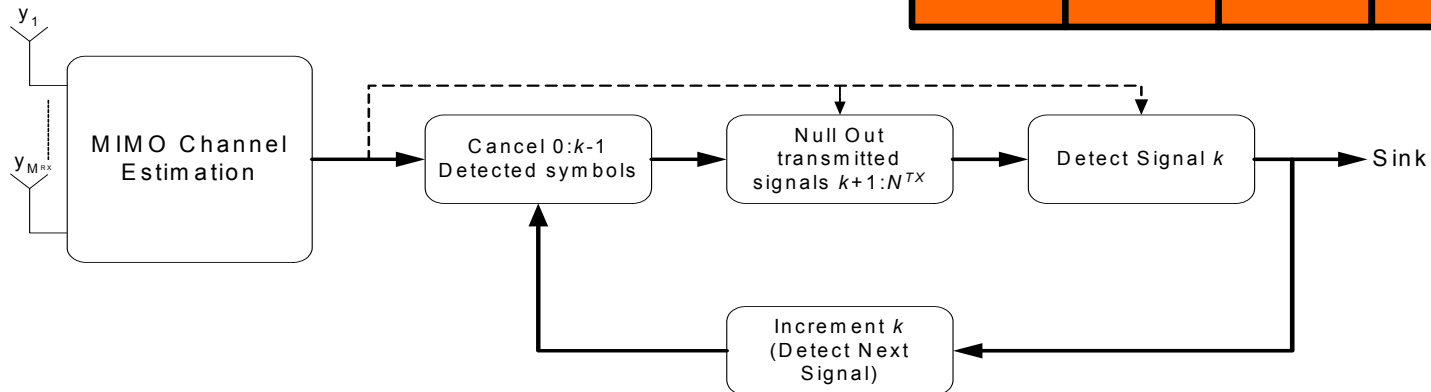
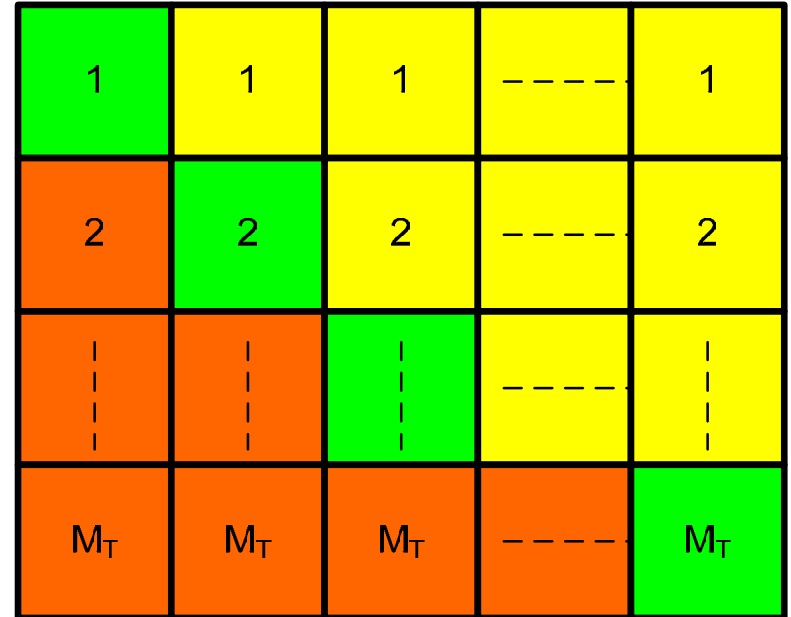
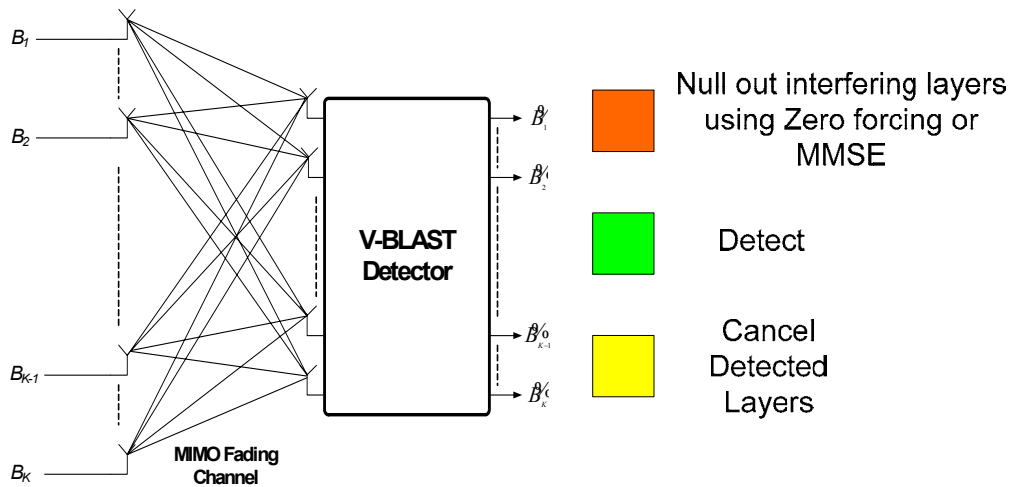
# Introduction: Open Loop MIMO Communication Systems



MICCC09 S. Al-Ghadhban



# Vertical BellLabs LAYERed Space Time (VBLAST) architecture



# Uplink Scheduling for Multiuser Systems with Spatial Multiplexing

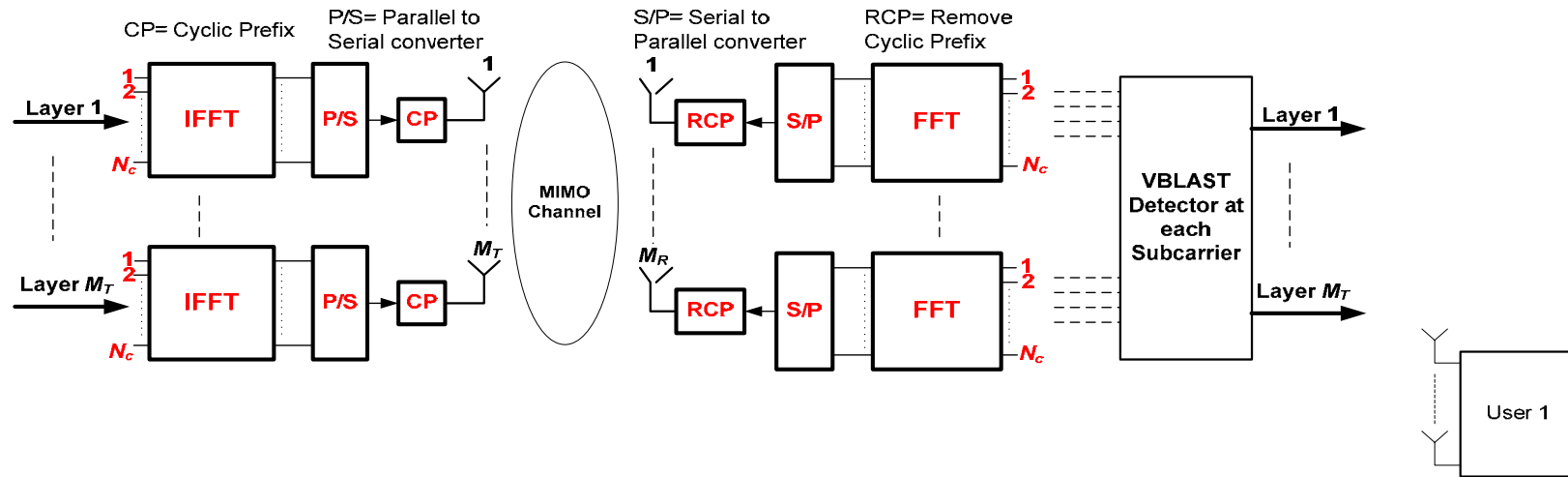
- In a multiuser environment, each user has different channel statistics.
- Scheduling transmission to the user with the best channel condition at each time leads to a form of selection diversity known as multiuser diversity.
- In SISO, MaxSNR scheduling maximizes the capacity of the uplink [Kno95] and downlink [Tse97].

## Our focus is on

- Scheduling for uplink MIMO-OFDM system.
- Scheduling and STBC aren't a good match [Gozali03].
- We focus on scheduling for spatial multiplexing systems selecting a single user at a time and we focus on practical detection algorithms, specifically V-BLAST.

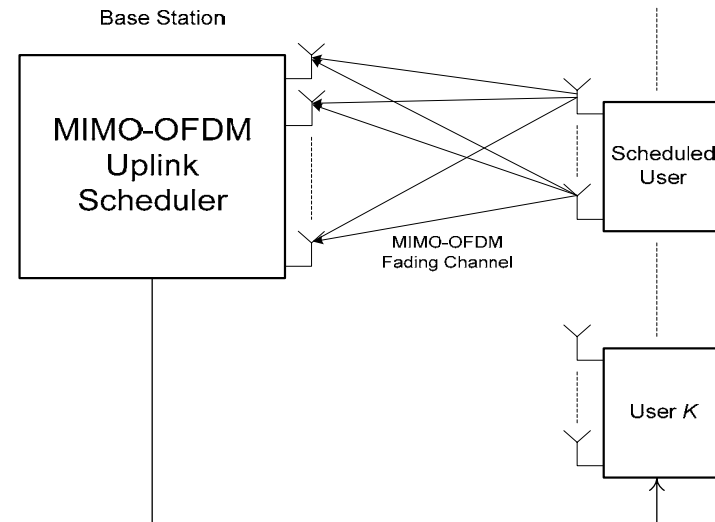


# System Model



the received signal for user  $k$  and at the  $i^{th}$  subcarrier is :

$$\mathbf{y}_{k,i} = \mathbf{H}_{k,i} \mathbf{x}_{k,i} + \boldsymbol{\eta}_{k,i}$$



# Scheduling Algorithms

- **Optimal MIMO capacity** maximizing scheduler

$$\max_{k=1,\dots,K} \left\{ \min_{i=1,\dots,N_c} \left\{ \log_2 \left( \det \left( \mathbf{I}_{M_R} + \frac{SNR}{M_T} \mathbf{H}_{k,i} \mathbf{H}_{k,i}^H \right) \right) \right\} \right\}$$

- **MaxSNR** scheduler selects the user with maximum MIMO channel power

$$\max_{k=1,\dots,K} \left\{ \min_{i=1,\dots,N_c} \left\{ \text{trace}(\mathbf{H}_{k,i} \mathbf{H}_{k,i}^H) \right\} \right\}$$

- **Round robin** scheduling allows each user to transmit in a time-division fashion regardless of their channel condition.

# Scheduling Algorithms

- **V-BLAST capacity** maximizing scheduler

V-BLAST capacity is dominated by the weakest layer [Pap02]

$$C_{VBLAST}^{ZF} = M_T \cdot \min_{i=1,2,K,M_T} \left\{ \log_2 \left( 1 + \frac{SNR}{M_T \|\mathbf{W}_{ZF,i}\|^2} \right) \right\}$$

Thus, the scheduler selects the user with

$$\max_{k=1,\dots,K} \left\{ \min_{i=1,\dots,N_c} \left\{ C_{VBLAST}^{ZF} \left( \mathbf{H}_{k,i} \right) \right\} \right\}$$

# Scheduling Algorithms

- **MinMaxES: Minimum Eigenspread**

$$\min_{k=1,\dots,K} \left\{ \max_{i=1,\dots,N_c} \left\{ s \left( \mathbf{H}_{k,i} \mathbf{H}_{k,i}^H \right) \right\} \right\} \text{ where } s \left( \mathbf{H}_{k,i} \mathbf{H}_{k,i}^H \right) = \lambda_{\max} / \lambda_{\min}$$

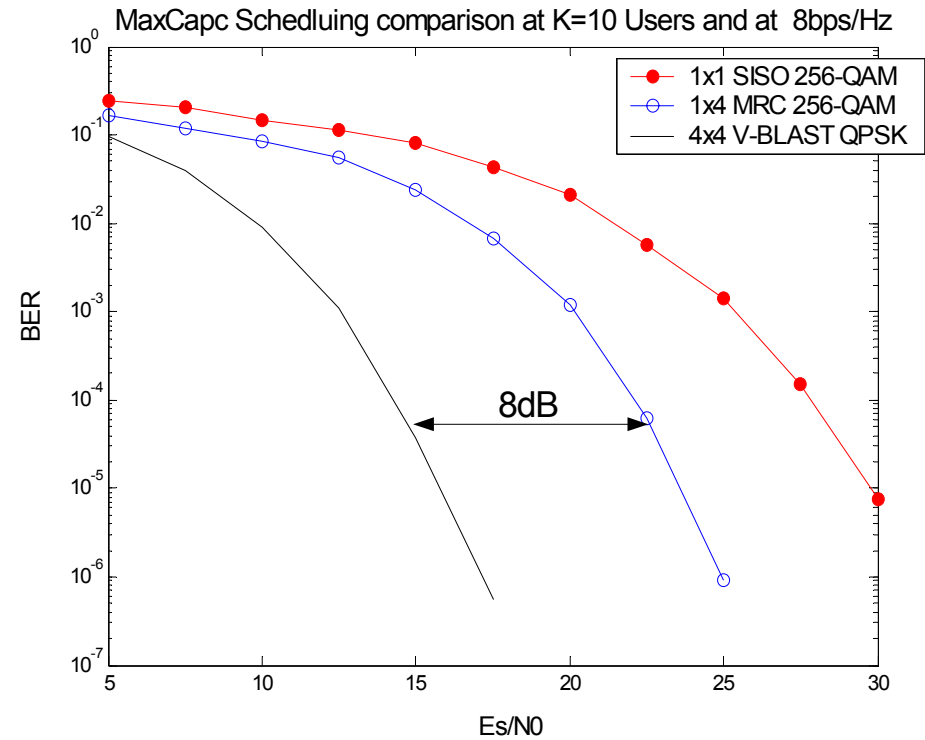
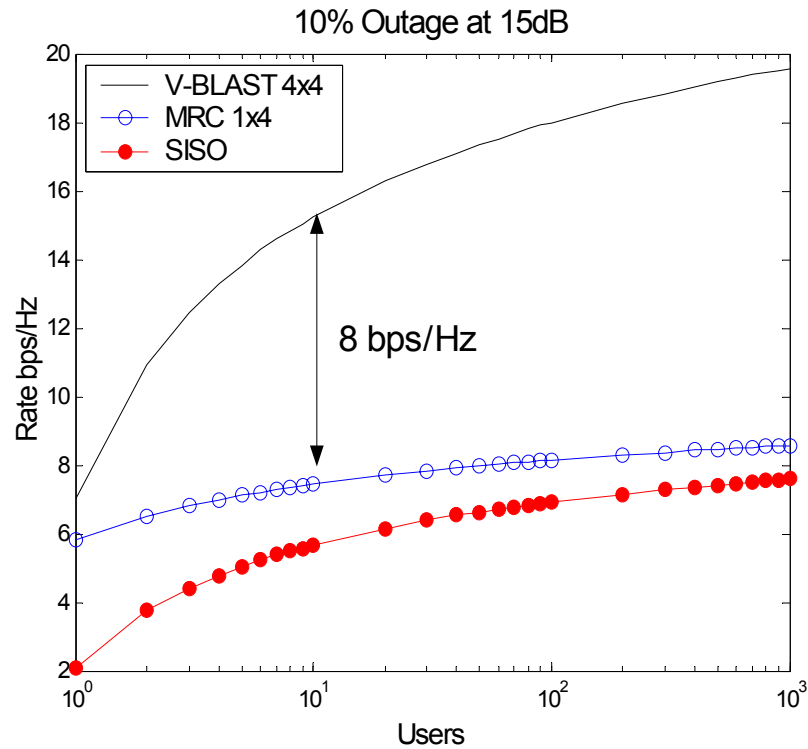
$\lambda_{\max}$  and  $\lambda_{\min}$  are the largest and smallest eigenvalues of  $\mathbf{H}_k \mathbf{H}_k^H$

- **MaxMinSV: Maximum Minimum Singularvalue**

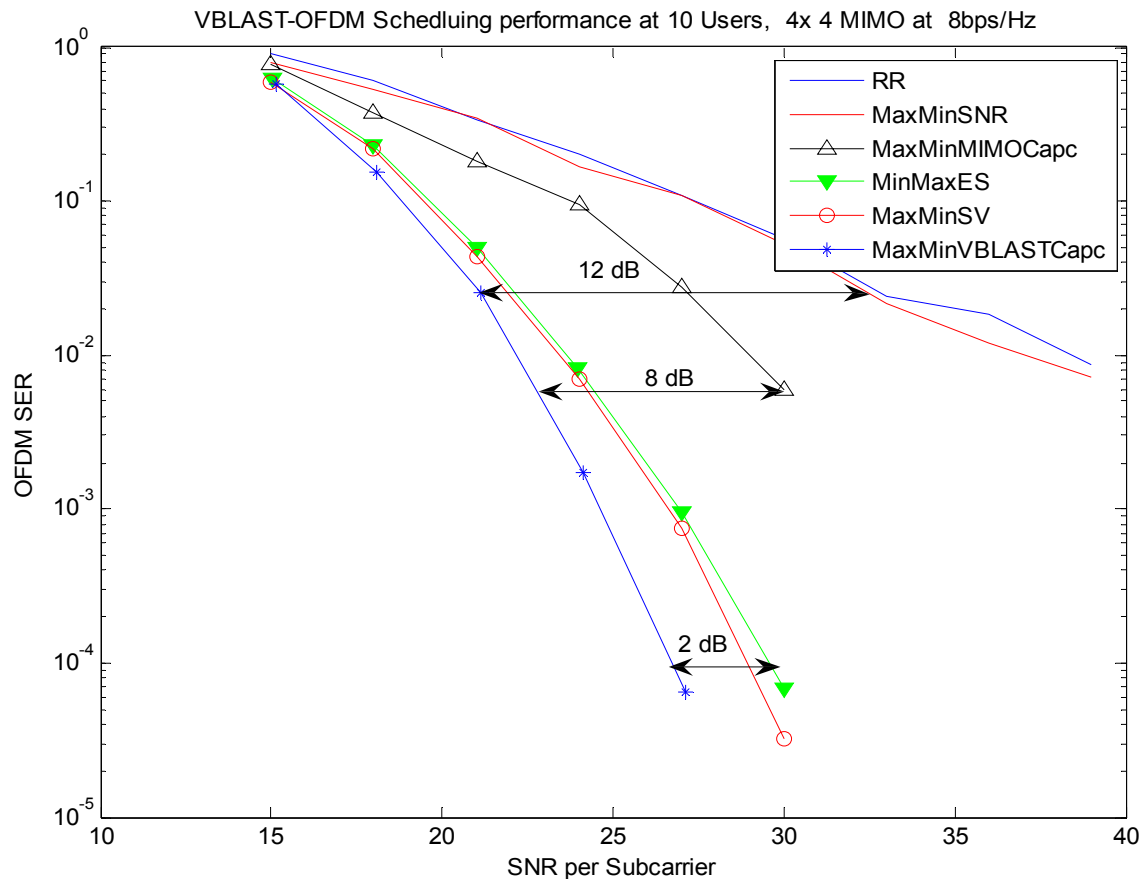
$$\max_{k=1,\dots,K} \left\{ \min_{i=1,\dots,N_c} \left\{ \rho_{\min} \left( \mathbf{H}_{k,i} \right) \right\} \right\} \text{ where } \rho_{\min} = \frac{\rho_{\max}}{\sqrt{s}}$$

$\rho_{\min}$  is the smallest singularvalue of  $\mathbf{H}_{k,i}$

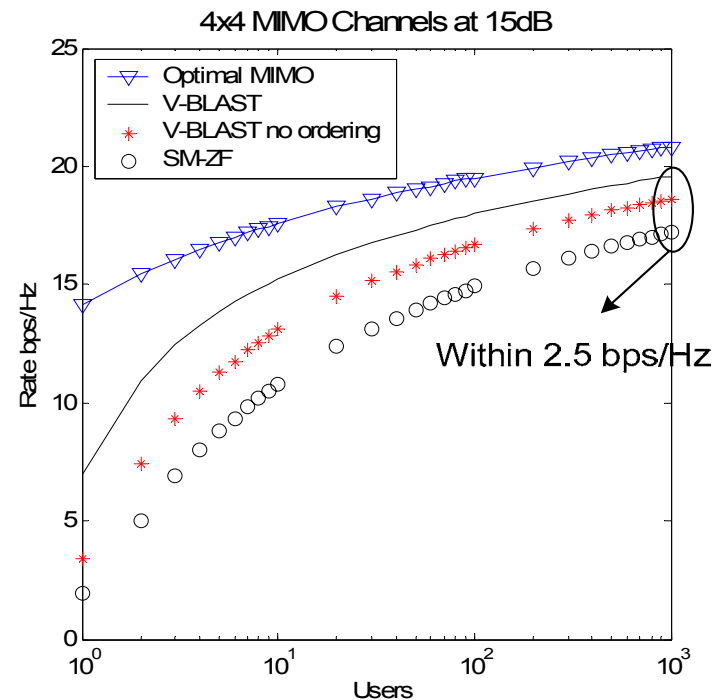
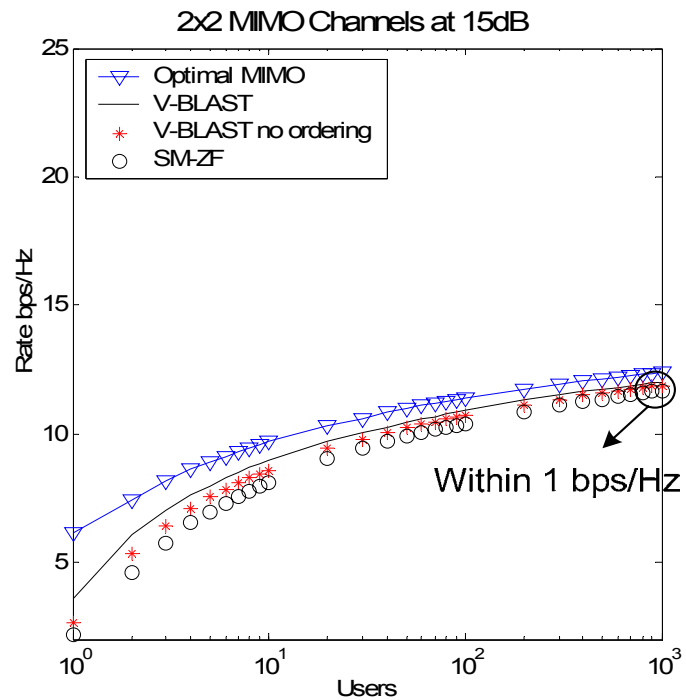
# Advantage of V-BLAST compared to SISO and SIMO systems



# Aggregate OFDM SER of 4x4 QPSK MIMO-OFDM uplink scheduling at 64 subcarriers and over FSC of length four



# Effect of Suboptimal Detection



# Scheduling and Fairness Issue

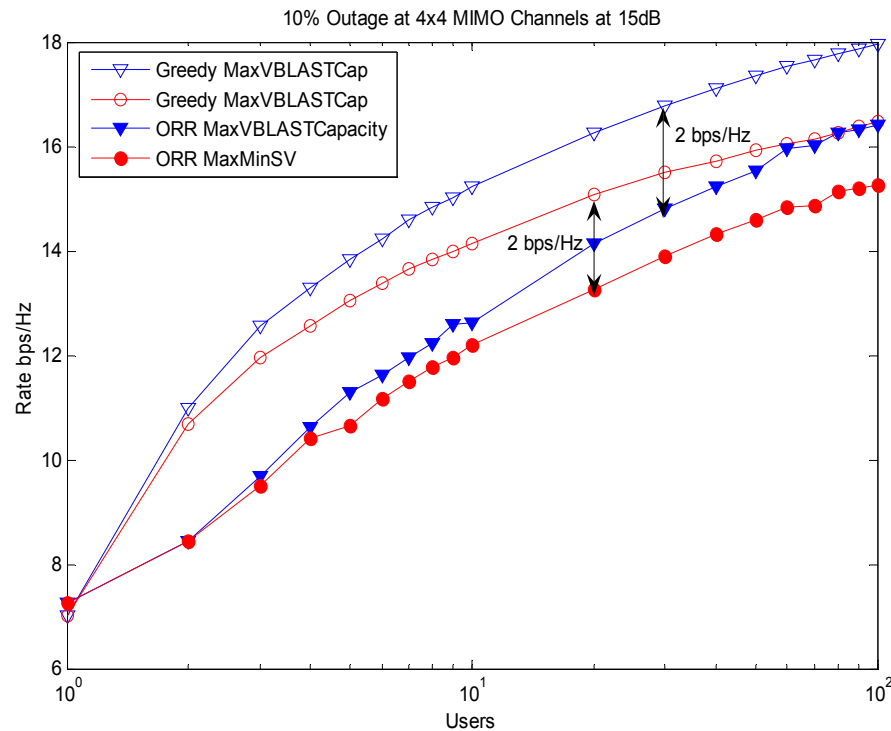
- The greedy algorithm selects the best user irrespective of other users.
- Fairness is considered in this work.
  - Opportunistic Round Robin
  - Proportional Fair

$$PF(\Psi) = \frac{\Psi}{T_k}$$

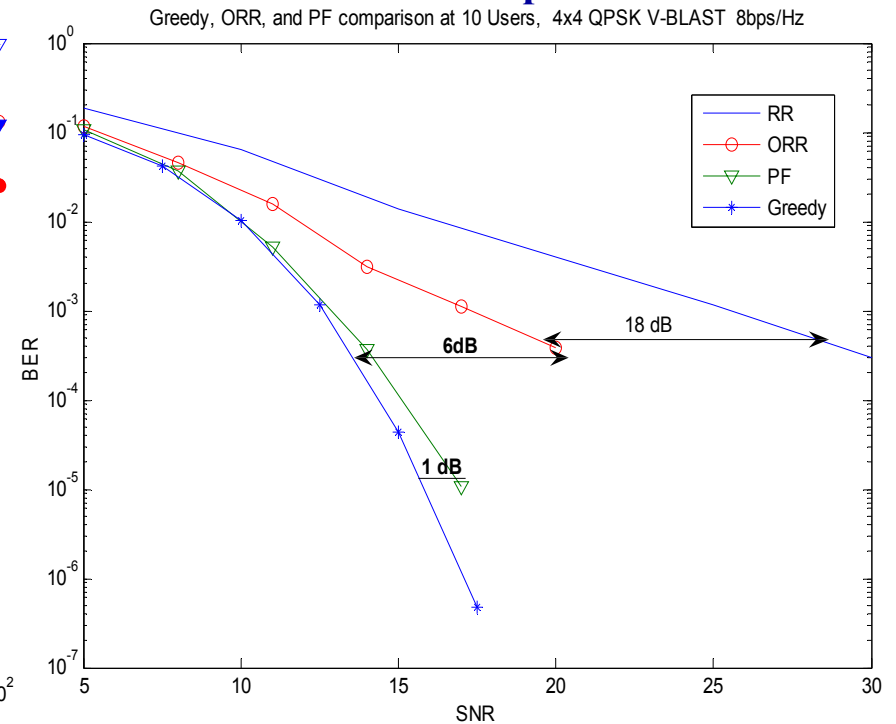


# Comparison: Greedy vs. ORR and PF

## 10% outage capacity comparison of Greedy and ORR schedulers over 4x4 MIMO channels and at SNR=15dB



## Greedy, PF and ORR at 10 users and over 4x4 MIMO Channels using MaxVBLASTCap scheduler



# Uplink MIMO-OFDM Scheduling

## Conclusions

- We presented and compare scheduling algorithms for MIMO-OFDM users based on V-BLAST scheme.
- We showed that scheduling based on maximum MIMO capacity doesn't work well for V-BLAST systems neither based on Maximum SNR.
- We compared several scheduling algorithms and found that MaxMinSV scheduling performs close to MaxVBLAST capacity scheduler.